

Article

A New Method for Impeller Inlet Design of Supercritical CO₂ Centrifugal Compressors in Brayton Cycles

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Abstract: Supercritical Carbon Dioxide (SCO₂) is considered as a potential working fluid in next generation power and energy systems. The SCO₂ Brayton cycle is advantaged with higher cycle efficiency, smaller compression work, and more compact layout, as compared with traditional cycles. When the inlet total condition of the compressor approaches the critical point of the working fluid, the cycle efficiency is further enhanced. However, the flow acceleration near the impeller inducer causes the fluid to enter two-phase region, which may lead to additional aerodynamic losses and flow instability. In this study, a new impeller inlet design method is proposed to achieve a better balance among the cycle efficiency, compressor compactness, and inducer condensation. This approach couples a concept of the maximum swallowing capacity of real gas and a new principle for condensation design. Firstly, the mass flow function of real gas centrifugal compressors is analytically expressed by non-dimensional parameters. An optimal inlet flow angle is derived to achieve the maximum swallowing capacity under a certain inlet relative Mach number, which leads to the minimum energy loss and a more compact geometry for the compressor. Secondly, a new condensation design principle is developed by proposing a novel concept of the two-zone inlet total condition for SCO₂ compressors. In this new principle, the acceptable acceleration margin (AAM) is derived as a criterion to limit the impeller inlet condensation. The present inlet design method is validated in the design and simulation of a low-flow-coefficient compressor stage based on the real gas model. The mechanisms of flow accelerations in the impeller inducer, which form low-pressure regions and further produce condensation, are analyzed and clarified under different operating conditions. It is found that the proposed method is efficient to limit the condensation in the impeller inducer, keep the compactness of the compressor, and maintain a high cycle efficiency.

Keywords: supercritical carbon dioxide; centrifugal compressor; impeller inlet design; maximum swallowing capacity; condensation

1. Introduction

Supercritical Carbon Dioxide (SCO₂) has superior thermodynamic properties such as high specific heat capacity, large isothermal compressibility, and small viscosity. A power generation system with SCO₂ as the working fluid usually needs smaller compression work and possesses higher cycle efficiency, as compared to a working fluid of superheated vapor [1]. Moreover, the density of SCO₂ is very large, leading to the benefit that the SCO₂ Brayton cycle is much more compact than the traditional Rankine cycle [2]. It is also known that the critical temperature of CO₂ (304.13 K) is lower than other

frequently-used working fluids. This makes the thermal cycle much easier to implement [3]. Due to the above advantages, SCO_2 Brayton cycles are widely used in nuclear energy systems [4], exhaust heat recovery systems [5], solar power systems [6], and geothermal energy systems [7], etc.

A centrifugal compressor is one of the key components in the SCO_2 Brayton cycle. When the compressor inlet fluid approaches its critical point, the compression work further decreases, and the cycle efficiency is additionally improved [8]. These benefits mainly come from the sharp increase of the isothermal compressibility of the working fluid near the critical point.

However, the aerothermodynamic properties of CO_2 near the critical point show severe nonlinear behaviors which significantly deviate from the perfect gas. The sharp variation of the fluid properties means larger uncertainty in experimental measurements and lower accuracy in numerical simulations for centrifugal compressors [9,10]. In recent years, a significant effort has been made to improve the reliability of numerical simulations for compressors running near the critical point. Ameli et al. [11] analyzed the sensitivity of the compressor aerodynamic performance and flow field with respect to the real gas models and operating conditions. A method was developed to overcome simulation difficulties. Baltadjiev et al. [12] presented a comprehensive assessment of real gas effects on the aerodynamic performance and rotor–stator matching of SCO_2 compressors. Kim et al. [13] carried out a three-dimensional numerical study for a SCO_2 compressor stage to obtain fundamental data for the design optimization near the critical point and in the supercritical state. More related studies can be found in the references [14,15].

On the other hand, if the inlet total condition of an SCO_2 compressor is very close to the critical point, the impeller inlet design could be much more difficult. Flow acceleration happens not only at the impeller inlet from stagnation condition to static one, but also at the inducer due to the suction side curvature of the blade leading edge. Since the acceleration may cause the fluid thermodynamic state to cross the saturation line, the fluid condensation (two-phase flow) is likely to occur [16]. The phase transition of the condensation brings about unsteady flow structures near the impeller inlet, which introduces instability and decreases the compressor efficiency. Pecnik et al. [17] carried out a three-dimensional CFD (computational fluid dynamics) study for a high-speed SCO_2 centrifugal compressor. Two-phase flow was captured in the suction side region of the full blade leading edge and in the wake-flow region near the impeller outlet. Baltadjiev et al. [12] defined a non-dimensional parameter to estimate the significance of two-phase flow effects. This parameter relates the time of liquid droplet formation to the residence time of the flow under saturation conditions.

To limit the condensation near the impeller inducer, design criteria have been developed. For example, Brenes [18] proposed a design criterion named acceleration margin to condensation (AMC), in which a large margin is reserved to avoid two-phase flow. AMC is a good criterion to select the proper inlet total condition, while it cannot be applied directly to the impeller design with a specified inlet condition. Shao et al. [19] introduced the inlet velocity ratio (IVR) to control the inlet condensation and, then, to define the impeller inlet geometry. However, IVR cannot explore the trade-off relationships among the non-dimensional impeller inlet parameters: the flow coefficients, the inlet relative Mach number, and the inlet flow angle. These parameters are closely related to the compressor flow capacity and aerodynamic loss.

To sum up, in the practice of SCO_2 compressor design, the inlet total condition should be close to the critical point in order to achieve a high cycle efficiency. On the other hand, to limit the condensation, the flow acceleration near the impeller inducer should be restricted. This means that for the specified mass flow rate, the cross-sectional area of the impeller inducer becomes relatively large. As a consequence, the compactness of the compressor deteriorates. The above analysis shows that the impeller inlet aerodynamic and geometrical parameters are coupled and interacted. In recent years, some preliminary design methods for SCO_2 compressors were developed by integrating the real gas model and the mean-line methods of air compressors [18,20]. However, those methods usually paid more attention to explore the impeller outlet parameters of SCO_2 compressors [19,21], and they cannot well cope with the interactions among impeller inlet parameters. Therefore, a new methodology

for aerothermodynamic design of real gas compressors is demanded, based on which the impeller inlet parameters could be explored to achieve a better balance between the inlet condensation and compressor compactness without losing the cycle efficiency.

The rest of this article is organized as follows. Firstly, the numerical simulation method for a SCO_2 compressor is validated. Secondly, a new impeller inlet design method is proposed, which couples a concept of the maximum swallowing capacity of real gas and a new design principle for condensation mitigation. Then, a low-flow-coefficient compressor stage is designed using this approach and, furthermore, simulated, and analyzed. Finally, some conclusions and remarks on future work are given.

2. Numerical Method Validation

As the final design scheme is assessed by the numerical simulation method, the CFD code for SCO_2 compressors is firstly validated based on the experimental data. In the following sub-sections, the thermodynamic properties of SCO_2 is discussed, and then the numerical method is presented and validated.

2.1. Thermodynamic Properties of SCO_2

For a specific substance, its critical temperature is defined as the highest temperature that can hold liquid–vapor equilibrium during phase change, and the corresponding pressure is termed the critical pressure. The gas and liquid states cannot coexist when the temperature is higher than the critical temperature. As shown in Figure 1, the thermodynamic properties of CO_2 near the critical point ($T_{\text{cr}} = 304.13 \text{ K}$, $p_{\text{cr}} = 7.38 \text{ MPa}$) are far away from perfect gas. A slight change of the pressure or temperature can cause great variation of the density and specific heat. In addition, the isolines of the thermodynamic properties show a sharp discontinuity when the fluid reaches the saturation lines.

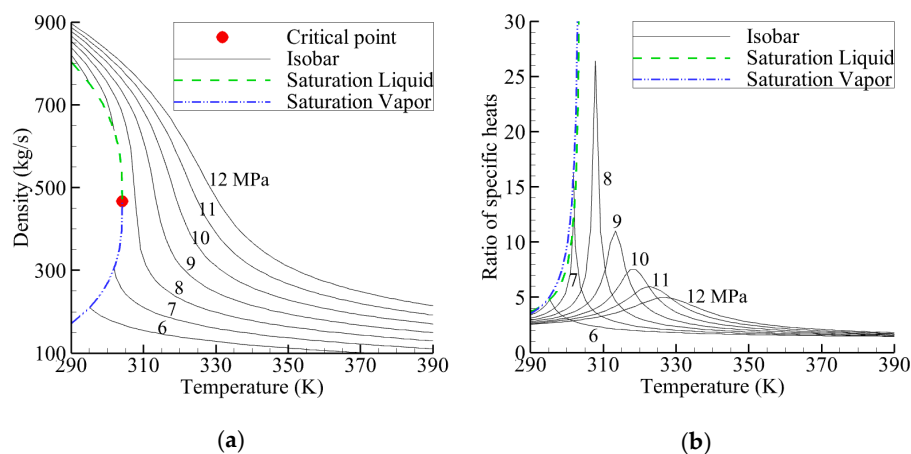


Figure 1. Thermodynamic properties of CO_2 versus temperature under different pressure: (a) Density; (b) Ratio of specific heats.

For the flow in compressors, the behavior of the working fluid along the whole compressor stage is far away from that of the perfect gas. Thus, the equations for the perfect gas (e.g., $p = \rho RT$, $a = \sqrt{\gamma RT}$ and $T_{t1}/T_1 = 1 + (\gamma - 1)M_{c1}^2/2$) are invalid for the preliminary design or numerical simulation of SCO_2 compressors. However, the mass, momentum, and energy conservations are independent of the fluid properties. Therefore, the flow in SCO_2 compressors is still governed by the Navier–Stokes equations. To complete the entire equation system, it is necessary to formulate the thermodynamic relations between the state variables (equation of state), and derive the viscosity coefficient and the thermal conductivity coefficient as functions of the state variables (transport properties). The transport properties are usually derived from the basic thermodynamic properties (such as temperature and density). Therefore, a suitable EOS (equation of state) of working fluid

should be firstly determined. A variety of EOS models exist with variable accuracy depending on the particular range of thermodynamic states of interest. For example, the Lee-Kesler (LK) model [22] is well-established and widely used in industry. The main advantage of the LK EOS model is to improve the accuracy of existing real gas models, particularly in the subcooled liquid and superheated vapor regions. The Span–Wagner (SW) model [23] is particularly developed for CO₂, whose accuracy is shown to be on the same order as the uncertainty of the experimental measurements.

However, the original SW model is inconvenient to be directly applied to thermodynamic calculation and numerical simulation due to hundreds of empirical coefficients. Hence, this state-of-the-art model is integrated into REFPROP (reference fluid thermodynamic and transport properties) [24] to reference properties of CO₂, supplemented by auxiliary models for the transport properties [25]. In this study, all required thermodynamic properties and their derivatives are generated based on the real gas database REFPROP to form an RGP (real gas property) table, which includes both the single-phase region and the vapor–liquid region. The general form of the function in REFPROP to create the RGP table is written as

$$y = f(x_1, x_2) \quad (1)$$

where y denotes $a, C_p, h, p, S, T, \gamma, \mu$ or ρ ; x_1 is h, p, T or ρ ; and x_2 stands for h, p, Q, S or ρ . The fundamental parameters for the RGP table are T and p .

2.2. Numerical Method for SCO₂ Compressor

The CFD code is validated based on the testing results of a Sandia SCO₂ centrifugal compressor [18,26], which includes an unshrouded impeller and a vaned diffuser. The geometrical parameters and flow boundary conditions of the compressor are listed in Table 1, and the solid model is given in Figure 2.

Table 1. Design parameters of the Sandia Supercritical Carbon Dioxide (SCO₂) compressor.

| Parameters | Values |
|--------------------------------|------------|
| Shaft speed | 59,584 rpm |
| Design mass flow rate | 2.609 kg/s |
| Number of full/splitter blades | 6/6 |
| Impeller tip diameter | 37.4 mm |
| Impeller outlet width | 1.8 mm |
| Impeller outlet blade angle | −50 deg |
| Tip clearance | 0.25 mm |
| Diffuser outlet diameter | 52 mm |
| Number of vanes | 17 |
| Inlet total pressure | 8.22 MPa |
| Inlet total temperature | 308.33 K |

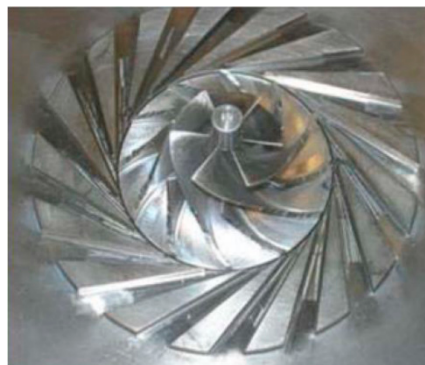


Figure 2. Solid model of the Sandia SCO₂ compressor.

The Reynolds-averaged Navier–Stokes equations are solved using NUMECA software suit (v10.2, NUMECA International, Brussels, Belgium). The $k - \omega$ SST (shear stress transport) turbulence model with an extended wall function is adopted to resolve turbulence, which can provide high-accurate results for the three-dimensional flow with strong pressure gradients, moderate curvature, and flow separation [27]. The approach of conservative coupling by pitchwise rows is adopted to deal with the rotor–stator interface of the compressor stage. This approach is capable to provide an exact conservation of mass flow, momentum, and energy through the interface. The spatial discretization used for the computation is a central scheme with artificial viscosity, and the time integration scheme is an explicit four-step Runge–Kutta algorithm. The residual smoothing, local time stepping, and multi-grid scheme are employed to accelerate the convergence.

A structured mesh with H-O-I topology is selected for the Sandia SCO₂ compressor. The size of the first cell to the wall y_{wall} is estimated by a truncated series solution of the Blasius equation as [28]

$$y_{\text{wall}} = 6 \left(\frac{c_{\text{ref}}}{\nu} \right)^{-7/8} \left(\frac{L_{\text{ref}}}{2} \right)^{1/8} y^+ \quad (2)$$

where, c_{ref} is the reference velocity and it is usually specified as the impeller inlet velocity, ν represents the kinematic viscosity of fluid, L_{ref} is the reference length and it is often specified as the impeller inlet blade height, and y^+ denotes the non-dimensional distance of first cell to the wall.

Since the kinematic viscosity of SCO₂ is quite small (the fluid density is very large while the dynamic viscosity is small), the Reynolds number of flows in SCO₂ compressor is very high. For high-Reynolds number condition, the recommended y^+ range of $k - \omega$ SST turbulence model (with an extended wall function) is between 20–50 [28]. In this extended wall function, the turbulent kinetic energy and the turbulent dissipation rate are fitted with polynomials to the DNS (direct numerical simulation) data [29]. Therefore, it allows to accurately solve the turbulence properties in the near wall region when the y^+ is in the recommended range. Here, $y^+ \approx 30$ is selected for the Sandia SCO₂ compressor and this value is also adopted by many other studies for SCO₂ compressor simulations [13,30,31]. According to Equation (2), the first cell to the wall is $y_{\text{wall}} = 3 \times 10^{-6}$ m.

Another frequently-used strategy to simulate the flow field of SCO₂ compressor is the $k - \omega$ SST turbulence model (no wall functions) with quite small y^+ (close to unity) [17,27]. In our study, however, due to the extremely small kinematic viscosity of SCO₂, a small value of y^+ will lead to a quite small grid size near the wall ($y^+ = 1$, $y_{\text{wall}} = 1 \times 10^{-7}$ m). As a consequence, the aspect ratio of grid cells near the wall would be very large (more than 10^4), which might result in a low-accuracy simulation in boundary layers due to the large numerical dissipation of poor-quality mesh. In order to improve the mesh quality, much more grid nodes should be added in the computational domain, and this would greatly increase the computational effort.

Our numerical tests show that the extended wall function approach ($y^+ = 30$, $y_{\text{wall}} = 3 \times 10^{-6}$ m, maximum aspect ratio is 350, total mesh is 2.69 million) can provide more accurate results (compared to experimental results) than the case without wall function ($y^+ = 1$, $y_{\text{wall}} = 1 \times 10^{-7}$ m, maximum aspect ratio is above 10^4 , same total mesh). Hence, the extended wall function method might be a better way to balance the computational effort and simulation accuracy when predicting condensation in impeller leading edge of SCO₂ compressors.

A baseline RGP table is preliminarily generated by cubic spline interpolation with 101 samples in the temperature range 216.6–1000 K and the pressure range 1–80 MPa (see Table 2). Based on the baseline RGP table, the mesh independency investigation is firstly conducted by coarse, medium, and fine meshes with total cell numbers of 1.75, 2.69, and 3.70 million, respectively (for a single passage of the impeller and vaned diffuser). It is clear from Figure 3a that the medium mesh seems to provide a good compromise between the accuracy and computational effort. Hence, this mesh (see Figure 4) is used for the rest of simulations.

Table 2. Four types of RGP tables with the corresponding maximum Courant–Friedrichs–Lewy (CFL) numbers to achieve a convergent solution under design condition.

| RGP | p (MPa) | T (K) | Samples | Max CFL | Running Time (hour) |
|----------|-----------|------------|---------|---------|---------------------|
| Baseline | 1–80 | 216.6–1000 | 101 | 0.1 | 9 |
| RGP-1 | 1–40 | 220–600 | 101 | 0.05 | 14 |
| RGP-2 | 1–40 | 220–600 | 301 | 0.05 | 16 |
| RGP-3 | 1–40 | 220–600 | 901 | 0.01 | 58 |

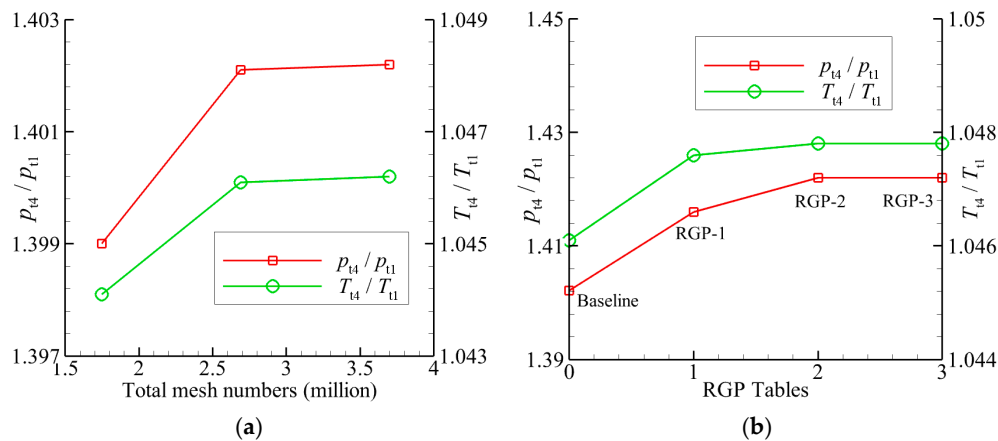


Figure 3. Independency study of the meshes and real gas property (RGP) resolution: (a) Mesh independency; (b) RGP resolution.

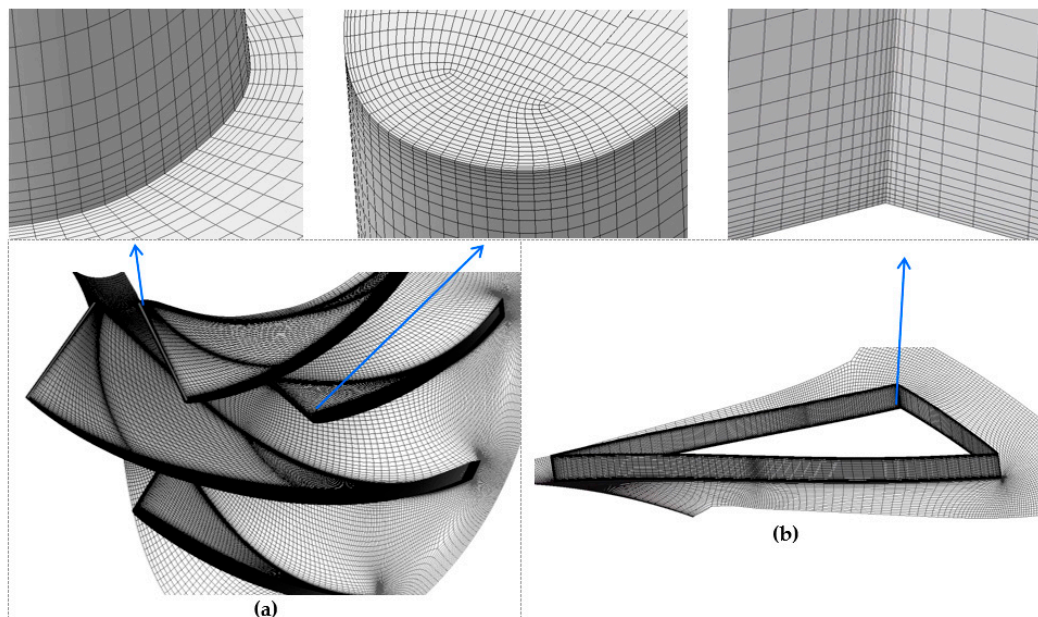


Figure 4. Computational meshes of the impeller and vaned diffuser: (a) Impeller; (b) Vaned diffuser.

On the other hand, the resolution of the RGP table may have a large effect on simulation results, since the fluid state is close to the critical point at the impeller inducer and its thermodynamic properties show a severe nonlinearity. Theoretically, more samples of the RGP table (higher resolution) will contribute to a higher accuracy of simulation. Nonetheless, this may significantly decrease the calculation stability. A smaller CFL (Courant–Friedrichs–Lewy) number is required for an RGP table with higher resolution.

Table 2 gives the other three RGP tables in addition to the baseline table, in which the resolution shows an upward trend. The fifth column of the table shows the corresponding maximum CFL

numbers to achieve a convergent solution under the same initial value for design mass flow rate. In order to clearly compare the computational effort, the required total running time of different RGP tables is also illustrated in the table. Each simulation was conducted parallelly on a workstation with a 24-core processor (Xeon(R) E5-2670 v3 2.3 GHz) and 64GB RAM (random-access memory), and the CPU (central processing unit) and RAM utilizations were about 80% and 45%, respectively.

Figure 3b illustrates the effects of the RGP resolution on the compressor performance. It is clear from the figure that the aerodynamic performance is much more sensitive to the resolution of the RGP table than to the mesh size. From Table 2 and Figure 3b, it is found that compared to RGP-2, RGP-3 introduces limited improvement for the simulation accuracy but greatly increases the computational time. Therefore, RGP-2 achieves a good balance between the numerical accuracy and computational time, and this RGP table is selected for the remaining studies.

Table 3 shows the comparison of the predicted and measured aerodynamic performance of the SCO₂ compressor based on the medium mesh and RGP-2. Generally, the prediction matches the measurement well under low-speed operating conditions ($\leq 56,000$ rpm). For high-speed conditions, the maximum relative error is about 5.8%, which is acceptable for SCO₂ compressor simulation [17]. Table 3 confirms the accuracy of the present numerical method.

Table 3. Comparison of the predicted and measured total pressure ratio of the Sandia SCO₂ compressor at diffuser outlet.

| Shaft Speed (rpm) | Inlet Total Temperature (K) | Inlet Total Pressure (MPa) | Mass Flow Rate (kg/s) | Experimental Total Pressure Ratio | Calculated Total Pressure Ratio | Error (%) |
|-------------------|-----------------------------|----------------------------|-----------------------|-----------------------------------|---------------------------------|-----------|
| 10,000 | 305.5 | 76.76 | 0.454 | 1.039 | 1.046 | 0.675 |
| 20,000 | 305.5 | 76.76 | 0.771 | 1.051 | 1.060 | 0.886 |
| 28,000 | 305.5 | 76.76 | 1.134 | 1.112 | 1.106 | 0.517 |
| 29,888 | 306.78 | 79.2 | 1.315 | 1.082 | 1.093 | 1.035 |
| 39,000 | 305.6 | 77.11 | 1.451 | 1.204 | 1.228 | 1.999 |
| 49,000 | 306.3 | 78.54 | 1.816 | 1.355 | 1.394 | 2.885 |
| 55,000 | 306.4 | 78.9 | 2.043 | 1.439 | 1.469 | 2.085 |
| 56,000 | 306.6 | 78.26 | 2.088 | 1.469 | 1.467 | 0.133 |
| 59,584 | 308.33 | 82.24 | 2.609 | 1.365 | 1.422 | 4.176 |
| 60,000 | 306.9 | 79.97 | 2.225 | 1.518 | 1.596 | 5.108 |
| 64,384 | 308.71 | 82.86 | 2.86 | 1.441 | 1.516 | 5.222 |
| 64,900 | 307.9 | 82.11 | 2.406 | 1.574 | 1.666 | 5.824 |

The main advantages of the confirmed numerical method are (1) the independency studies of the meshes and RGP resolution are implemented, which can minimize the errors from unreasonable mesh density and unreal thermodynamic properties of working fluid; (2) the $k - \omega$ SST turbulence model with an extended wall function is discussed in more detail, and it might be a better approach to balance the computational effort and simulation accuracy when predicting condensation in impeller leading edge of SCO₂ compressors.

3. Impeller Inlet Design Method

In order to prevent the inlet condensation and keep the compressor geometrical compactness but remain the high cycle efficiency, a new method of designing impeller inlet is proposed for SCO₂ compressors. This method is made up of the maximum swallowing capacity concept of real gas and a new condensation design principle.

3.1. Maximum Swallowing Capacity

In centrifugal compressor, the mass flow function Φ is usually used to assess the flow capacity of an impeller [32], and it is defined as

$$\Phi = \frac{\dot{m}}{\rho_{t1} D_2^2 a_{t1}} \quad (3)$$

The equation of continuity at the impeller inlet is written as

$$\dot{m} = \rho_1 A_1 c_{1m} \quad (4)$$

Using the definition of the impeller inlet shape factor $k = 1 - (D_{1h}/D_{1s})^2$, the impeller inlet area A_1 is

$$A_1 = \frac{\pi}{4}(D_{1s}^2 - D_{1h}^2) = \frac{\pi}{4}kD_{1s}^2 \quad (5)$$

For constant angular velocity, the diameter ratio equals the blade speed ratio as

$$\frac{D_{1s}}{D_2} = \frac{u_{1s}}{u_2} \quad (6)$$

Substituting Equations (4)–(6) into Equation (3) yields

$$\Phi = \frac{\pi k \rho_1 u_{1s}^2 c_{1m}}{4 \rho_{t1} u_2^2 a_{t1}} \quad (7)$$

From the impeller inlet velocity triangle (see Figure 5), we obtain

$$c_1 = \frac{c_{1m}}{\cos \alpha_1}; \quad c_{1m} = w_{1s} \cos \beta_{1s}; \quad u_{1s} = w_{1s} \cos \beta_{1s} (\tan \beta_{1s} + \tan \alpha_1) \quad (8)$$

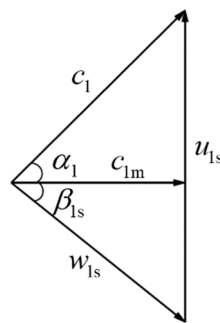


Figure 5. The impeller inlet velocity triangle near the shroud.

Substituting Equation (8) into Equation (7) yields

$$\begin{aligned} \Phi &= \frac{\pi k \rho_1 w_{1s}^2 \cos^2 \beta_{1s} (\tan \beta_{1s} + \tan \alpha_1)^2 w_{1s} \cos \beta_{1s}}{4 \rho_{t1} u_2^2 a_{t1}} \\ &= \frac{\pi k \rho_1 a_1^3 w_{1s}^3 a_{t1}^2}{4 \rho_{t1} a_{t1}^3 a_1^3 u_2^2} \cos^3 \beta_{1s} (\tan \beta_{1s} + \tan \alpha_1)^2 \\ &= \frac{\pi k M_{w1}^3 \rho_1 a_1^3}{4 M_{u2}^2 \rho_{t1} a_{t1}^3} \cos^3 \beta_{1s} (\tan \beta_{1s} + \tan \alpha_1)^2 \end{aligned} \quad (9)$$

The above equations are derived based on the fundamental theories of turbomachinery, and they are independent of fluid properties.

For Equation (9), the remaining task is to crystallize ρ_1/ρ_{t1} and a_1^3/a_{t1}^3 . In the case of a perfect gas, it is easy to give their specific equations based on aerodynamic correlations. However, for a real gas case especially near the critical point, these equations would be much more complicated.

According to the reference [33], the relations between the static parameters and total ones for a real gas case are written as

$$\begin{aligned} \frac{p}{p_t} &= \left(1 + \frac{n_s-1}{2} M^2\right)^{-\frac{n_s}{n_s-1}} \\ \frac{\rho}{\rho_t} &= \left(1 + \frac{n_s-1}{2} M^2\right)^{-\frac{1}{n_s-1}} \end{aligned} \quad (10)$$

where n_s is the isentropic exponent. It can be derived from the fundamental equations of thermodynamics as

$$n_s = \frac{\gamma}{\beta_T p} \quad (11)$$

where the specific heat ratio γ and the isothermal compressibility β_T are

$$\begin{aligned} \gamma &= \frac{C_p}{C_v} = \left(\frac{\partial p}{\partial v} \right)_s / \left(\frac{\partial p}{\partial v} \right)_T \\ \beta_T &= -\frac{1}{v} \left(\frac{\partial v}{\partial p} \right)_T \end{aligned} \quad (12)$$

It is clear from Equation (11) that in the case of the real gas, the isentropic exponent n_s is no longer equal to the specific heat ratio γ . The n_s also involves the isothermal compressibility β_T in addition to the γ , which is significantly different from the perfect gas.

Note that in the derivation of Equation (10), it assumes that the isentropic exponent remains constant from the total to static conditions ($n_{s,t} = n_s$). This assumption is reasonable when the fluid state (both total and static) is not close to the critical point. In this case, the variations in n_s are small enough such that an average value between the total and static conditions can be used.

The speed of sound for the real gas under the static and total conditions can be respectively written as

$$a = \sqrt{n_s \frac{p}{\rho}}; \quad a_t = \sqrt{n_{s,t} \frac{p_t}{\rho_t}} \quad (13)$$

Substituting Equation (10) into Equation (13) yields

$$\frac{a}{a_t} = \left(1 + \frac{n_s - 1}{2} M^2 \right)^{-\frac{1}{2}} \quad (14)$$

Concretely, substituting the impeller inlet parameters into Equations (10) and (14), and replacing the absolute Mach number by the relative one using Equation (8) yields

$$\begin{aligned} \frac{\rho_1}{\rho_{t1}} &= \left(1 + \frac{\bar{n}_{s1} - 1}{2} M_{w1}^2 \frac{\cos^2 \beta_{1s}}{\cos^2 \alpha_1} \right)^{-\frac{1}{\bar{n}_{s1} - 1}} \\ \frac{a_1}{a_{t1}} &= \left(1 + \frac{\bar{n}_{s1} - 1}{2} M_{w1}^2 \frac{\cos^2 \beta_{1s}}{\cos^2 \alpha_1} \right)^{-\frac{1}{2}} \end{aligned} \quad (15)$$

where \bar{n}_{s1} is an average value between the total and static conditions of the impeller inlet. It reads

$$\bar{n}_{s1} = \frac{1}{2} \left(\frac{\gamma_{t1}}{\beta_{T,t1} p_{t1}} + \frac{\gamma_1}{\beta_{T,1} p_1} \right) \quad (16)$$

Substituting Equation (15) into Equation (9) yields

$$\Phi = \frac{\pi k M_{w1}^3}{4 M_{u2}^2} \frac{\cos^3 \beta_{1s} (\tan \beta_{1s} + \tan \alpha_1)^2}{\left(1 + \frac{\bar{n}_{s1} - 1}{2} M_{w1}^2 \frac{\cos^2 \beta_{1s}}{\cos^2 \alpha_1} \right)^{\frac{3}{2} + \frac{1}{\bar{n}_{s1} - 1}}} \quad (17)$$

It is clear from Equation (17) that the mass flow function Φ can be generally expressed as the function of the non-dimensional parameters such as M_{w1} , M_{u2} , β_{1s} , and α_1 .

Eliminating the machine Mach number M_{u2} in Equation (17) yields the modified mass flow function Φ' as

$$\Phi' = \frac{4M_{u2}^2}{\pi k} \Phi = \frac{M_{w1}^3 \cos^3 \beta_{1s} (\tan \beta_{1s} + \tan \alpha_1)^2}{\left(1 + \frac{\bar{n}_{s1}-1}{2} M_{w1}^2 \frac{\cos^2 \beta_{1s}}{\cos^2 \alpha_1}\right)^{\frac{3}{2} + \frac{1}{\bar{n}_{s1}-1}}} \quad (18)$$

Equation (18) contains four parameters (M_{w1} , β_{1s} , α_1 , and \bar{n}_{s1}), but only M_{w1} and β_{1s} are independent variables. The prewhirl angle α_1 is usually specified as a constant. Additionally, the inlet total condition is often given at the preliminary design phase for a compressor, leading to a determined value of \bar{n}_{s1} . Therefore, from Equation (18) it is possible to achieve the maximum swallowing capacity (maximum Φ') of the SCO₂ compressor under a certain inlet velocity (specified M_{w1}).

In Equation (18), letting $\partial\Phi'/\partial\beta_{1s} = 0$. This yields the criterion of the maximum swallowing capacity as

$$\cos \beta_{1s} = \sin \beta_{1s} \tan \alpha_1 + \frac{1}{3 \cos \beta_{1s}} + \frac{M_{w1}^2}{3 \cos^2 \alpha_1} (\cos^3 \beta_{1s} - \tan \alpha_1 \cos^2 \beta_{1s} \sin \beta_{1s} - \bar{n}_{s1} \cos \beta_{1s}) \quad (19)$$

Equation (19) is expressed in an implicit form, and the iteration method is used to solve this criterion. If the prewhirl angle α_1 is zero (axial inlet), the Equations (17)–(19) are simplified to be

$$\Phi = \frac{\pi k M_{w1}^3}{4 M_{u2}^2} \frac{\cos \beta_{1s} \sin^2 \beta_{1s}}{\left(1 + \frac{\bar{n}_{s1}-1}{2} M_{w1}^2 \cos^2 \beta_{1s}\right)^{\frac{3}{2} + \frac{1}{\bar{n}_{s1}-1}}} \quad (20)$$

$$\Phi' = \frac{M_{w1}^3 \cos \beta_{1s} \sin^2 \beta_{1s}}{\left(1 + \frac{\bar{n}_{s1}-1}{2} M_{w1}^2 \cos^2 \beta_{1s}\right)^{\frac{3}{2} + \frac{1}{\bar{n}_{s1}-1}}} \quad (21)$$

$$\cos \beta_{1s} = \frac{\sqrt{\bar{n}_{s1} M_{w1}^2 + 3} + 2M_{w1} - \sqrt{\bar{n}_{s1} M_{w1}^2 + 3} - 2M_{w1}}{2M_{w1}} \quad (22)$$

The modified mass flow function Φ' is plotted over β_{1s} for a series of M_{w1} at two different values of prewhirl angle ($\alpha_1 = 0$ deg and 30deg) in Figure 6. It shows that for a given M_{w1} , there exists an optimal β_{1s} leading to the maximum swallowing capacity (maximum Φ'). In other words, for a specified flow capacity (given Φ'), there is a certain β_{1s} corresponding to the minimum M_{w1} . It is widely recognized that reducing M_{w1} is one of the most important design objectives for high speed compressors since it can minimize the passage aerodynamic losses and improve the isentropic efficiency. On the other hand, M_{w1} is related to the fluid acceleration at impeller inlet. Thus, restricting M_{w1} may help limit the condensation near the impeller inducer, which is a special design criterion for SCO₂ compressors.

Therefore, the maximum swallowing capacity concept for impeller inlet design has the potential to balance the inlet condensation and compressor compactness while maintain the cycle efficiency. At the preliminary design phase, the parameters Φ , M_{u2} , α_1 and \bar{n}_{s1} can be usually predefined based on the design specification, and the variables k , M_{w1} , and β_{1s} are expected to be determined. However, there are only two independent Equations (17) and (19) for the above three unknown variables, for which an additional equation should be supplemented. As a matter of fact, the condensation design principle in the next subsection tends to provide this equation.

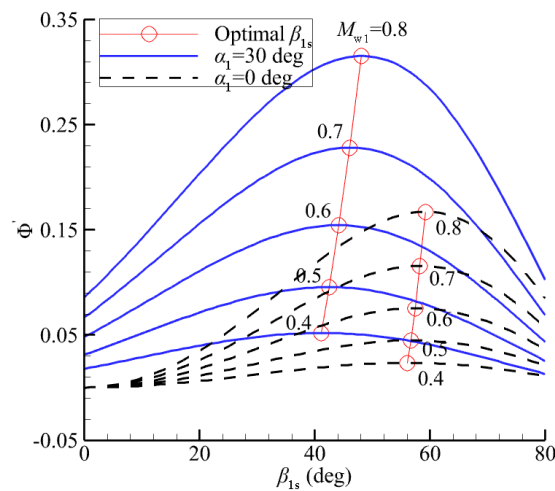


Figure 6. Modified mass flow function Φ' versus inlet flow angle β_{1s} for centrifugal impellers with different prewhirl angles based on Equations (18) and (19), where $\bar{n}_{s1} = 1.529$.

3.2. Condensation Design Principle

Though the total condition at the impeller inlet is located in the supercritical region, the flow acceleration at the impeller inducer may cause the local static properties of the fluid to enter the two-phase region (reach or cross the saturation line). As a result, the aerodynamic losses will increase since the two-phase fluid will break the original flow structures. Meanwhile, the flow becomes unstable due to the sharp discontinuity of the fluid properties near the saturation line. The term “condensation” in this study is not limited to represent the change of the physical state of a fluid from the gas phase into the liquid phase. This term is generalized to deal with the fluid reaching or crossing the saturation line (including the condensation and vaporization), which will be further explained in Figure 7.

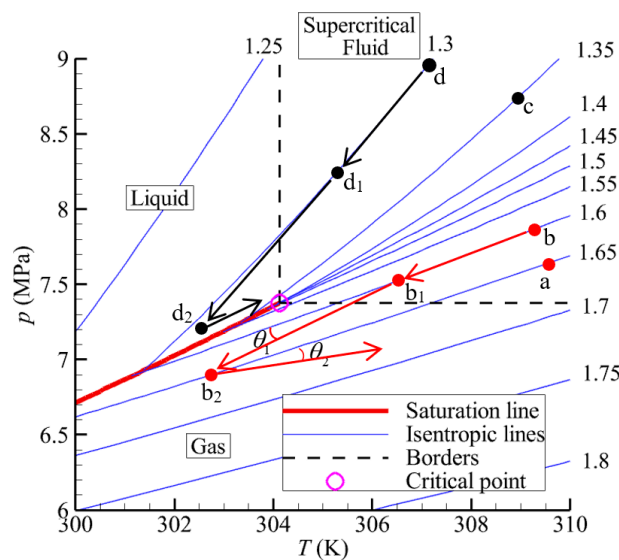


Figure 7. Expansion process of SCO_2 near impeller inlet.

In order to limit the condensation near the impeller inlet, an effective and objective indicator should be firstly defined to estimate the probability of entering the condensation. The inlet absolute Mach number M_{c1} represents the degree of the fluid expansion from the total to static conditions (the first

acceleration). This parameter is selected as the indicator of potential condensation. Further, M_{c1} is linked to the inlet relative Mach number M_{w1} as follows

$$M_{w1} = \frac{M_{c1} \cos \alpha_1}{\cos \beta_{1s}} \quad (23)$$

Equation (23) is actually the third independent equation for the impeller inlet design in addition to Equations (17) and (19). Therefore, if we can determine a reasonable value of M_{c1} , it is possible to limit the inlet condensation and achieve a compact compressor design simultaneously. Here, it is assumed that M_{c1} is the function of the impeller inlet total condition as

$$M_{c1} = g(T_{t1}, p_{t1}) \quad (24)$$

The remaining task is to determine the specific form of the function g in Equation (24).

Now, we consider the expansion process at the impeller inlet. As shown in Figure 7, the red thick line is the saturation line, and the blue lines are the isentropic lines, for which the clockwise direction indicates increasing entropy. The pink hollow circle is the critical point. The whole region is divided into three parts: gas, liquid, and supercritical fluid.

Taking point b as an example: point b represents the total condition, point b_1 is the corresponding static state. At the impeller inlet, point b reaches point b_1 through the isentropic expansion along the isentropic line (the first acceleration), and the red arrow shows the changing direction. Then, due to the contraction of the impeller inducer area and the curvature of the blade leading edge, the flow will further accelerate from point b_1 to point b_2 (the second acceleration). This expansion process is nearly adiabatic rather than isentropic. Therefore, the changing direction deviates from the isentropic line and points to a region with larger entropy, and the deviation angle $\theta_1 > 0$. Finally, as the fluid flows through the impeller passage, both pressure and temperature increase along the passage. The entropy of this process rises, and the corresponding deviation angle $\theta_2 > 0$.

Point d shows a similar process as point b illustrated above. However, the results of the two cases are completely different. From point b_1 to point b_2 , and further to a downstream point, the fluid moves away from the saturation line. In contrast, from point d_1 to point d_2 , and further to a downstream point, the fluid gets close to the saturation line. The moving trends indicate that point d is more likely stuck in the two-phase region than point b .

Therefore, the supercritical inlet total conditions for the SCO_2 compressor should be split into two zones: Zone I and Zone II. Zone I contains the points a and b , which expand isentropically to the saturation line through the gas region, whereas Zone II comprises the points c and d , which go through the liquid region. The two types of inlet total conditions have the opposite directions to cross the saturation line and then enter the two-phase region (Zone I for condensation and Zone II for vaporization). Hence, different measures should be taken to limit two-phase flow for the two cases. Note that there is not phase change when the fluid crosses the border lines (dashed lines in Figure 7), since the isolines of thermodynamic properties (like isobar and isentropic lines) are continuous from supercritical fluid to gas or liquid.

Here, a simple procedure is proposed to judge the type of a specific inlet total condition (T_{t1}, p_{t1}) as follows:

Procedure I

(1) Obtain the total entropy $S_{t1} = f(T_{t1}, p_{t1})$ according to Equation (1); from the total to static condition through the isentropic expansion, the static entropy equals the total one $S_1 = S_{t1}$.

(2) Assume that it reaches the critical temperature through the isentropic expansion, then the corresponding reference pressure is $p_{ref} = f(T_{cr}, S_1)$.

(3) Compare the reference pressure p_{ref} and the critical pressure p_{cr} , if $p_{ref} > p_{cr}$, the point is in Zone II, otherwise, the point belongs to Zone I.

Supposing that the fluid does not enter the two-phase region, the maximum degree of the isentropic expansion is to reach the saturation line. The maximum achievable Mach number in this expansion process, called MAM (maximum acceleration margin), is used to represent the degree of the expansion. In essence, MAM can be considered as an equivalent distance between the inlet total condition and the saturation line. Obviously, the impeller inlet absolute Mach number M_{c1} is smaller than MAM.

Here, an algorithm is given to obtain MAM for a specified inlet total condition (T_{t1}, p_{t1}) , and the procedure is:

Procedure II

(1) Obtain the total entropy $S_{t1} = f(T_{t1}, p_{t1})$ according to Equation (1); from the total condition to the saturation line through the isentropic expansion, the static entropy equals the total one $S_1 = S_{t1}$.

(2) Use Procedure I to judge the type of the total condition, if it is in Zone I, $Q = 1$; Otherwise, $Q = 0$.

(3) Set an initial temperature range $[T_{1,lower}, T_{1,upper}]$, the recommended values for $T_{1,lower}$ and $T_{1,upper}$ are 216.6 K and 304.13 K, respectively.

(4) Guess the value of temperature $T_{1,g} = (T_{1,lower} + T_{1,upper})/2$.

(5) Calculate corresponding values of entropy $S_{1,g} = f(T_{1,g}, Q)$, $S_{1,lower} = f(T_{1,lower}, Q)$.

(6) Check the error between S_1 and $S_{1,g}$, if it meets the minimum error criterion, then $T_1 = T_{1,g}$, go to the next step; otherwise, update the temperature range by the following rule:

{if $(S_{1,g} - S_1)(S_{1,lower} - S_1) < 0$, then $T_{1,upper} = T_{1,g}$, else $T_{1,lower} = T_{1,g}$ }, and go back to step (4).

(7) Calculate the total enthalpy $h_{t1} = f(T_{t1}, p_{t1})$, the static enthalpy $h_1 = f(T_1, Q)$, the speed of sound $a_1 = f(T_1, Q)$, the fluid velocity $c_1 = \sqrt{2(h_{t1} - h_1)}$, and the Mach number $M_{c1} = c_1/a_1$. Here M_{c1} is the MAM corresponding to the given total condition.

Based on Procedure II, MAM versus the impeller inlet total condition is plotted in Figure 8a. As shown in the figure, a severe nonlinear relationship between MAM and the total pressure under certain temperature is observed. The inflection points of those isotherms appear at higher pressure regions when the temperature increases. The value of MAM should be as high as possible in order to avoid two-phase flow at the impeller throat. At the same time, however, the cycle efficiency is reduced since the impeller inlet total condition is now far away from the critical point. According to the correlation between the cycle efficiency and the inlet total condition [18], $0.4 \leq \text{MAM} \leq 0.6$ seems to be an acceptable range to balance the performance and condensation. In fact, MAM provides an alternative criterion to select the suitable inlet total condition, while it cannot be directly applied to the impeller inlet design with specified total condition.

Here, a more practical criterion for impeller inlet design is proposed: AAM (acceptable acceleration margin), which is an acceptable Mach number to limit condensation at impeller throat. AAM is defined as

$$\text{AAM} = \lambda \times \text{MAM} \quad (25)$$

For a given inlet total condition, MAM is uniquely determined by procedure II, the remaining task is to find the empirical coefficient λ .

As illustrated in Figure 7, the flow near impeller leading edge will be further accelerated (the second acceleration) in addition to the acceleration from total to static condition (the first acceleration). According to the area ratio of throat-to-inlet, and local curvature of the blade leading edge, this second acceleration is about 2 times compared to the first acceleration. Assuming that after further acceleration, the fluid just reaches the saturation line, then the local Mach number equals MAM. Thus, AAM should be 0.5 times of MAM ($\lambda = 0.5$). As analyzed in Figure 7, the condensation is more likely to take place for Zone II than Zone I. Therefore, a more conservative value of λ is selected for Zone II. The following expression is recommended for λ as

$$\lambda = \begin{cases} 0.5, & \text{total condition} \in \text{Zone I} \\ 0.3, & \text{total condition} \in \text{Zone II} \end{cases} \quad (26)$$

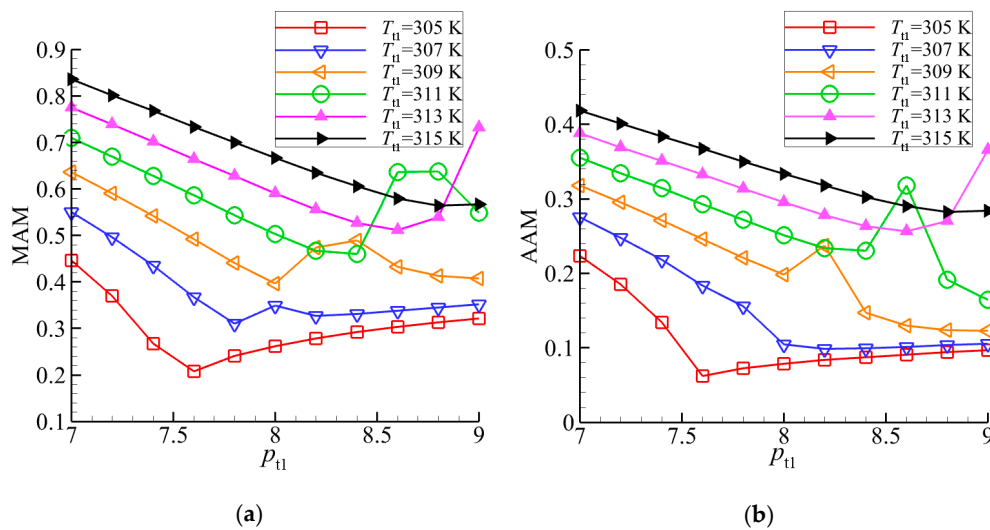


Figure 8. MAM and AAM as the functions of total pressure and temperature at impeller inlet: (a) MAM; and (b) AAM.

The AAM versus impeller inlet total condition is plotted in Figure 8b, and the patterns of isotherms in the figure are similar to Figure 8a. By checking Figure 8b, we can quickly obtain AAM for a certain inlet condition.

In order to limit condensation, the impeller inlet absolute Mach number M_{c1} should meet the criterion as

$$M_{c1} = g(T_{t1}, p_{t1}) \leq \text{AAM} \quad (27)$$

In design practice, M_{c1} is selected based on the above equation.

At this point, all equations for impeller inlet design have been derived. By combining Equations (17), (19), (23) and (27), the key parameters such as k , M_{w1} , and β_{1s} are determined, which are able to limit the impeller condensation and achieve a compact compressor while maintain a high cycle efficiency.

To validate the condensation design principle, a method is proposed to detected fluid condensation based on the impeller inlet total condition (T_{t1}, p_{t1}) and the local flow parameters (T, p, ρ). For the detection of a certain point, the procedure is:

Procedure III

(1) Use Procedure I to judge the type of the impeller inlet total condition, if it is in Zone I, $Q = 1$; Otherwise, $Q = 0$.

(2) Assume that the local flow parameters T, p, ρ are known. If $T \geq T_{cr}$, then the point is not in condensation, stop the procedure; otherwise, go next.

(3) Get reference pressure $p_{ref} = f(T, Q)$ and reference density $\rho_{ref} = f(T, Q)$.

(4) If ($Q = 1$ and $p \geq p_{ref}$ and $\rho \geq \rho_{ref}$) or ($Q = 0$ and $p \leq p_{ref}$ and $\rho \leq \rho_{ref}$), then the point is in condensation; otherwise, the point is not in condensation; stop the procedure.

Note that Procedure III assumes that condensation occurs suddenly as soon as the fluid reaches the saturation line, and this process has no delay. The heterogeneous nucleation on the passage wall and the homogeneous nucleation into the stream bulk are ignored.

4. Design Method Validation

A low-flow-coefficient SCO_2 compressor stage is designed based on the inlet design method, and the flow field is simulated and analyzed to verify the effectiveness of the design approach.

4.1. Preliminary Design and Numerical Simulation

The design specification is given in Table 4. Based on the stage aerodynamic performance, the total pressure ratio and isentropic efficiency of the impeller are estimated as $\varepsilon_i = 2, \eta_i = 88.5\%$. According to the inlet total condition, MAM is calculated by Procedure II and yields 0.4514, which is in the recommended range between 0.4 and 0.6. This means that the inlet total condition can achieve a high cycle efficiency. From Procedure I, we find that the inlet total condition belongs to Zone I, thus the empirical coefficient $\lambda = 0.5$ in Equation (26). By combining Equations (17), (19), (23), and (27), the key parameters of the optimal impeller inlet are obtained, and they are listed in Table 5 (the second column, Optimal Design). The inlet relative Mach number M_{c1} of the optimal design is selected as $M_{c1} = 0.92 \times \text{AAM}$.

Table 4. Design specification of the SCO_2 compressor stage.

| Parameters | Values |
|-----------------------------|------------|
| Shaft speed | 40,000 rpm |
| Design mass flow rate | 5 kg/s |
| Stage isentropic efficiency | >78% |
| Stage total pressure ratio | >1.8 |
| Inlet total temperature | 310 K |
| Inlet total pressure | 8 MPa |
| Inlet prewhirl angle | 0 deg |

Table 5. Preliminary design parameters of the three design schemes: Optimal Design, Reference Design I, and Reference Design II.

| Parameters | Optimal Design | Reference Design I | Reference Design II |
|---------------------------------------|----------------|--------------------|---------------------|
| Inlet relative Mach number | 0.3695 | 0.3981 | 0.3695 |
| Inlet flow angle at shroud (deg) | 55.8034 | 70.0000 | 70.0000 |
| Mass flow function | 0.0118 | 0.0118 | 0.0095 |
| Inlet absolute Mach number | 0.2077 | 0.1362 | 0.1264 |
| Inlet flow angle at hub (deg) | 41.2957 | 59.1288 | 59.1088 |
| Impeller inlet shroud diameter (mm) | 27.9 | 34.4 | 32.0 |
| Impeller inlet hub diameter (mm) | 16.6 | 21.0 | 19.5 |
| Impeller trim | 11.6623 | 17.8084 | 15.3741 |
| Impeller inlet area (mm^2) | 392.84 | 586.43 | 506.74 |
| Average isentropic exponent | 1.5290 | 1.5386 | 1.5396 |
| Machine Mach number | | 0.8799 | |
| Impeller tip diameter (mm) | | 81.6 | |
| Work coefficient | | 0.7824 | |
| Inlet prewhirl angle (deg) | | 0 | |

The optimal design meets the criterion of the maximum swallowing capacity (Equation (19)). This means that the compressor should be much more compact than those without the criterion. In order to validate this criterion, two additional compressors (reference design I and design II) are developed that do not follow the criterion (see Table 5). Their inlet flow angles β_{1s} are specified as a constant (70 deg), instead of being calculated by Equation (19).

By comparing the optimal design and the reference I, we find that for a specified flow capacity (given mass flow function), this criterion is able to achieve a smaller inlet relative Mach number (smaller aerodynamic losses), and smaller impeller trim and impeller inlet area (more compact inlet geometry). If we compare the optimal design and the reference II, it is clear that for a given inlet relative Mach number, this criterion can increase the swallowing capacity of compressors (larger mass flow function). We can also find a more interesting phenomenon: even though the swallowing capacity is increased, a more compact impeller inlet might be also achieved.

The above results agree well with the theoretical analysis in Section 3.1. Therefore, the design criterion of the maximum swallowing capacity (Equation (19)) has the potential to achieve a more compact design with smaller aerodynamic losses.

The optimal design in Table 5 is selected as the final preliminary design scheme for further three-dimensional design and CFD simulation. Table 6 summarizes the geometrical parameters of the optimal SCO_2 compressor stage after three-dimensional design. Figure 9 illustrates the solid models of the impeller and volute. The numerical method established and validated in Section 2.2 is used for the simulation of the low-flow-coefficient SCO_2 compressor stage. Similarly, the mesh independency and RGP table resolution investigations are also implemented for the compressor stage. As a result, the mesh with the total cell number of 3.49 million (1.79 million for the single impeller and 1.70 million for the volute) in combination with RGP-2 could achieve a better balance between the simulation accuracy and computational effort. Figure 10 presents the computational domain and mesh of the compressor stage. Note that an unstructured mesh with hexahedral cells is adopted for the volute. The wall cell width and expansion ratio of viscous layers are consistent with those of the impeller.

Table 6. Geometrical parameters of the optimal SCO_2 compressor stage.

| Parameters | Values |
|--|---------|
| Number of full/splitter blades | 9/9 |
| Impeller tip diameter | 81.6 mm |
| Impeller inlet hub diameter | 16.6 mm |
| Impeller inlet shroud diameter | 27.9 mm |
| Impeller outlet blade angle | −30 deg |
| Impeller outlet width | 1.2 mm |
| Impeller tip clearance | 0.2 mm |
| Diffuser outlet diameter | 88 mm |
| Volute cross-sectional outlet diameter | 21.5 mm |

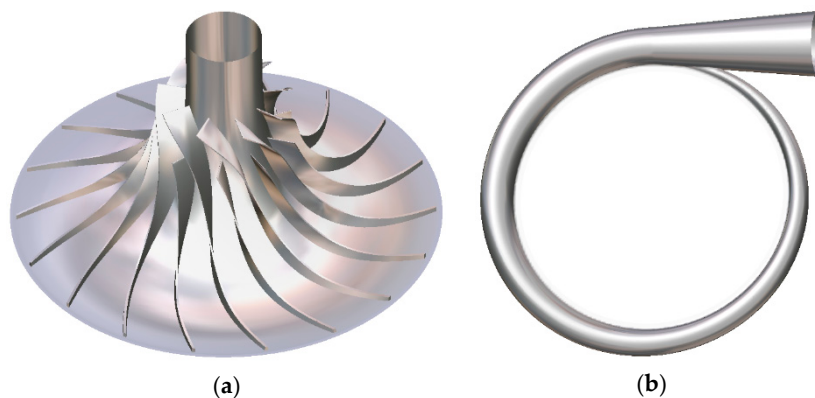


Figure 9. The solid model of the optimal compressor stage: (a) Impeller; and (b) Volute.

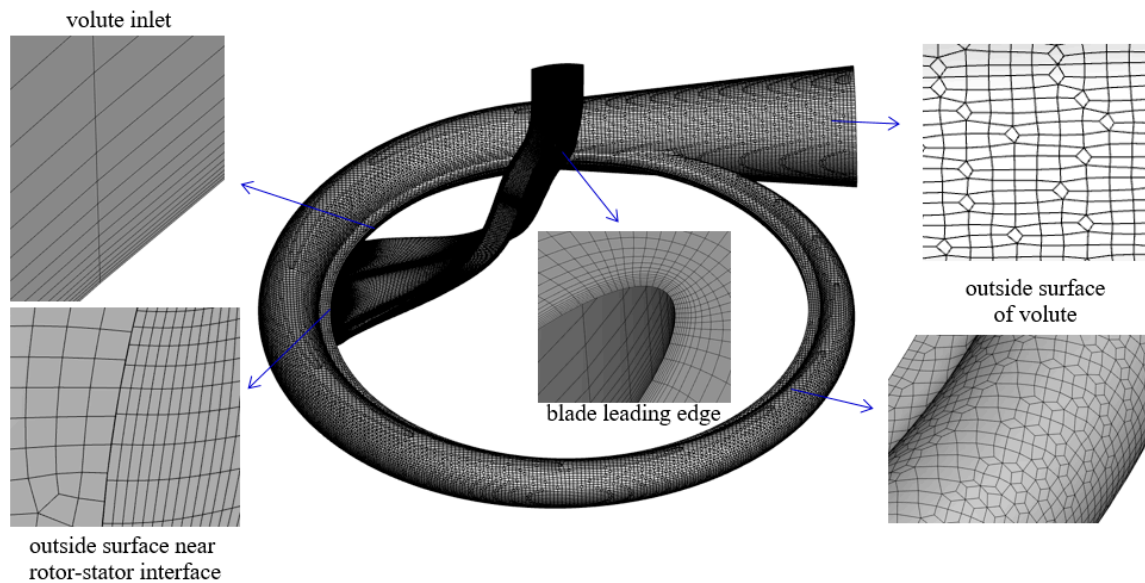


Figure 10. The computational domain and mesh of the optimal compressor stage.

Table 7 shows the relative errors between the preliminary design (based on analytical equations in Section 3 and REFPROP database) and numerical simulation (from Navier–Stokes equations coupled with RGP table) for the SCO_2 compressor at the design condition. In the Table 7, S1, S2, and S6 are the cross-sections of the impeller inlet, impeller outlet, and volute outlet, respectively. It is found that the numerical simulation results show satisfactory agreement with the preliminary design. Generally, the three-dimensional design meets the design specifications. It also confirms that the RGP table is able to reproduce the thermodynamic properties of REFPROP points with small errors, and RGP-2 is accurate and reliable for SCO_2 compressor simulations.

Table 7. The relative errors of the preliminary design results against the numerical simulation solutions for the optimal compressor stage.

| Parameters | S1 | S2 | S6 |
|-----------------------------|-------|----------------------------|-------|
| Total temperature | 0.01% | 0.27% | 0.34% |
| Static temperature | 0.08% | 0.17% | 0.47% |
| Total pressure | 0.05% | 0.04% | 0.46% |
| Static pressure | 0.13% | 0.07% | 0.91% |
| Density | 1.75% | 1.61% | 0.87% |
| Absolute velocity | 0.86% | 0.30% | 2.70% |
| Overall Performance | | | |
| Stage isentropic efficiency | 0.03% | Stage total pressure ratio | 0.44% |

Figure 11 shows the overall aerodynamic performance of the compressor at the design speed that is obtained from the numerical simulation. The isentropic efficiency peaks at the design mass flow rate (5 kg/s), which matches the design expectation. Overall, the compressor has a satisfactory aerodynamic performance over the whole speed line. However, simulation stability issues are encountered for the mass flow rate larger than 7.5 kg/s. The convergence problem is due to the potential condensation of the working fluid at the impeller inducer.

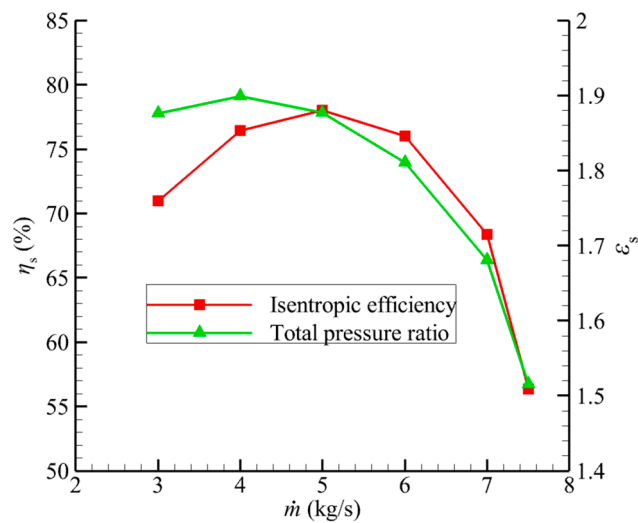


Figure 11. The characteristic curves of the isentropic efficiency η_s and total pressure ratio ϵ_s for the optimal compressor stage.

4.2. Results Analysis

This section presents the detailed flow analyses based on the numerical simulations to validate the inlet design method. As mentioned in Section 4.1, MAM of the designed compressor is in the recommended range. This implies that the inlet total condition can maintain a high cycle efficiency. Moreover, the compressor meets the criterion of the maximum swallowing capacity (Equation (19)), which means that the compressor compactness is theoretically guaranteed. This conclusion is further validated by the preliminary design results illustrated in Table 5. Therefore, the main task is to check whether this method can limit the condensation in the impeller inducer.

From the simulation results it is found that the low-pressure regions are mainly located upstream of the impeller, where the condensation is easy to happen. Thus, for the analysis of the condensation phenomenon, the focus is on the impeller instead of the volute.

Figure 12 illustrates the static pressure contours which are below the critical pressure for the design and off-design operating conditions at 10%, 50%, and 80% spans of the impeller. Three operating conditions: 3 kg/s, 5 kg/s, and 7 kg/s are analyzed, which correspond to the near surge condition, design condition, and near choke condition.

At the design condition (5 kg/s), low-pressure regions are found at the leading-edge suction sides of full and splitter blades. The regions result from the flow acceleration around the suction side of the blade leading edge due to the geometrical curvature. The condensation might take place in those regions.

When the compressor runs near the surge condition (3 kg/s), the mass flow rate decreases, leading to smaller inlet velocity and higher static pressure. On the other hand, according to the inlet velocity triangle, the smaller inlet velocity means a larger positive incidence angle at the leading edge, which intensifies flow acceleration on the suction side. The combined effect of the above two factors depends on their relative intensity. As a result, the flow acceleration is strengthened at 10% and 50% spans but is weakened at 80% span near the full blade. Furthermore, the acceleration is decreased over the whole span near the leading edge of the splitter blade.

Conversely, as the compressor operates near the choke condition (7 kg/s), the increasing mass flow rate will result in larger inlet velocity and lower static pressure. In addition, it forms a negative attack angle at the full blade, which contributes to the flow acceleration near the pressure sides of the blade leading edge. Both effects further aggravate the acceleration of the working fluid. As a consequence, a large low-pressure region has been found near the pressure side of the full blade leading edge. Sheltered by the full blades, the splitter blades are less affected by the change of the incidence angle, and the low-pressure region is still located on the suction side.

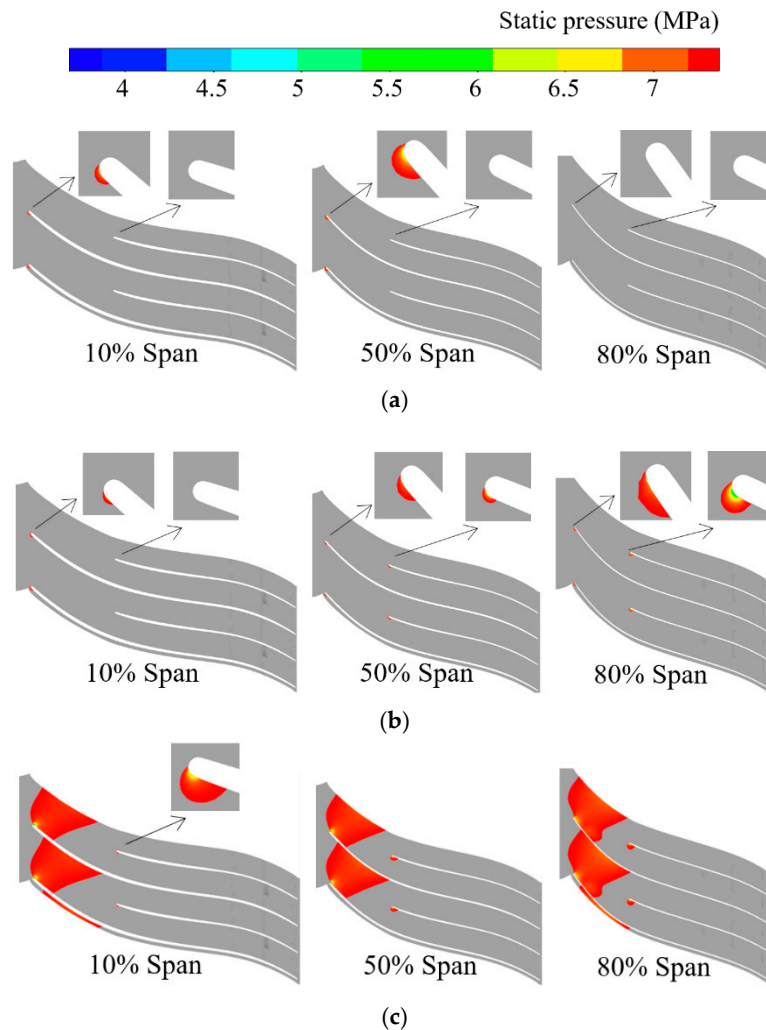


Figure 12. The static pressure contours below the critical pressure of the three operating conditions (3 kg/s, 5 kg/s, and 7 kg/s) at 10%, 50%, and 80% spans: (a) $\dot{m} = 3$ kg/s; (b) $\dot{m} = 5$ kg/s; and (c) $\dot{m} = 7$ kg/s.

However, identifying low-pressure regions is not sufficient to justify the occurrence of the fluid condensation. Procedure III in Section 3.2 is used to detect the condensation near the impeller inducer based on the numerical simulation results. Figure 13 displays the condensation regions (marked in red) of the impeller near the surge condition, at the design condition and near the choke condition. Figure 13a shows the computational domain, in which region A is the leading edge of the full blade and region B represents the leading edge of the splitter blade. At the design condition, only a tiny condensation region is found near the suction side of the splitter blade leading edge (Figure 13c). When the mass flow rate decreases to approach the surge condition, the condensation region becomes larger and transforms to the suction side of the full blade leading edge (Figure 13b). This process is consistent with the local acceleration of the working fluid in Figure 12a. In contrast, when the compressor operates near the choke condition, the condensation is observed on the leading-edge pressure side of the full blade (Figure 13d) and the suction side of the splitter blade (Figure 13e), which corresponds to the low-pressure regions in Figure 12c.

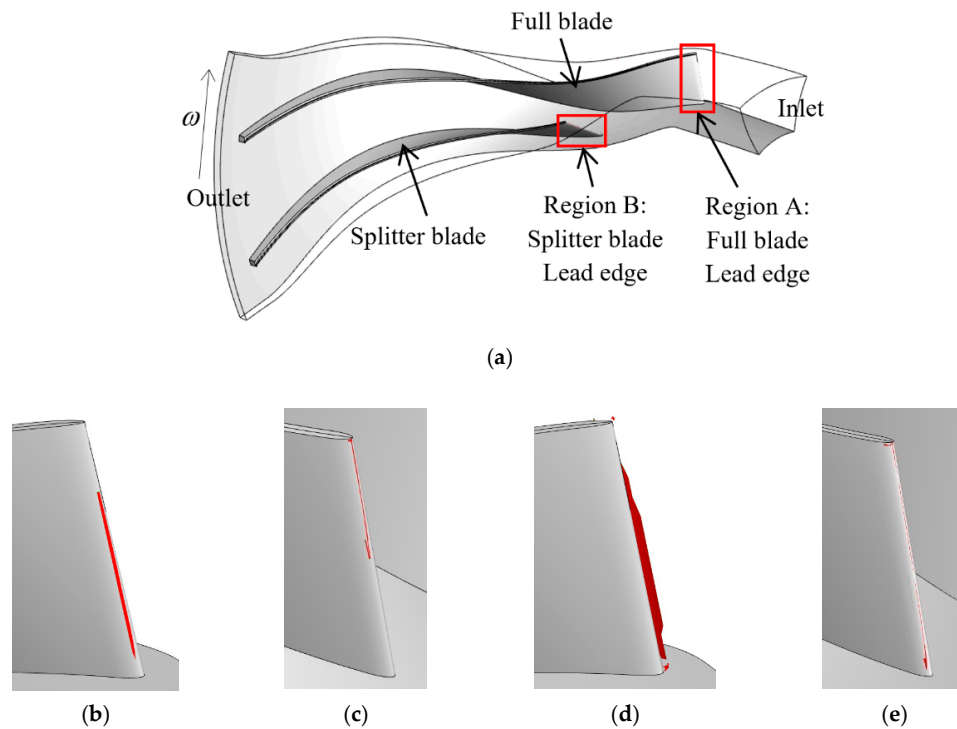


Figure 13. The condensation regions marked in red color at three operating conditions (3 kg/s, 5 kg/s, and 7 kg/s): (a) Computational domain; (b) $\dot{m} = 3$ kg/s: Region A; (c) $\dot{m} = 5$ kg/s: Region B; (d) $\dot{m} = 7$ kg/s: Region A; and (e) $\dot{m} = 7$ kg/s: Region B.

By comparing Figures 12 and 13, we can conclude that the low-pressure regions are mainly generated by the increased mean inlet velocity, while the condensation is mainly created by the local acceleration of the working fluid due to the geometrical curvature of the blade leading edge. Moreover, for the full blades, the fluid incidence angle (positive for the surge condition and negative for the choke condition) determines whether the condensation occurs on the leading-edge suction side or pressure side. However, sheltered by the full blades, the splitter blades are insensitive to the incidence angle, and the condensation is always observed on the leading-edge suction side.

Figure 13 confirms that the inlet design method can in general limit the condensation in the impeller inducer under the whole operating conditions.

To further discuss the flow characteristics of the compressor stage at design and off-design conditions, all computational points (control volumes) from the numerical simulations are plotted for the impeller (Figure 14) and the volute (Figure 15), respectively.

As shown in Figure 14, the blue filled triangle denotes the inlet total condition, and the green filled square stands for the inlet static one. The distance between them represents the degree of the isentropic expansion (the first acceleration), which can be quantified by the inlet absolute Mach number M_{c1} . Obviously, this expansion tends to increase with the ascending mass flow rate. The outspread points below the green filled square denote the further expansion near the blade leading edge (the second acceleration). This expansion also presents an increasing trend with the rising mass flow rate. The distribution laws of the computational points below the inlet total condition completely correspond to those of the low-pressure regions in Figure 12. These phenomena can be explained by the following facts.

As mentioned in Section 3.2, the second acceleration in impeller inducer is due to two factors: (I) the contraction of the impeller inducer area; and (II) the curvature of the blade leading edge. When the mass flow rate increases, both the first acceleration and the factor (I) of the second acceleration will increase the mean inlet velocity of impeller, as a result, the outspread computational points below the inlet total condition are increased, and vice versa. However, once the mass flow rate deviates from the

design condition (attack angle appears), the factor (II) of the second acceleration will boost the local velocity of working fluid near the suction side or pressure side of the blade leading edge, which causes the fluid to enter condensation. These analyses further conform the conclusion: the low-pressure regions (or computational points below the inlet total condition) are mainly generated by the increased mean inlet velocity, while the condensation is mainly created by the local acceleration due to the geometrical curvature of the blade leading edge.

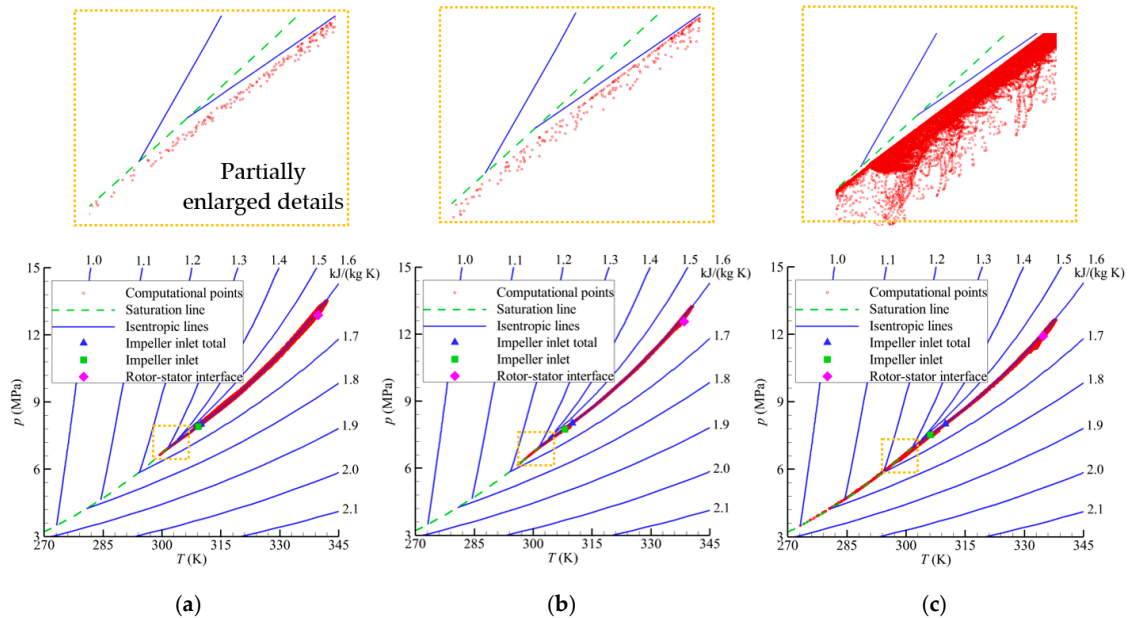


Figure 14. The simulation results of all computational points (control volumes) and partial enlarged details in the impeller at three operating conditions: (a) $\dot{m} = 3 \text{ kg/s}$; (b) $\dot{m} = 5 \text{ kg/s}$; and (c) $\dot{m} = 7 \text{ kg/s}$.

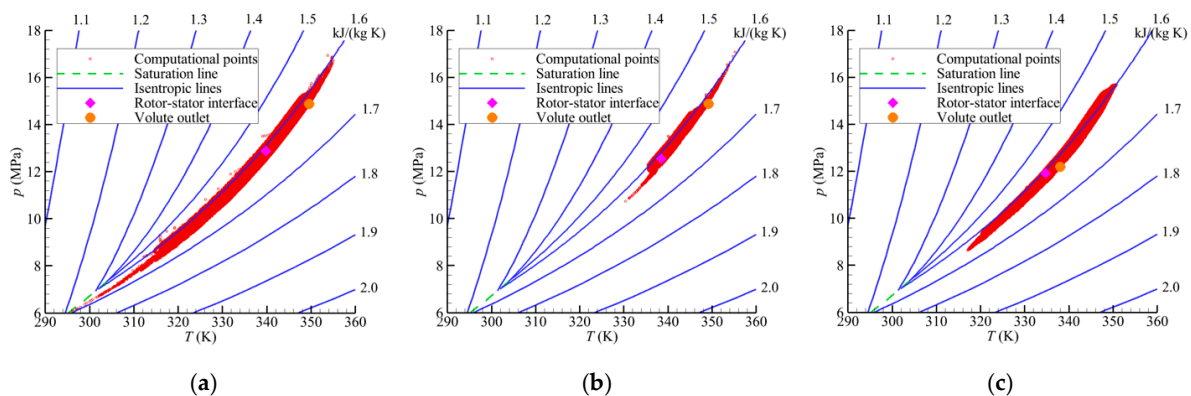


Figure 15. The simulation results of all computational points (control volumes) in the volute at three operating conditions: (a) $\dot{m} = 3 \text{ kg/s}$; (b) $\dot{m} = 5 \text{ kg/s}$; and (c) $\dot{m} = 7 \text{ kg/s}$.

Now, the partially enlarged details of Figure 14a–c are analyzed. During the second acceleration process of the working fluid near the blade leading edge (adiabatic but not isentropic), all computational points deviate from the isentropic line, resulting in a delay to reach the saturation line (the condensation). In this design case, the inlet total condition belongs to Zone I, which should be less likely to achieve the condensation as illustrated in Figure 7. Therefore, the numerical simulation results completely agree with the theoretical analysis in Section 3.2, indicating that the condensation design principle is reliable.

Additionally, it is clear from Figure 14 that the computational points at the design condition are generally located along the isentropic line. However, the patterns of the computational points near the surge and choke conditions present larger scales. It means that the off-design conditions have caused more aerodynamic losses.

Figure 15 shows the simulation results of all computational points (control volumes) in the volute under the design and off-design conditions. It is found that the pattern scale of the computational points at the design condition is small, while those near the surge and choke conditions are large. This shows that more energy losses are observed in the volute under the off-design conditions.

Figure 15a shows that near the surge condition some computational points are below the critical point of the working fluid, and they might enter the two-phase region. Procedure III in Section 3.2 is used to detect condensation, showing that no condensation occurs in the volute.

As shown in Figure 15c, the croci filled circle denotes the average static condition at the volute outlet. Near the choke condition, the outspread computational points above the croci filled circle are much more than those under the other operating conditions. This means that the diffusion process in the volute is significantly non-uniform near the choke condition, and this will cause much more additional aerodynamic losses.

5. Conclusions and Remarks

In order to seek a better balance between the cycle efficiency, compressor geometrical compactness, and inducer condensation, a new method for designing impeller inlet is proposed for SCO_2 compressors. In this method, the concept of the maximum swallowing capacity of real gas is coupled with a new condensation design principle. Based on the approach, a low-flow-coefficient SCO_2 compressor stage is designed and analyzed. The following conclusions are drawn:

The mass flow function is generally expressed by a set of non-dimensional parameters for real gas compressors. An optimal inlet flow angle is derived to achieve the maximum swallowing capacity at a certain inlet relative Mach number, which contributes to the minimum energy losses and a more compact compressor geometry.

A new condensation design principle is developed, in which a novel concept of the two-zone inlet total condition for SCO_2 compressors is firstly proposed, and then the acceptable acceleration margin (AAM) is derived as a criterion to limit the impeller inlet condensation.

A low-flow-coefficient compressor stage is designed based on the inlet design method. The mechanisms of the flow acceleration, which forms low-pressure regions and further produces the condensation, are analyzed under different operating conditions. It is found that the condensation is mainly created by the local acceleration of the working fluid due to the geometrical curvature of the blade leading edge rather than the mean inlet velocity. In addition, the fluid incidence angle determines the location of the condensation near the impeller leading edge. It is also found that the numerical simulation results agree well with the theoretical analysis of the two-zone inlet total condition. The condensation design principle is efficient to limit the two-phase region in the impeller inducer.

Furthermore, there are some remarks of the proposed method:

The first one is that the method tends to obtain a compact geometry of compressors by achieving the maximum swallowing capacity and the minimum inlet relative Mach number. As a consequence, the design condition of the compressor developed by the method is much closer to its choke condition. Hence, the method is not suitable for designs that require a large choke margin (i.e., ultra-low-speed compressors). But this is not a serious limitation, since modern compressors are usually high-speed or even transonic/supersonic, where the design condition is very close to the choke condition (operating at unique incidence condition).

Another aspect is that the blade leading edge of the impeller in this study is elliptical type. This means that the local acceleration is ineluctable even at the design condition. Special features of blade leading edge could be adopted, such as extremely thin blades with reduced suction surface curvature, and leading-edge sweepback, then the fluid condensation at impeller inducer under the design condition would be further reduced. However, the effects of those special features on off-design conditions are much more complicated due to potential flow separations. For transonic or supersonic SCO_2 compressors design, the interactions among shock waves, boundary layer separations,

tip leakage vortices, and phase transition might be the most tough challenge to balance the compressor compactness, cycle efficiency and inlet condensation.

A further limitation of the impeller inlet design method is that the condensation detection criterion (Procedure III) is conservative. It assumes that condensation (or evaporation) occurs suddenly as soon as the fluid reaches the saturation line, and this process has no delay. In fact, in an impeller inducer, phase transition proceeds at a finite time instead of an instant. If the expansion of the gas is rapid enough, the fluid attains a nonequilibrium state (crosses the saturation line) without condensation, since there is not enough time for fluid to form droplet when it just reaches the saturation line [34]. Thus, it is conservative to judge the occurrence of condensation by checking whether the fluid crosses the saturation line. A more accurate method is to define a ratio of timescales (the ratio of the residence time of fluid in the saturated region to the time of liquid droplet formation) to consider the condensation effects. When the ratio of timescales is below 1, the nucleation time is longer than the residence time, which means that condensation cannot really occur [16]. However, the determination of the timescales becomes challenging near the critical point, due to the increased coalescence of the molecules [12]. Hence, Procedure III in this article is a “rough” but much “safer” criterion. The focus of this study is on the trade-off exploration among the non-dimensional impeller inlet parameters and to achieve an optimal inlet geometry, rather than the nucleation mechanism. Therefore, the proposed method is still able to provide some useful information for compressor impeller inlet design at the preliminary design phase. In addition, this conservative condensation detection criterion (Procedure III) might be more suitable for off-design conditions of SCO₂ compressors, since the accelerations of working fluid under such conditions are further intensified compared to the design condition (see Figure 14), and the condensation (or evaporation) is more likely to occur. Anyway, a more accurate condensation detection criterion should be developed to make the impeller inlet design method more accurate and robust over the whole operating range of SCO₂ compressors.

The in-depth investigations of the above limitations are the authors’ future work.

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Nomenclature

Notation

| | |
|------------------|---|
| A | Impeller inlet area (m ²) |
| a | Speed of sound (m/s) |
| AAM | Acceptable Acceleration Margin |
| AMC | Acceleration Margin to Condensation |
| C_p | Specific heat at constant pressure (J/(kg K)) |
| C_v | Specific heat at constant volume (J/(kg K)) |
| c | Absolute velocity (m/s) |
| c_{ref} | Reference velocity (m/s) |
| CFD | Computational Fluid Dynamics |
| CFL | Courant–Friedrichs–Lewy |
| D | Diameter (m) |
| DNS | Direct Numerical Simulation |
| EOS | Equation of State |
| f | Function provided by REFPROP software |
| h | Enthalpy (J/kg) |
| IVR | Inlet Velocity Ratio |

| | |
|------------------|--|
| k | Impeller inlet shape factor, $k = 1 - (D_{1h}/D_{1s})^2$ |
| L | Thermal conductivity (W/(m K)) |
| L_{ref} | Reference length |
| LK | Lee-Kesler model |
| M | Mach number |
| M_{c1} | Inlet absolute Mach number |
| M_{w1} | Inlet relative Mach number at shroud |
| M_{u2} | Machine Mach number |
| \dot{m} | Mass flow rate (kg/s) |
| MAM | Maximum Acceleration Margin |
| n_s | Isentropic exponent |
| \bar{n}_s | Average isentropic exponent |
| p | Pressure (MPa) |
| Q | Quality (vapor fraction) |
| R | Gas constant (J/(kg K)) |
| RGP | Real Gas Property |
| S | Entropy (J/(kg K)) |
| SCO ₂ | Supercritical Carbon Dioxide |
| SW | Span-Wagner model |
| T | Temperature (K) |
| u | Impeller blade speed (m/s) |
| v | Specific volume (m ³ /kg) |
| w | Relative velocity (m/s) |
| y_{wall} | Size of the first cell to the wall |
| y^+ | Non-dimensional distance of first cell to the wall |

Greek Symbols

| | |
|---------------|--|
| α_1 | Inlet prewhirl angle (deg) |
| β_{1s} | Inlet flow angle (deg) at shroud, relative to meridional direction |
| β_T | Isothermal compressibility (1/Pa) |
| γ | Specific heat ratio |
| ε | Total pressure ratio |
| η | Isentropic efficiency, total to total |
| λ | Empirical coefficient of AAM |
| μ | Dynamic viscosity (Pa s) |
| ν | Kinematic viscosity (m ² /s) |
| ρ | Density (kg/m ³) |
| Φ | Mass flow function |
| Φ' | Modified mass flow function |
| ω | Angular velocity (rad/s) |

Subscripts

| | |
|-----|----------------------------------|
| 1 | Impeller inlet |
| 2 | Impeller outlet |
| 4 | Diffuser outlet |
| 6 | Volute outlet |
| c | Absolute value |
| cr | Properties at the critical point |
| g | Guess value |
| h | Hub |
| i | Impeller |
| m | Meridional |
| ref | Reference value |
| s | Shroud, Compressor stage |
| t | Total condition |
| u | Tangential direction |
| w | Relative value |

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