

## Article

# Prediction of Oxidation Stability of Biodiesel Derived from Waste and Refined Vegetable Oils by Statistical Approaches

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**Abstract:** The oxidation stability (OX) of the biodiesel is an essential parameter mainly during storage, which reduces the quality of the biodiesel, thus affecting the engine performance. Moreover, many factors affect oxidation stability. Therefore, determining the most significant parameter is essential for achieving accurate predictions. In this paper, an empirical equation (Poisson Regression Model (PRM)), machine learning models (Multilayer Feed-Forward Neural Network (MFFNN), Cascade Feed-forward Neural Network (CFNN), Radial Basis Neural Network (RBFNN), and Elman neural network (ENN)) with various combinations of input parameters are utilized and employed to identify the most relevant parameters for prediction of the oxidation stability of biodiesel. This study measured the physicochemical properties of 39 samples of waste frying methyl ester and their blends with various percentages of palm biodiesel and refined canola biodiesel. To this aim, 14 parameters including concentration amount of WFME (X1), PME (X2), and RCME (X3) in the mixture, kinematic viscosity (KV) at 40 °C, density at 15 °C (D), cloud point (CP), pour point (PP), the estimation value of the sum of the saturated ( $\sum SFAMs$ ), monounsaturated ( $\sum MUFAMs$ ), polyunsaturated ( $\sum PUFAMs$ ), degree of unsaturation (DU), long-chain saturated factor (LCSF), very-long-chain fatty acid (VLCFA), and ratio ( $\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}$ ) fatty acid composition were considered. The results demonstrated that the RBFNN model with the combination of X1, X2, X3,  $\sum SFAMs$ ,  $\sum MUFAMs$ ,  $\sum PUFAMs$ , VLCFA, DU, LCSF,  $\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}$ , KV, and D has the lowest value of root mean squared error and mean absolute error. In the end, the results demonstrated that the RBFNN model performed well and presented high accuracy in estimating the value of OX for the biodiesel samples compared to PRM, MFFNN, CFNN, and ENN.

**Keywords:** multilayer feed-forward neural network; cascade feed-forward neural network; radial basis neural network; Elman neural network; poisson regression model; oxidation stability



**Citation:** Çamur, H.; Al-Ani, A.M.R. Prediction of Oxidation Stability of Biodiesel Derived from Waste and Refined Vegetable Oils by Statistical Approaches. *Energies* **2022**, *15*, 407. <https://doi.org/10.3390/en15020407>

Academic Editor: Diego Luna

Received: 27 November 2021

Accepted: 2 January 2022

Published: 6 January 2022

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## 1. Introduction

Biodiesel is considered one of the most promising potential fuels to supplement or substitute diesel. It has many advantages over diesel fuel, such as inherent lubricity, non-toxic and biodegradable, free of sulfur and aromatics, higher cetane number and flashpoint, and lower exhaust emissions, excepting higher NO<sub>x</sub> emissions [1–3].

Biodiesel is commonly produced from various edible and non-edible sources [4,5]. According to the literature [5–7], waste frying oil is considered as an efficient primary source among these sources for biodiesel production due to its low cost and easy availability. Generally, the transesterification reaction is widely used to produce biodiesel from any oil resources, where triglycerides are converted into fatty acid esters using homogeneous (acid and alkaline) or heterogeneous catalysts. Thus, the process of transesterification influences the biodiesel yield and production cost. Additionally, the operating conditions (catalyst type, temperature, methanol amount, reaction time) are attributed to biodiesel production. Hence, several researchers have used machine learning and mathematical models to maximize or optimize biodiesel production [8–11].

Moreover, the properties of produced biodiesel depend on its feedstock's physico-chemical properties and fatty acid composition. According to Yaşar [12], biodiesel's most critical physicochemical properties, such as viscosity, density, oxidation stability, and cold flow properties, are dependent on the fatty acid characteristics of feedstock, including chain length and the number of double bonds. Moreover, several scientific researchers have predicted biodiesel's critical properties based on its chemical structure. For instance, Giakoumis and Sarakatsanis [13] used multiple linear regression analysis to investigate the relationship between some selected properties of biodiesel (cetane number, density, kinematic viscosity, and heating values) and fatty acid weight composition. Alviso et al. [14] utilized genetic programming to estimate the physicochemical properties of biodiesel (the kinematic viscosity, flash point, cloud point, pour point, cold filter plugging point, cetane number, iodine number) and its fatty acids composition. Razavi et al. [15] predicted biodiesel properties, including pour point, cloud point, iodine value, and kinematic viscosity, as a function of fatty acids composition using the Least squares support vector machine.

As mentioned previously, the physicochemical properties of biodiesel depend on the fatty acid profile and the raw materials used for the production of biodiesel. In this study, the authors have focused on the oxidation of biodiesel produced from various oil resources. Oxidation stability (OX) is considered one of the vital fuel quality criteria for biodiesel and should be addressed since oxidation products may impair fuel quality and, subsequently, engine performance [16]. Many factors can affect the oxidation stability of biodiesel like fatty acid composition, impurities (metals, free fatty acids, additives and antioxidants, water), physical parameters (sample mass, agitation, viscosity, temperature, light, and air exposure), as well as the degree of prior sample aging [17–21]. Besides, biodiesel, which contains a high amount of unsaturated methyl esters, is very susceptible to oxidative degradation [22]. Oxidation of unsaturated esters in biodiesel occurs by contact with air and other pro-oxidizing conditions during the storage period [23].

Moreover, most biodiesel produced requires antioxidants to meet the minimum requirement of oxidation stability, which is outlined in EN-14214 (6 h or 8 h) and ASTM D-6751 (3 h). The addition of antioxidants to biodiesel could help slow down the process of oxidation caused by free radicals [24]. Recently, researchers have explored the influence of adding different antioxidants such as tertiary butyl-hydroquinone (TBHQ), pyrogallol (PY), propyl gallate (PG), butylated hydroxytoluene (BHT), and butylated hydroxyanisole (BHA) antioxidants on the oxidation stability of biodiesel [25,26].

Consequently, this can be a challenging problem in biodiesel research. As an ongoing study of authors on the properties of biodiesel, mainly oxidation stability [27–30], the present study aims to identify the most relevant parameters for the prediction of oxidation stability of biodiesel. In literature, several empirical models such as machine learning models, regression models, and other hybrid forecasting models are reported to predict biodiesel properties such as kinematic viscosity, density, cetane number, flash point, and so on. To the best of our knowledge, there are no studies in the literature about identifying the most appropriate input parameters for the prediction of oxidation stability using machine learning models and regression models. With this primary objective, Poisson Regression Model (PRM) and machine learning models (Multilayer Feed-Forward Neural Network (MFFNN), Cascade Feed-forward Neural Network (CFNN), Radial Basis Neural Network (RBNN), and Elman neural network (ENN) models are developed to find the most influencing input parameters for oxidation stability of biodiesel. For this aim, model 1, model 2, and model 3 with various input variables are proposed. Model 1 is developed using the estimation value of the sum of the saturated ( $\sum SFAMs$ ), monounsaturated ( $\sum MUFAMs$ ), polyunsaturated ( $\sum PUFAMs$ ), degree of unsaturation ( $DU$ ), long-chain saturated factor ( $LCSF$ ), very-long-chain fatty acid ( $VLCFA$ ), and ratio ( $\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}$ ) fatty acid composition. Knowing that these values are calculated based on the fatty acid composition of biodiesel, model 2 is developed by adding kinematic viscosity (at 40 °C), density (at 15 °C). Model 3 is designed using all input variables. To this aim, to achieve this, the fatty acid composition, kinematic viscosity (at 40 °C), density (at 15 °C), and cold flow properties

were measured for 41 different fatty acid methyl ester biodiesels and their blends. Additionally, the influence of blending various amounts of palm biodiesel and refined canola biodiesel with waste frying biodiesel on the oxidation stability of the blend was discussed.

## 2. Materials and Methods

In this section, the preparation of PME-WFME-RCME fuel samples and measurements of their properties according to ASTM standards are explained. Figure 1 schematically illustrates the description of the proposed study.

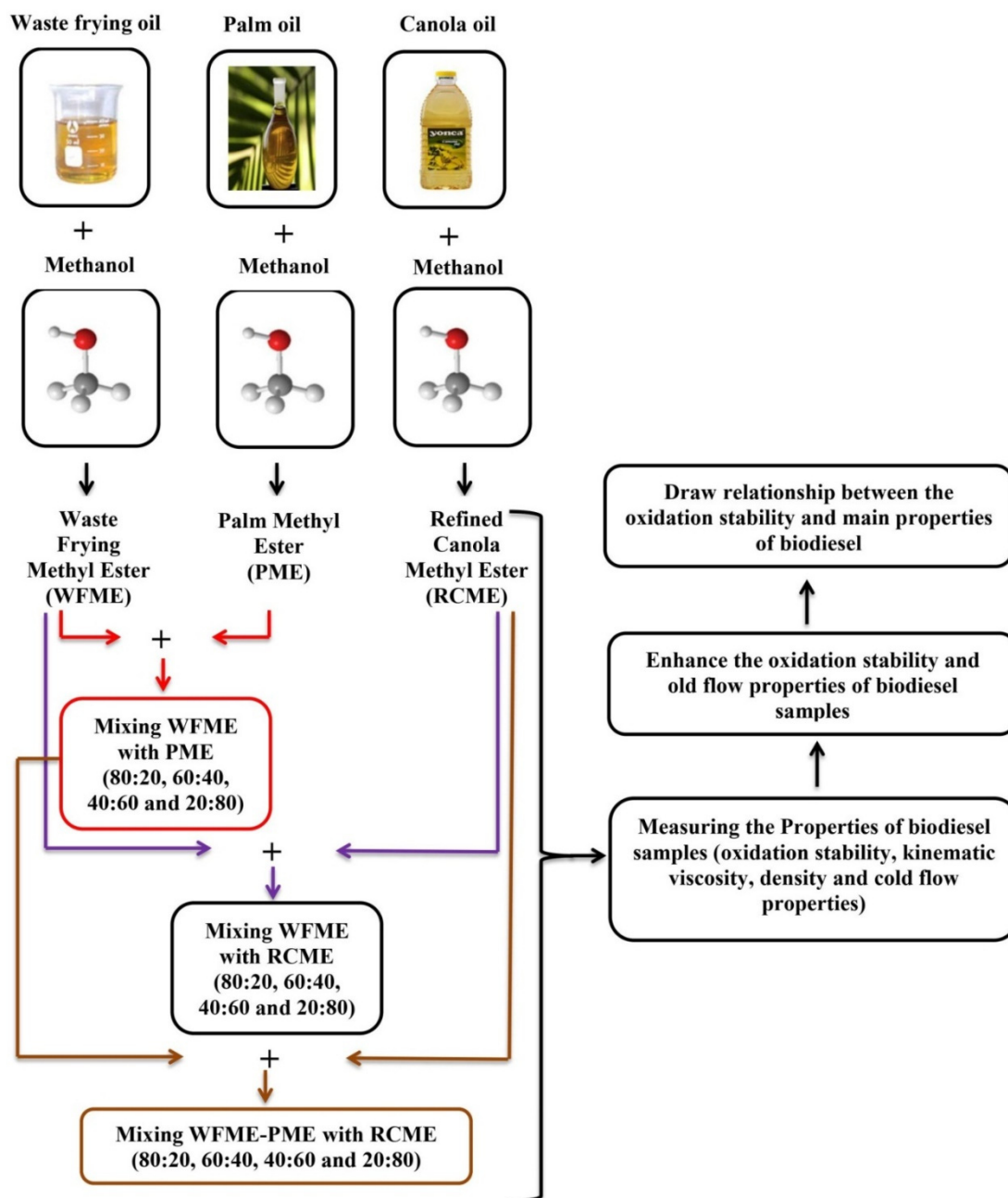


Figure 1. Flowchart of analysis procedure in the present study.

### 2.1. Raw Materials

Forty-one different types of biodiesels with various fatty acid compositions were used in this study. Considering this, thirty-nine of these biodiesels were produced from waste vegetable oils, which were collected from households, traditional restaurants, hotels,

and cafés. Additionally, canola oil and palm oil were purchased from the local market in Northern Cyprus.

## 2.2. Instruments

In this study, the kinematic viscosity (KV), density (D), cold flow properties including Cloud Point (CP) and Pour Point (PP), and oxidation stability (OX) were measured for all the fuel samples. The KV and D were measured using Ubbelohde viscometers and Pycnometer with a bulb capacity of 25 mL following the standard ASTM D445 [31] and ASTM D854 [32], respectively. Furthermore, CP and PP were determined according to ASTM D2500 [33] and ASTM D97 [34]. Finally, the OX was evaluated using the Rancimat instrument following EN 14112 [35]. Measuring these properties is explained in detail in Refs. [29,30].

## 2.3. Fuel Characteristics

All biodiesel samples were analyzed by gas chromatography (GC) to evaluate the fatty acid profile of the fuel. The estimating values of the sum of the saturated ( $\sum SFAMs$ ), monounsaturated ( $\sum MUFAMs$ ), polyunsaturated ( $\sum PUFAMs$ ), degree of unsaturation ( $DU$ ), long-chain saturated factor ( $LCSF$ ), very-long-chain fatty acid ( $VLCFA$ ), and ratio ( $\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}$ ) are presented in Table 1. These values can be determined using Equations (1)–(7).

$$\sum MUFAMs = \sum wt\%C_{xx} : 1 \quad (1)$$

$$\sum PUFAMs = \sum wt\%C_{xx} : 2 + \sum wt\%C_{xx} : 3 \quad (2)$$

$$\sum SFAMs = \sum wt\%C_{xx} : 00 \quad (3)$$

$$DU = [\text{monounsaturated } C_n : 1] + 2[\text{polyunsaturated } C_n : 2, 3] \quad (4)$$

$$LCSF = 0.1 \times [C16 : 0] + 0.5 \times [C18 : 0] + [C20 : 0] + 1.5 \times [C22 : 0] + 2 \times [C24 : 00] \quad (5)$$

$$VLCFA = [C20 : 0] + [C20 : 1] + [C22 : 0] + [C24 : 00] \quad (6)$$

$$R = \frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs} \quad (7)$$

The identification of the principal fatty acid compositions (FACs) in Palm methyl ester (PME) were oleic (43.20%), palmitic (39.1%), linoleic (11.00%), and stearic (4.10%) acids. Several other FACs were detected in lesser (<2%) amounts. The combined content of *MUFAM*, *PUFAM*, *SFAM*, *DU*, *LCSF*, and *VLCFA* were 44.90, 43.50, 11.20, 65.90, and 0.5%, respectively. These results agreed with previous reports on the FAC profile of PME [36–38]. Refined canola methyl ester (RCME) was characterized by a high percentage of oleic acid (58.9%), linoleic acid (20.57%), Linolenic acid (9.34%), and Palmitic acid (4.14%). The estimated value of *MUFAM*, *PUFAM*, *SFAM*, *DU*, *LCSF*, and *VLCFA* of RCME was 60.25, 39.91, 6.73, 120.07, 2.00, and 1.98%, respectively. These results agreed with previous reports on the FAC profile of RCME [39–41]. Moreover, it is observed that the highest content of saturated fatty acid was obtained from WFME11 followed by WFME17. Additionally, it is found that the highest content of *MUFAM* and lowest content of *PUFAM* were recorded for WFME 12 and WFME17.

## 2.4. Blend Preparation

The fuel samples obtained from waste frying oils were blended with PME and RCME with various percentages from 20 to 80 (%v/v) in the step of 20 (%v/v) for improving the properties of PME-WFME and RCME-WFME samples. Furthermore, the PME-WFME samples were mixed with different concentrations of RCME (20%, 40%, 60%, and 80%) for enhancing the oxidation stability and cold flow properties of PME-WFME-RCME. The blends are prepared using a beaker and electrical stirrer with a stainless-steel propeller at room temperature for 30 min.

**Table 1.** Quantified MUFAMEs, PUFAMEs, SFAME, DU, LCSF, VLCFA, and R.

Samples	SFAM	MUFAM	PUFAM	VLCFA	DU	LCSF	$\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}$
WFME1	7.74	64.01	28.33	1.50	120.67	1.81	11.93
WFME2	9.50	62.83	27.81	1.43	118.46	2.01	9.54
WFME3	11.27	61.65	27.30	1.35	116.25	2.20	7.90
WFME4	13.03	60.47	26.78	1.28	114.04	2.40	6.70
WFME5	16.55	58.11	25.75	1.13	109.62	2.79	5.07
WFME6	20.08	55.75	24.72	0.98	105.20	3.19	4.01
WFME7	25.38	52.22	23.18	0.75	98.58	3.78	2.97
WFME8	30.65	48.68	21.63	0.53	91.93	4.37	2.29
WFME9	34.20	46.32	20.60	0.38	87.52	4.77	1.96
WFME10	39.47	42.78	19.05	0.15	80.88	5.35	1.57
WFME11	42.99	40.42	18.02	0.00	76.46	5.75	1.36
WFME12	7.74	65.43	27.33	1.92	120.09	1.81	11.98
WFME13	14.79	60.43	25.27	1.54	110.96	2.60	5.79
WFME14	21.84	55.43	23.21	1.15	101.84	3.38	3.60
WFME15	28.89	50.42	21.14	0.77	92.71	4.17	2.48
WFME16	35.94	45.42	19.08	0.38	83.59	4.96	1.79
WFME17	42.99	40.42	17.02	0.00	74.46	5.75	1.34
WFME18	22.13	52.07	25.48	1.31	103.03	4.13	3.50
WFME19	22.70	51.00	26.22	1.29	103.43	4.20	3.40
WFME20	23.28	49.93	26.95	1.27	103.83	4.28	3.30
WFME21	23.85	48.85	27.69	1.26	104.23	4.35	3.21
WFME22	24.43	47.78	28.42	1.24	104.63	4.43	3.12
WFME23	25.00	46.71	29.16	1.22	105.03	4.50	3.03
WFME24	21.55	50.45	28.79	1.36	108.04	3.96	3.68
WFME25	18.10	54.20	28.43	1.50	111.05	3.42	4.57
WFME26	14.64	57.94	28.06	1.64	114.07	2.89	5.87
WFME27	11.19	61.69	27.70	1.78	117.08	2.35	7.99
WFME28	19.25	54.74	25.85	1.43	106.44	3.66	4.19
WFME29	16.37	57.41	26.22	1.55	109.85	3.20	5.11
WFME30	13.50	60.09	26.59	1.68	113.27	2.74	6.42
WFME31	10.62	62.76	26.96	1.80	116.68	2.27	8.45
WFME32	39.39	41.68	19.45	0.24	80.57	5.50	1.55
WFME33	35.79	42.94	21.88	0.49	86.69	5.25	1.81
WFME34	32.20	44.19	24.30	0.73	92.80	5.00	2.13
WFME35	28.60	45.45	26.73	0.98	98.92	4.75	2.52
WFME36	26.30	49.74	23.79	1.05	97.32	4.45	2.80
WFME37	30.47	47.41	22.10	0.79	91.60	4.78	2.28
WFME38	34.65	45.08	20.40	0.52	85.89	5.10	1.89
WFME39	38.82	42.75	18.71	0.26	80.17	5.42	1.58
RCME	6.73	60.25	29.91	1.98	120.07	2.00	13.40
PME	44.90	43.50	11.20	0.50	65.90	6.36	1.22
WFME:	Waste frying methyl ester						
PME:	Palm methyl ester						
RCME:	Refined canola methyl ester						

## 2.5. Empirical Models

This section explains the selected empirical models to choose the more relevant variables for oxidation stability prediction. In this study, Matlab and Minitab are employed in training and evaluating the models.

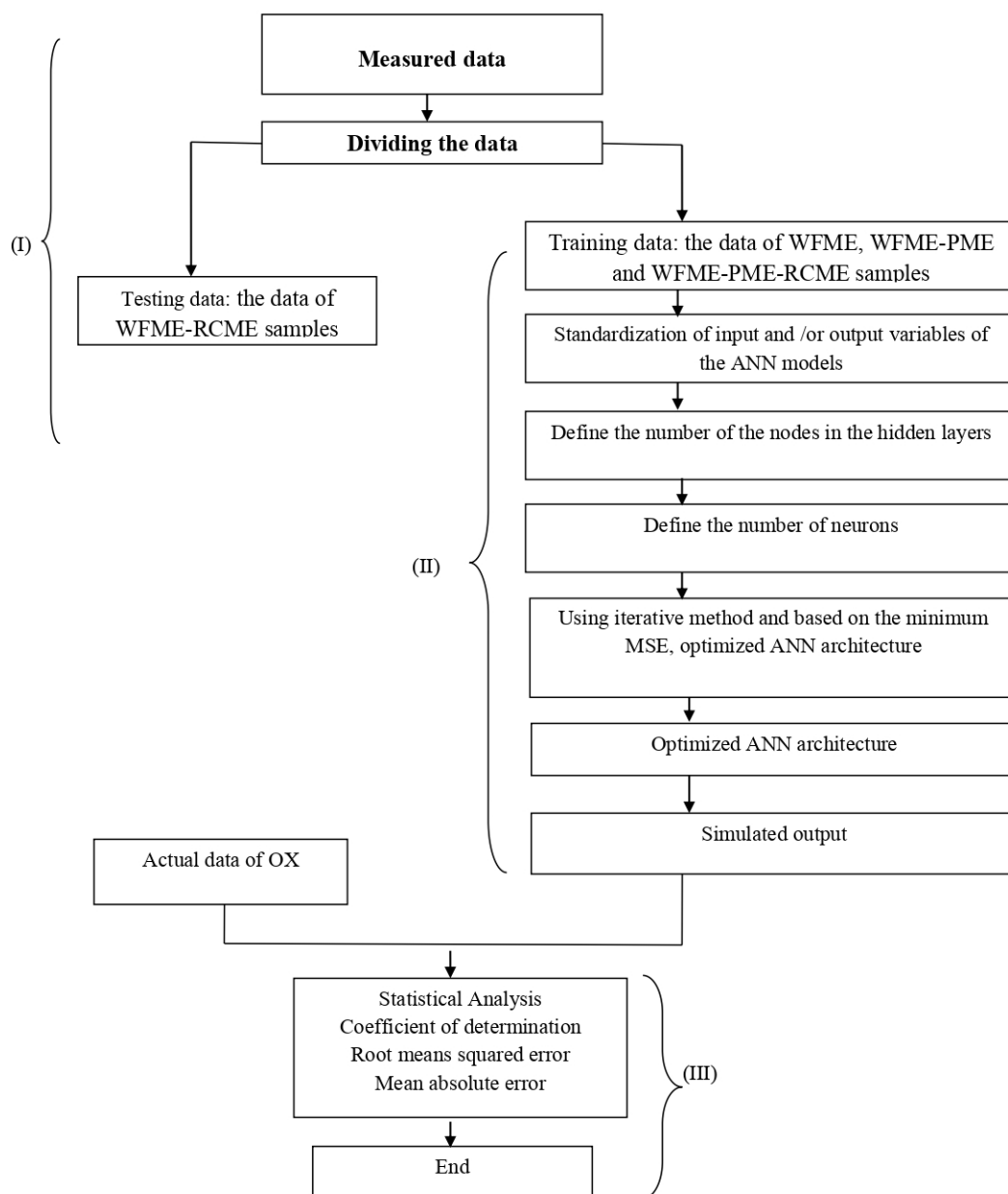
### 2.5.1. Artificial Neural Networks (ANN)

Machine learning models are used as alternative tools to describe a complex system [42]. They are utilized in a wide variety of applications in engineering and science. In this study, four empirical models (Multilayer feed-Forward Neural Network (FFNN), Cascade Forward Neural Network (CFNN), Radial Basis Function Neural Network (RBFNN), and Elman neural network (ENN)) are developed to predict the cold flow properties and oxi-

duction stability of fuel samples. This work uses the value of *MUFAM*, *PUFAM*, *SFAM*, *DU*, *LCSF*, *VLCFA*, volume fraction, *KV*, *D*, *CP*, and *PP* as explanatory input variables. The data are divided into training and testing groups, and the results by the models are compared with each.

(a) *Multilayer feedforward neural network (MFNN)*

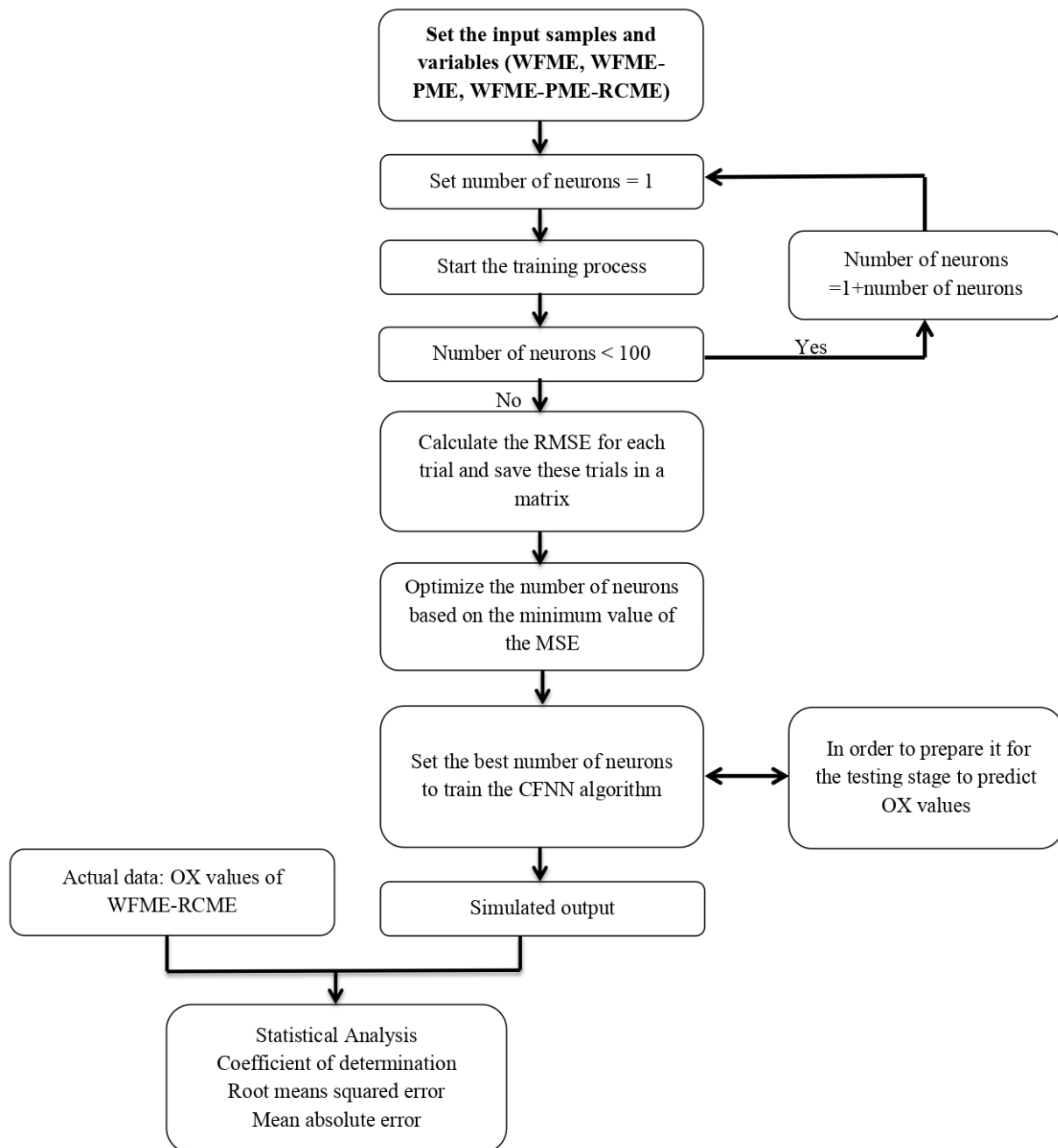
The MFNN consists of three layers (input, hidden, and output layers). Several neurons and hidden layers should be cautiously selected as they influence the validity of training. TRAINLM is used for training function. In addition, Mean squared error (MSE) is estimated to find the best performance of the training algorithm. The declining gradient of the back-propagation algorithm is utilized to reduce the value of MSE between the actual and estimated output. The description of the developed model was given in Kassem and Gokcekus [42]. Figure 2 illustrates the explanation process of the proposed MFNN method.



**Figure 2.** The proposed algorithm of predicting OX values using MFNN.

## (b) Cascade feedforward neural network (CFNN)

Figure 3 describes the steps of the proposed model (CFNN). CFNN represents a static neural network where the signals only move forward [43]. It is similar to a feedforward neural network, but it contains a connection from the input and every previous layer to the layers of the following layer [42–44]. The favorable position of this model is that it can convey the nonlinear association without getting rid of the linear association between input and output. The ideal number of neurons is established on the lowest value of RMSE. The description of the developed model was given in Kassem and Gokcekus [42].

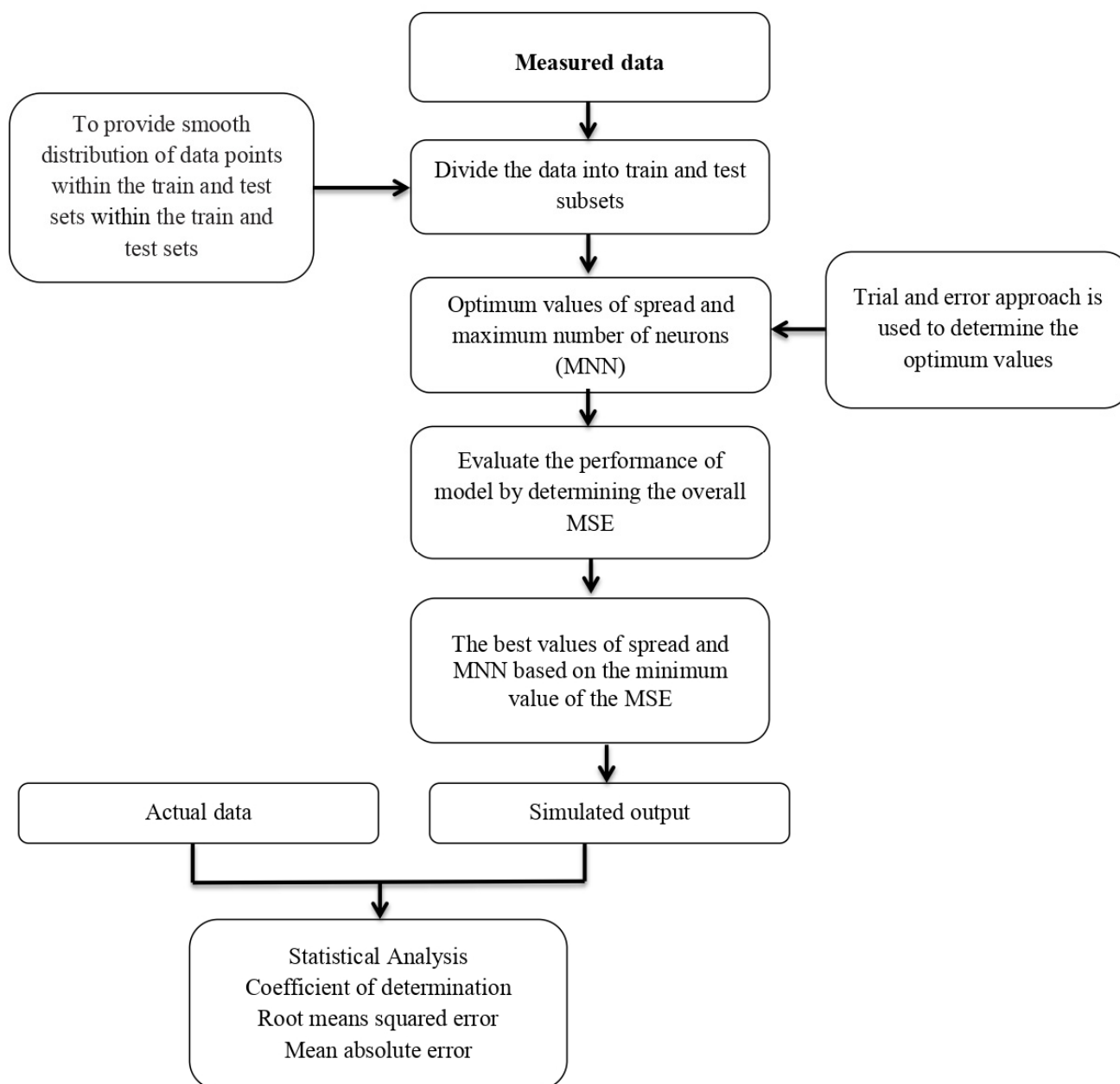


**Figure 3.** The proposed algorithm of predicting OX values using CFNN.

## (c) Radial basis neural networks (RBFNN)

RBFNN is a feedforward network, which includes one input, one hidden, and one output layer. It is used radial basis functions as activation functions [45]. Speed and effi-

ciency are the most important advantages of RBFNN models compared to other multilayer perceptron models due to their simple structure. The description of the developed model was given in Kassem and Gokcekus [42]. Figure 4 illustrates the steps of the proposed model (RBFNN).



**Figure 4.** The proposed algorithm of predicting OX values using RBFNN.

(d) *Elmanneural network (ENN)*

The ENN is a simple type of recurrent neural network. It includes four main layers: the input layer, context layer, hidden layer, and the output layer [46]. The main ENN structure is similar to the multilayer neural network. As stated earlier, there is a context layer in ENN where the inputs of this layer come about from outputs of the hidden layer, which was used to keep the hidden layer's output values from the last time [47].

### 2.5.2. Poisson Regression Model (PRM)

Poisson regression is a generalized linear model (GLM) often utilized to imitate infrequent happenings and count data. Many academics in many different disciplines have employed PRM in their research work [48].

Two main assumptions have been made whilst using the Poisson Regression Model. The first is that the response variable follows a Poisson distribution.

$$P = e^{-\lambda} \frac{\lambda^k}{k!} \quad (8)$$

where  $P$  is the likelihood that  $k$  number of happenings will occur per interval of time and  $\lambda$  is the happening rate. The second major assumption is that the response variable's variance and mean are equal. Thus, only one parameter can define the likelihood distribution,  $\lambda$  [49].

The parameter,  $\lambda$ , is specified by the log-linear function

$$\lambda = \exp(-x_i\beta) \quad (9)$$

where  $x_i$  is a vector of input data for the time  $i$  and  $\beta$  is an accompanying vector of model parameters, which is further improved during training [49].

### 2.5.3. Model Performance Criteria

Coefficient of determination ( $R^2$ ), mean absolute error ( $MSE$ ), root mean squared error ( $RMSE$ ), mean absolute error ( $MAE$ ), standard error of prediction ( $SEP$ ), and average absolute deviation ( $AAD$ ) were used to measure the estimation success of the models. The following equations were used for evaluation.

$$R^2 = 1 - \frac{\sum_{i=1}^n (a_{a,i} - a_{p,i})^2}{\sum_{i=1}^n (a_{p,i} - a_{a,ave})^2} \quad (10)$$

$$MSE = \frac{1}{n} \sum_{i=1}^n (a_{a,i} - a_{p,i})^2 \quad (11)$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (a_{a,i} - a_{p,i})^2} \quad (12)$$

$$MAE = \frac{1}{n} \sum_{i=1}^n |a_{a,i} - a_{p,i}| \quad (13)$$

$$SEP = 100 \times \frac{RMSE}{a_{a,ave}} \quad (14)$$

$$AAD = \frac{100}{n} \sum_{i=1}^n \frac{|a_{a,i} - a_{p,i}|}{a_{a,i}} \quad (15)$$

where  $n$  is the number of data,  $a_{p,i}$  is the predicted values,  $a_{a,i}$  is the actual values,  $a_{a,ave}$  is the average actual values, and  $i$  is the number of input variables.

## 3. Results

### 3.1. Fuel Properties

The properties of pure biodiesel samples, including kinematic viscosity (KV), density (D), oxidation properties (OX), cloud point (CP), and Pour point (PP), are illustrated in Figure 5. It should be noted that the KV and D were measured at 40 °C and 15 °C, respectively. It is found that the values of KV are within the range of 4.33–5.71 mm<sup>2</sup>/s, which met the standard required viscosity values at 40 °C of ASTM D445 (1.9–6.0 mm<sup>2</sup>/s). Additionally, in the case of the EN ISO 3104 standard (3.5–5.0 mm<sup>2</sup>/s), it is found that the KV value of WFME3, WFME4, WFME5, WFME6, WFME7, and WFME8 was above the maximum

limit of the specification in the standard. These results were in agreement with previous reports on the KV value of WFME, PME, and RCME [28,50–65]. Additionally, it was found that all density values of biodiesel samples were above the minimum recommended value of ASTM D854 ( $860 \text{ kg/m}^3$  at  $15^\circ\text{C}$ ), as shown in Figure 2. Additionally, in the case of EN14214 standard (recommended values:  $860\text{--}900 \text{ kg/m}^3$  at  $15^\circ\text{C}$ ), WFME1, WFME2, WFME3, WFME4, WFME5, WFME6, WFME7, WFME8, WFME9, WFME10, WFME11, PME, and RCME were below the maximum specified limit in standard. Compared with other literature results, it is noticed that these results (Figure 2) agreed with previous reports on the density of WFME, PME, and RCME [28–30,39,62,66–68].

Furthermore, it is observed that the minimum and maximum stability values were recorded for WFME15 (6.17 h) and PME (18.35 h), respectively, as shown in Figure 5. Additionally, it is noticed that all oxidation stability values of biodiesel samples were above the minimum specified limit in ASTM D6751 ( $>3.0 \text{ h}$ ) and EN 14214 ( $>6.0 \text{ h}$ ), while the OX value of WFME4–WFME10, WFME18–WFME24, WFME28–WFME39, and PME were above the minimum limit specified in EN 14214:2014 ( $\geq 8 \text{ h}$ ). These observations can be supported by other scientific researchers who measured the OX of biodiesel derived from waste frying oil, palm oil, and refined canola oil [29,68–70].

The acquired CP and PP values for the samples were plotted and are shown in Figure 5. It can be seen that CP and PP values were between  $-4.0\text{--}17.4^\circ\text{C}$  and  $-12.0\text{--}15.0^\circ\text{C}$ , respectively. The CP and PP values for WFME11 and PME were much higher due to the existence of a higher proportion of SFAME. It is a fact that the melting point is inversely related to double bond content; as the former increases, the latter decreases. Many scientific researchers have identified resembling cases [28,39,50,51,68].

Moreover, in this work, PME and RCME were added to the WFME samples to enhance the oxidation stability and cold flow properties (CP and PP). The KV, D, OX, CP, and PP of the sampled WFME-PME, WFME-RCME, and WFME-PME-RCME are illustrated in Figures S1–S3 as Supplementary Material, respectively. It is found that the values of KV are varied from  $4.47 \text{ mm}^2/\text{s}$  (P20WFME18) to  $5.60 \text{ mm}^2/\text{s}$  (P20WFME38) for WFME-PME,  $4.43 \text{ mm}^2/\text{s}$  (R20WFME18) to  $5.56 \text{ mm}^2/\text{s}$  (R20WFME5) for WFME-RCME, and  $4.480 \text{ mm}^2/\text{s}$  (RC20P20WFME18) to  $5.38 \text{ mm}^2/\text{s}$  (R20P20WFME5) for WFME-PME-RCME. These values were met the standard required kinematic viscosity values at  $40^\circ\text{C}$  of ASTM D445 ( $1.9\text{--}6.0 \text{ mm}^2/\text{s}$ ). It should be mentioned that composing blending was carried out as BXWFMEY, where letter B depicts the sort of biodiesel mixed with WFME (P: PME, R: RCME), X is the Mass fraction of biodiesel in WFMEY mixtures, and Y is the number of specimens.

For example, R20P40WFME17 corresponded to a 20% concentration of RCME added to the blend of P40WFME17 (40% concentration of PME added to WFME 17). Additionally, it observed that PME and RCME could be mixed up to 80% with WFME samples without exceeding the standard accepted ratio for biodiesel density.

Furthermore, the initial OX of the WFME samples was above the minimum value specified limit in ASTM D6751 ( $>3.0 \text{ h}$ ) and EN 14214 ( $>6.0 \text{ h}$ ). In contrast, the OX value of RCME was not satisfactory according to the oxidative stability specification listed in ASTM D6751 and EN 14214. In contrast, the OX value of PME has met the recommended oxidation stability specification in EN 14214:2014 ( $\geq 8 \text{ h}$ ) due to the high percentage of SFAM. Based on the results, it is observed that it was necessary to add a high proportion of PME to the WFME samples having low OX values would help to increase the OX stability to meet the recommended oxidation stability specification in EN 14214:2014 ( $\geq 8 \text{ h}$ ). In addition, mixing WFME18 with RCME helped increase the OX stability from  $2.60 \text{ h}$  (RCME) to  $11.70 \text{ h}$  (RC20 WFME18) and improved the cold flow properties of the WFME samples and WFME-PME samples, as shown in Figures S1–S3 as Supplementary material.

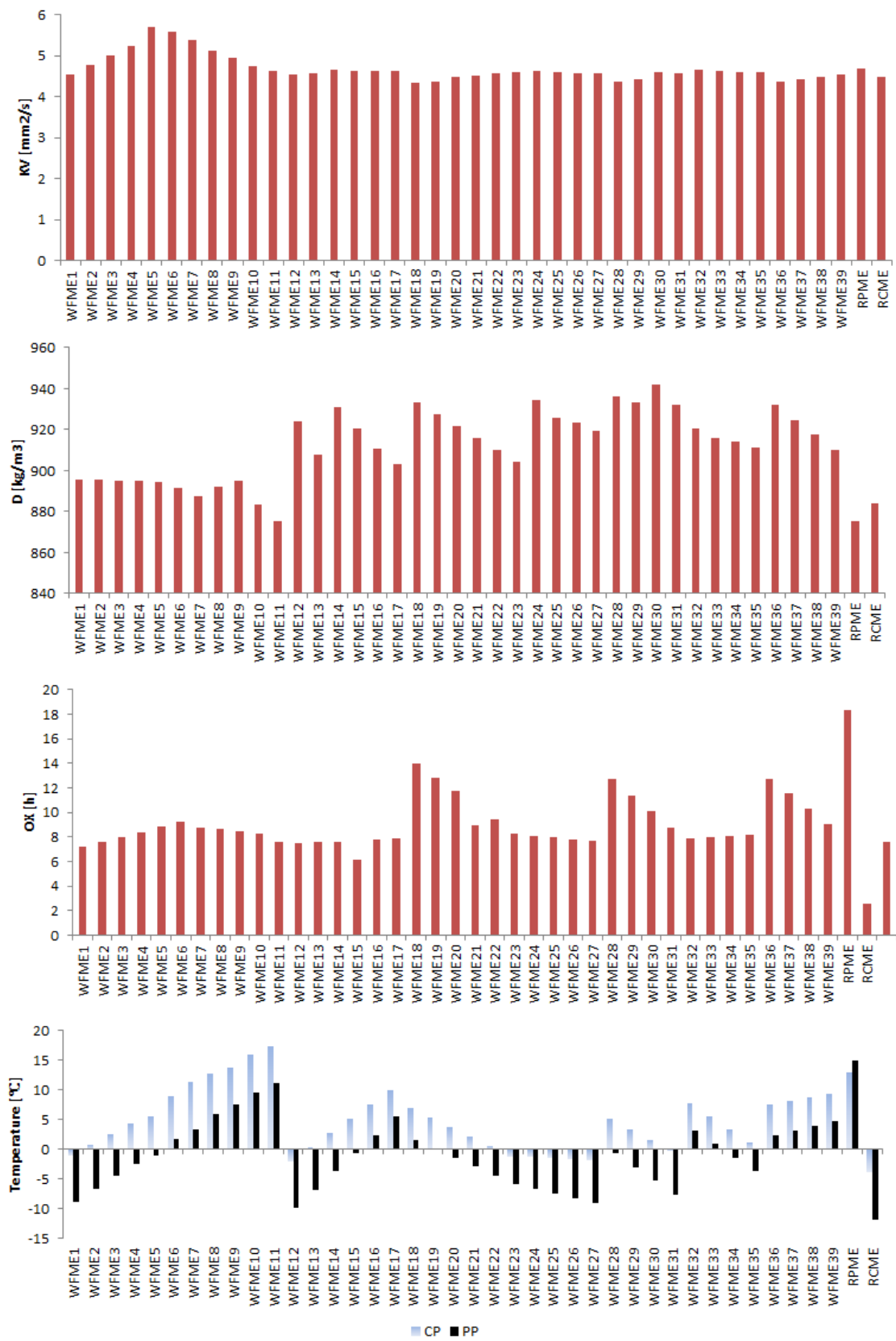


Figure 5. Properties of pure biodiesel samples.

### 3.2. Empirical Models

As mentioned previously, four neural network models were employed to predict the oxidation stability of the biodiesel samples. Thus, the concentration amount of WFME, PME, and RCME in the mixture, the value of total saturated, total monounsaturated, total polyunsaturated, very-long-chain fatty acid, degree of unsaturation, long-chain saturated factor, kinematic viscosity, density, cloud point, and pour point were used as explanatory input variables. The data were divided into training and testing groups and the results by the models were compared with each other. In this study, the data are divided into about 70% of the collect data (353 data) for training and the remaining data (156 data) for testing. The training was done using data for WFME, WFME-PME, and WFME-PME-RCME, and the developed model was used to predict the oxidation stability of WFME-RCME, then compared with the actual data obtained by performing laboratory tests on actually prepared WFME-RCME samples. The summary statistics, including standard deviation (SD), coefficient of variation (CV), minimum (Min.), and maximum (Max.) of the selected variables, are listed in Table 2.

**Table 2.** Statistical parameters of used variables.

Data	Variable	Explanation	SD	CV	Max.	Min.	Unit
Training	X <sub>1</sub>	Concentration amount of WFME in the mixture	26.47	47.43	20	100	%
	X <sub>2</sub>	Concentration amount of PME in the mixture	26.47	59.89	0	80	%
	X <sub>3</sub>	Concentration amount of RCME in the mixture	28.98	131.16	0	80	%
	$\sum SFAMs$	Total saturated	8.013	26.02	6.73	44.9	wt%
	$\sum MUFAMs$	Total monounsaturated	4.751	9.63	40.42	65.43	wt%
	$\sum PUFAMs$	Total polyunsaturated	3.886	19.75	11.2	29.91	wt%
	VLCA	Very-long-chain fatty acid	0.3461	38.03	0	1.98	wt%
	DU	Degree of unsaturation	11.64	13.13	65.9	120.67	wt%
	LCSF	Long-chain saturated factor	0.9306	19.77	1.808	6.36	wt%
	$\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}$	Ratio	1.5297	59.16	1.2183	13.3967	-
	KV (at 40 °C)	Kinematic viscosity	0.1859	3.95	4.3285	5.705	Mm <sup>2</sup> /s
	D (at 15 °C)	Density	13.84	1.54	875	941.79	Kg/m <sup>3</sup>
	CP	Cloud Point	3.678	50.36	−4	17.4	°C
	PP	Pour Point	5.203	120.92	−12	15	°C
	XO	Oxidation stability	2.68	21.89	2.6	18.35	h
Testing	X <sub>1</sub>	Concentration amount of WFME in the mixture	22.43	44.87	20	80	%
	X <sub>2</sub>	Concentration amount of PME in the mixture	0	*	0	0	%
	X <sub>3</sub>	Concentration amount of RCME in the mixture	22.43	44.87	20	80	%
	$\sum SFAMs$	Total saturated	6.765	44.03	6.932	35.738	wt%
	$\sum MUFAMs$	Total monounsaturated	4.399	7.84	44.386	64.394	wt%
	$\sum PUFAMs$	Total polyunsaturated	2.254	8.28	19.598	29.76	wt%
	VLCA	Very-long-chain fatty acid	0.3567	23.61	0.396	1.968	wt%
	DU	Degree of unsaturation	8.34	7.54	83.58	120.55	wt%
	LCSF	Long-chain saturated factor	0.7674	26.06	1.8462	4.999	wt%
	$\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}$	Ratio	2.974	45.01	1.79	13.081	-
	KV (at 40 °C)	Kinematic viscosity	0.1895	4.09	4.4343	5.5595	Mm <sup>2</sup> /s
	D (at 15 °C)	Density	11.9	1.32	880.83	934.41	Kg/m <sup>3</sup>
	CP	Cloud Point	3.413	811.73	−3.6	13.12	°C
	PP	Pour Point	3.817	−57.83	−11.6	6.48	°C
	XO	Oxidation stability	1.744	30.06	3.308	11.72	h

\* Not determined.

Moreover, three conditions were considered in the model development of empirical models with different input combinations and are utilized for training the model to identify the best variety of inputs to estimate the oxidation stability of biodiesel. Several empirical models with various possible combinations of the used inputs were built in this work. Next,

they were trained respectively, and then the performance of these models was estimated. The best models that gave the highest performance are shown in Table 3.

**Table 3.** Proposed models with different input combinations.

Model Name	Combination of Input
Model 1	$X1, X2, X3, \sum SFAMs, \sum MUFAMs, \sum PUFAMs, VLCFA, DU, LCSF,$ and $\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}$
Model 2	$X1, X2, X3, \sum SFAMs, \sum MUFAMs, \sum PUFAMs, VLCFA, DU, LCSF$ and $\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}, KV$ (at 40 °C) and D (at 15 °C)
Model 3	$X1, X2, X3, \sum SFAMs, \sum MUFAMs, \sum PUFAMs, VLCFA, DU, LCSF$ and $\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}, KV$ (at 40 °C), D (at 15 °C), CP and PP

### 3.2.1. Machine Learning Models

A string of models were studied to reasonably guess the best number of hidden layers (HL), the number of neurons (NN), and transfer function (TF) for the MFFNN, CFNN, and ENN models. It should be mentioned that the number of HLs and NNs in the MFFNN, CFNN, and ENN models were established by using trial and error methods.

Based on the value of MSE, it was found that one hidden layer and five neurons are selected as the best for the MFFNN model (5:1:1). At the same time, it was found that one hidden layer and ten neurons were chosen as an optimum number for the CFNN model (5:1:1). Additionally, it was observed that the ENN model (5:1:1) with eight and ten neurons has the minimum MSE. Table 4 shows the best number of hidden layers (HL) and neuron (NN)s and the activation function (AF) that was chosen for each ANN model.

**Table 4.** Performance of the proposed models.

Machine Learning Model	Model Name	TF	HL	NN	MSE (Training)	Epoch	R <sup>2</sup> (Training)
MFFNN	Model 1	1	5	TANSIG	$9.29 \times 10^{-5}$	759	0.9984
	Model 2	1	5	TANSIG	$1.66 \times 10^{-4}$	18	0.9936
	Model 3	1	5	TANSIG	$9.06 \times 10^{-5}$	325	0.9962
CFNN	Model 1	1	5	LOGSIG	$2.06 \times 10^{-4}$	19	0.9911
	Model 2	1	5	LOGSIG	$7.26 \times 10^{-5}$	345	0.9978
	Model 3	1	5	LOGSIG	$2.02 \times 10^{-4}$	8	0.9916
ENN	Model 1	1	8	TANSIG	$3.74 \times 10^{-5}$	999	0.9988
	Model 2	1	10	TANSIG	$1.42 \times 10^{-4}$	294	0.9897
	Model 3	1	10	TANSIG	$1.06 \times 10^{-4}$	912	0.9992

Furthermore, the 10th order root of the input data was utilized instead of the actual input data to better perform for the RBFNN model. This assists in evening out the variation of the input data points inside a narrow span, and this gives better precision of the applied model. The data points were haphazardly split into training and testing subcategories. This process was executed many times to stop the gathering of data points in the preferred domain of the problem and allow even spread of data points inside the training and testing subcategories. Typically, the distribution and the maximum number of neurons (MNN) have great significance in the fabric of RBFNN, as the performance and the values of these parameters crucially influence the precision of the applied model.

Similarly, the optimum values of these parameters were estimated by a trial and error approach. It was observed that the optimum values that provide the most accurate performance for the RBFNN model are 0.002 and 230 for the spread and MNN, respectively. In general, R-squared was used to evaluate the performance of artificial models. R-squared means the degree of the linear relationship between the observed and modeled values. The line is almost straight with a 45° angle, and this proves the accuracy of the provided model. For the training phase, the R-squared value was found to be approximately 0.99, as shown

in Table 4. The results obtained from the ANN models show that the use of ANN is enough to predict the oxidation stability of biodiesel.

### 3.2.2. Poisson Regression Model (PRM)

The developed PRM was implemented to predict the oxidation stability of WFME-RCME. The data of the concentration amount of WFME, PME, and RCME in the mixture, the value of total saturated, total monounsaturated, total polyunsaturated, very-long-chain fatty acid, degree of unsaturation, long-chain saturated factor, kinematic viscosity, density, cloud point, and pour point were used to generate a mathematical equation as given in Table 5. The actual data results and the corresponding values predicted by Equations (Table 5) are displayed in Figure 6. To test the fit of the model, R-squared was determined. For higher modeling accuracy, the R-squared value should be closer to 1. In this case, the values of R-squared for training data were within the range of 0.9769–0.9811 for all proposed models.

**Table 5.** The mathematical equation used to predict the OX value of biodiesel samples.

Model Name	Mathematical Equation
Model 1	$OX = EXP(-7.2 + 0.027 \cdot X_1 + 0.121 \cdot X_3 - 3.5 \cdot \sum SFAMs + 7.47 \cdot \sum MUFAMs + 1.43 \cdot \sum PUFAMs - 2.24 \cdot VLCFA + 10.38 \cdot LCSF - 0.74 \cdot (\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}))$
Model 2	$OX = EXP(-7.2 + 0.016 \cdot X_1 + 0.147 \cdot X_3 - 3.5 \cdot \sum SFAMs + 7.33 \cdot \sum MUFAMs + 1.33 \cdot \sum PUFAMs - 2.25 \cdot VLCFA + 10.39 \cdot LCSF - 0.58 \cdot (\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}) + 0.158 \cdot KV + 0.172 \cdot D)$
Model 3	$OX = EXP(-7.0 + 0.046 \cdot X_1 + 0.135 \cdot X_3 - 4.1 \cdot \sum SFAMs + 7.4 \cdot \sum MUFAMs + 1.06 \cdot \sum PUFAMs - 2.18 \cdot VLCFA + 11.1 \cdot LCSF - 0.55 \cdot (\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}) + 0.20 \cdot KV + 0.139 \cdot D + 0.61 \cdot CP - 0.80 \cdot PP)$

### 3.3. Performance Evaluation of Artificial Models and Mathematical Models for Testing Data

The data were divided into training and testing groups and the results by the models were compared with each other. In this study, the training was done using data for WFME, WFME-PME, and WFME-PME-RCME. The developed model was used to predict the OX values for WFME-RCME samples, and then compared with the actual data obtained by performing laboratory tests on actually prepared WFME-RCME.

In this study, the statistical approach using Analysis of Variance (ANOVA) parameters, namely  $R^2$ , SEP, MAE, RMSE, and ADD, was used to assess and evaluate the predictive capability of MFFNN, CFNN, ENN, RBFNN, and PRM as listed in Table 6. RMSE, SEP, and MAE values are used to estimate the error in the predicted data, while ADD value measures the accuracy of the developed models [71,72]. It was observed that CFNN (model 3) and RBFNN (model 2) gave good predictions according to the R-squared values for the testing data. In addition, it was found that the RBFNN has the lowest value of RMSE, MAE, SPE, and ADD for the testing data, as shown in Table 6. Moreover, Figures 7–10 compare the estimated and observed values of the deviator stress for all models. Out of the proposed models, Model 2 has given the best prediction with the combinations of ( $X_1$ ,  $X_2$ ,  $X_3$ ,  $\sum SFAMs$ ,  $\sum MUFAMs$ ,  $\sum PUFAMs$ ,  $VLCFA$ ,  $DU$ ,  $LCSF$ ,  $\frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}$ ,  $KV$  (at 40 °C), and  $D$  (at 15 °C)). The proposed approach illustrates how the RBFNN modeling technique can be used to identify the critical variables required to the most significant meteorological parameters affecting the oxidation stability of biodiesel.

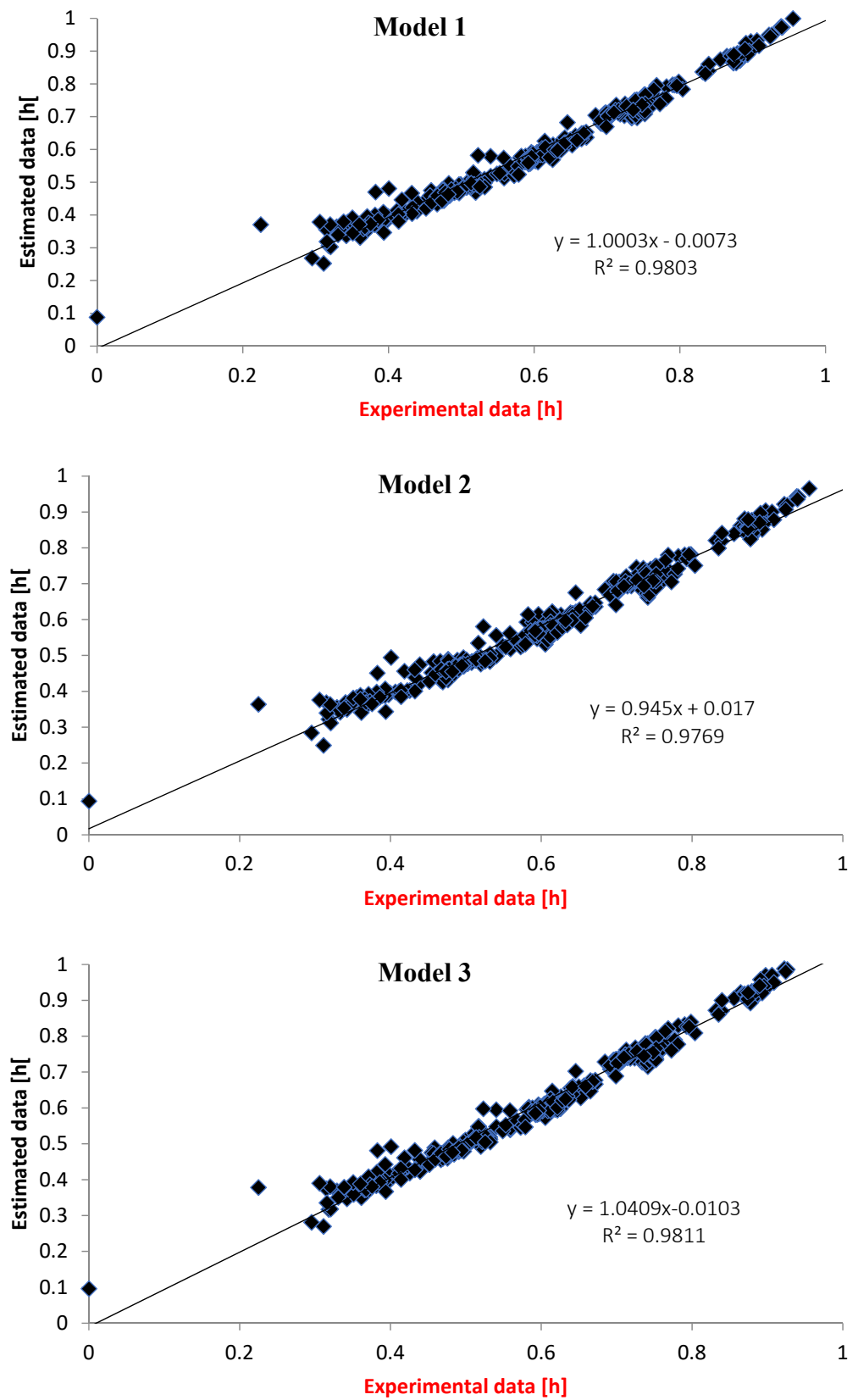
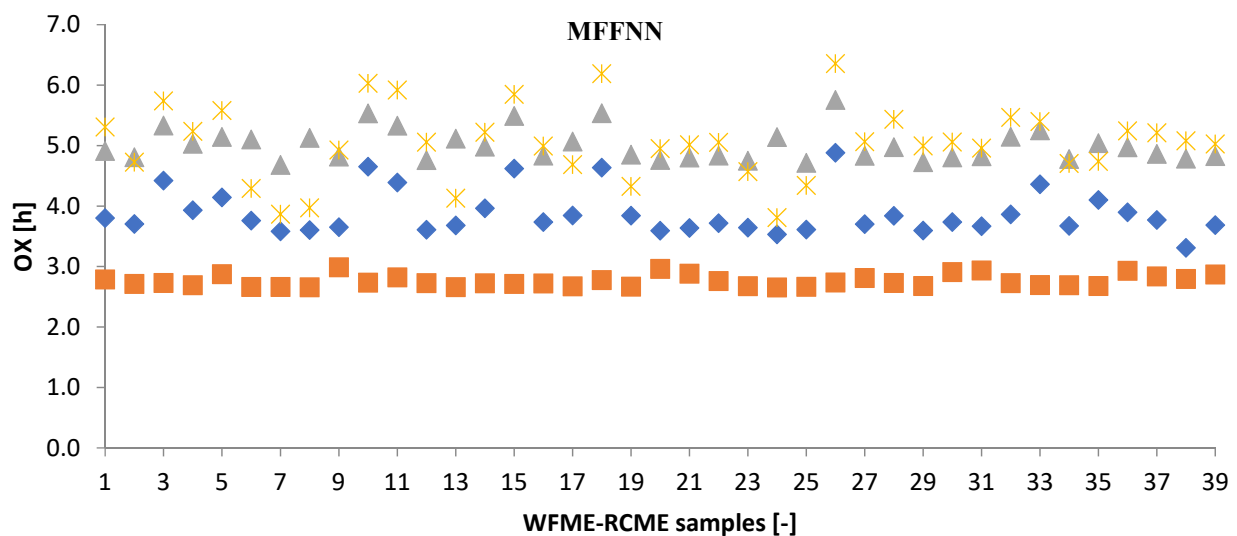


Figure 6. Comparison between estimated data with experimental data of oxidation stability.

**Table 6.** Performance evaluation of the models.

Volume Fraction of RCME	Statistical Indicator	FFNN			CFNN			ENN		
		Model 1	Model 2	Model 3	Model 1	Model 2	Model 3	Model 1	Model 2	Model 3
80%	R <sup>2</sup>	0.7991	0.0051	0.5890	0.3389	0.0060	0.8949	0.3389	0.8283	0.1349
	RMSE	1.1328	1.1838	1.2243	0.3454	0.6959	0.6502	0.3454	0.9031	2.0591
	MAE	1.1195	1.1216	1.1580	0.2637	0.5601	0.5813	0.2637	0.8479	1.9408
	SEP [%]	40.5801	28.9035	23.1596	6.1730	11.1167	15.6565	8.6950	25.7013	52.2759
	ADD [%]	29.3626	28.3311	29.8648	6.4473	14.7524	14.4612	6.4473	21.3468	50.3830
60%	R <sup>2</sup>	0.7916	0.0218	0.8205	0.7309	0.2397	0.9354	0.6757	0.5071	0.4765
	RMSE	1.4319	2.0104	1.0372	2.5319	2.4843	1.4000	0.8627	1.7190	2.5829
	MAE	1.3492	1.8567	0.9232	2.4335	2.0343	1.3124	0.7540	1.6330	2.3980
	SEP [%]	40.8346	35.9766	14.1804	34.2581	33.6743	48.1172	21.3737	42.4309	54.0799
	ADD [%]	26.2692	35.0161	17.6570	46.2930	39.7644	24.6975	13.9619	31.0069	46.5722
40%	R <sup>2</sup>	0.7252	0.3923	0.8731	0.8005	0.4275	0.9440	0.7737	0.6157	0.3441
	RMSE	2.2280	2.5151	1.0236	3.4191	2.7897	1.4965	1.1222	2.0331	2.4568
	MAE	1.9370	2.3690	0.8338	3.2888	2.3318	1.4146	1.0241	1.9195	2.2607
	SEP [%]	47.5647	36.7778	10.2969	37.6053	32.8045	44.8733	22.6488	38.1872	41.5207
	ADD [%]	29.4424	36.0984	12.5047	50.1892	36.6401	21.4080	15.7027	29.4800	35.9919
20%	R <sup>2</sup>	0.7640	0.7305	0.8968	0.9158	0.7493	0.9552	0.8699	0.4941	0.8288
	RMSE	2.7585	2.4453	0.7200	2.8433	1.8142	0.7945	0.9900	1.7729	1.1751
	MAE	2.3567	2.3227	0.5572	2.7589	1.5783	0.7510	0.8637	1.3976	1.0920
	SEP [%]	43.6498	30.0795	5.5680	29.6656	19.7853	15.1332	13.6207	19.9475	15.8655
	ADD [%]	29.8220	29.8999	7.2084	35.4254	20.9252	9.6503	11.2800	17.6835	14.8233
80%	R <sup>2</sup>	0.0002	0.9427	0.1020	0.1594	0.2171	0.2508			
	RMSE	5.6655	0.0942	2.3867	1.3278	1.2901	1.5098			
	MAE	5.6520	0.0689	2.1923	1.2798	1.2486	1.4761			
	SEP [%]	147.0920	1.2357	22.9985	24.9530	20.5602	28.6048			
	ADD [%]	147.5842	1.8045	57.0214	33.7886	32.9778	38.8593			
60%	R <sup>2</sup>	0.0002	0.9471	0.4375	0.4307	0.4938	0.5447			
	RMSE	4.1872	0.1676	1.7904	1.0019	0.9461	1.1475			
	MAE	4.1123	0.1023	1.6346	0.8699	0.8297	1.0388			
	SEP [%]	80.0758	1.3712	17.6268	14.6157	12.2521	17.3059			
	ADD [%]	82.7778	2.0723	32.3416	17.9959	17.1649	21.3994			
40%	R <sup>2</sup>	0.0002	0.9481	0.8118	0.6853	0.7123	0.7552			
	RMSE	2.8745	0.2464	0.9742	0.7856	0.7597	0.8964			
	MAE	2.63924	0.14269	0.88132	0.67287	0.64838	0.76202			
	SEP [%]	40.9905	1.77558	9.73032	9.78586	8.91425	11.0382			
	ADD [%]	44.3097	2.38234	14.2071	11.0757	10.6262	12.8206			
20%	R <sup>2</sup>	0.00032	0.94878	0.95132	0.83521	0.83661	0.86433			
	RMSE	1.97698	0.32938	0.42331	0.66956	0.67909	0.75028			
	MAE	1.76736	0.1827	0.32411	0.54833	0.54779	0.60237			
	SEP [%]	22.7605	2.10091	3.64829	6.88776	6.8504	7.60394			
	ADD [%]	24.2113	2.61405	4.47543	7.41835	7.46685	8.56032			



**Figure 7.** Cont.

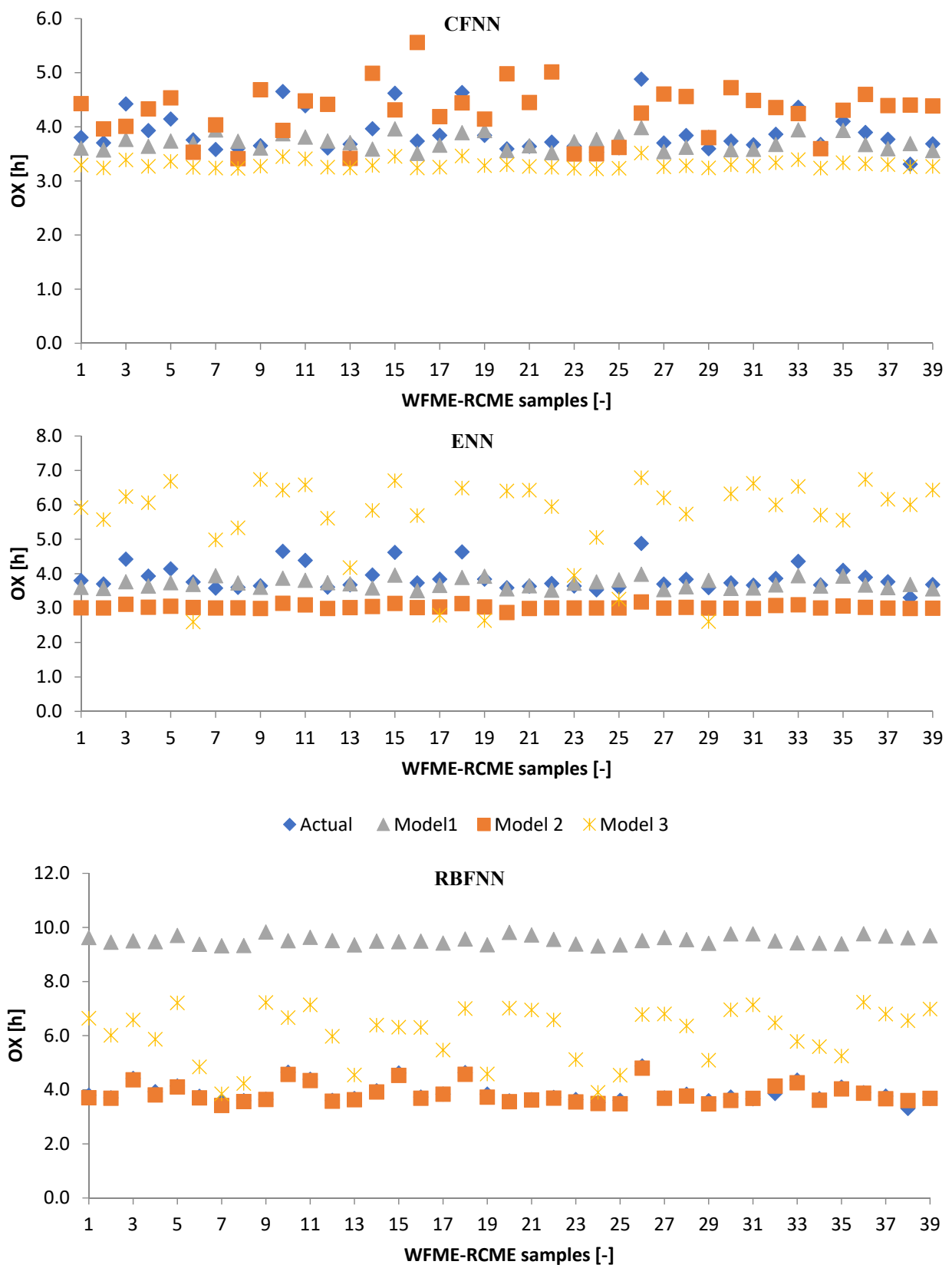


Figure 7. Cont.

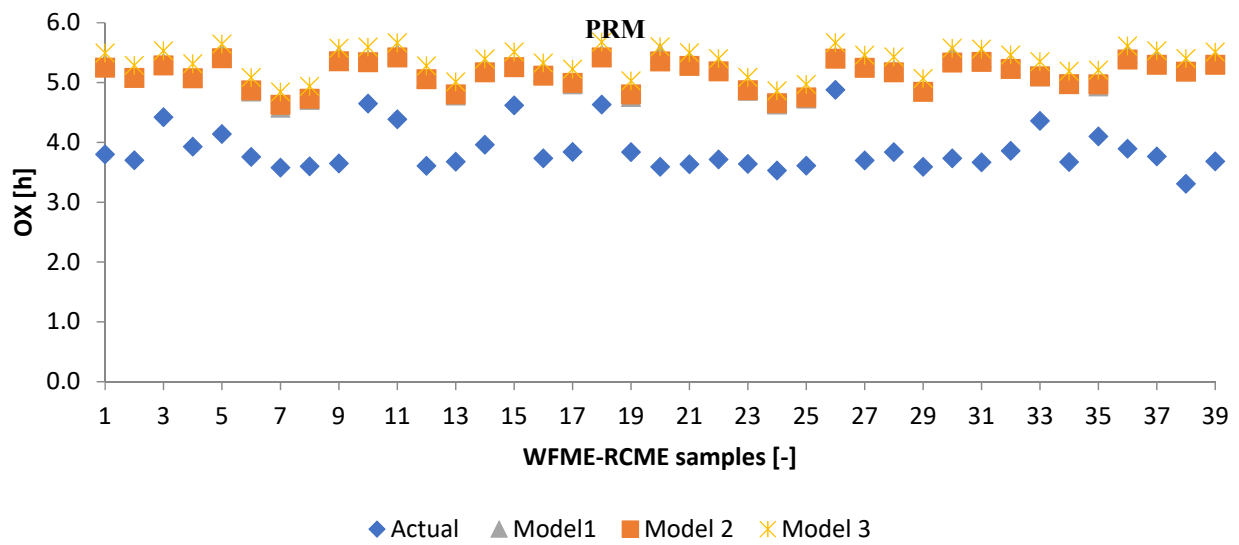


Figure 7. Comparison of the predicted and observed values of the OX values of WFME-RCME (20–80%).

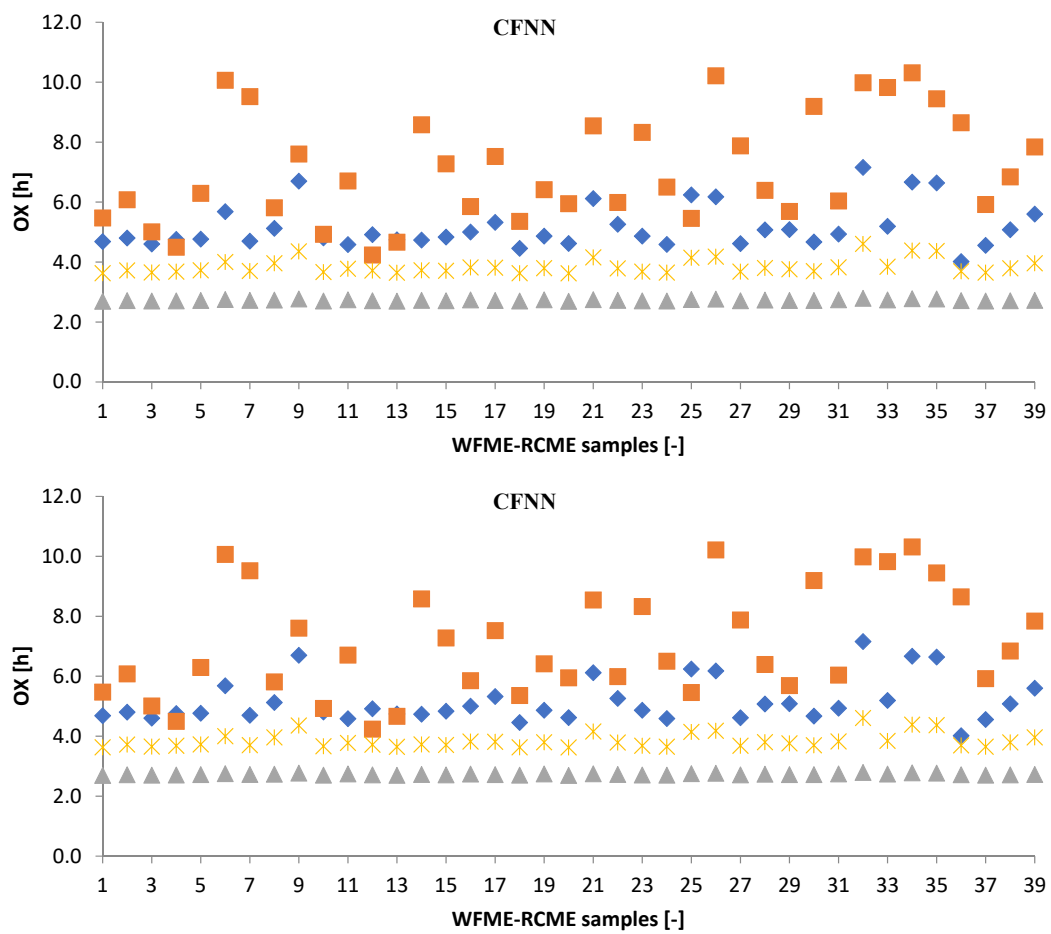
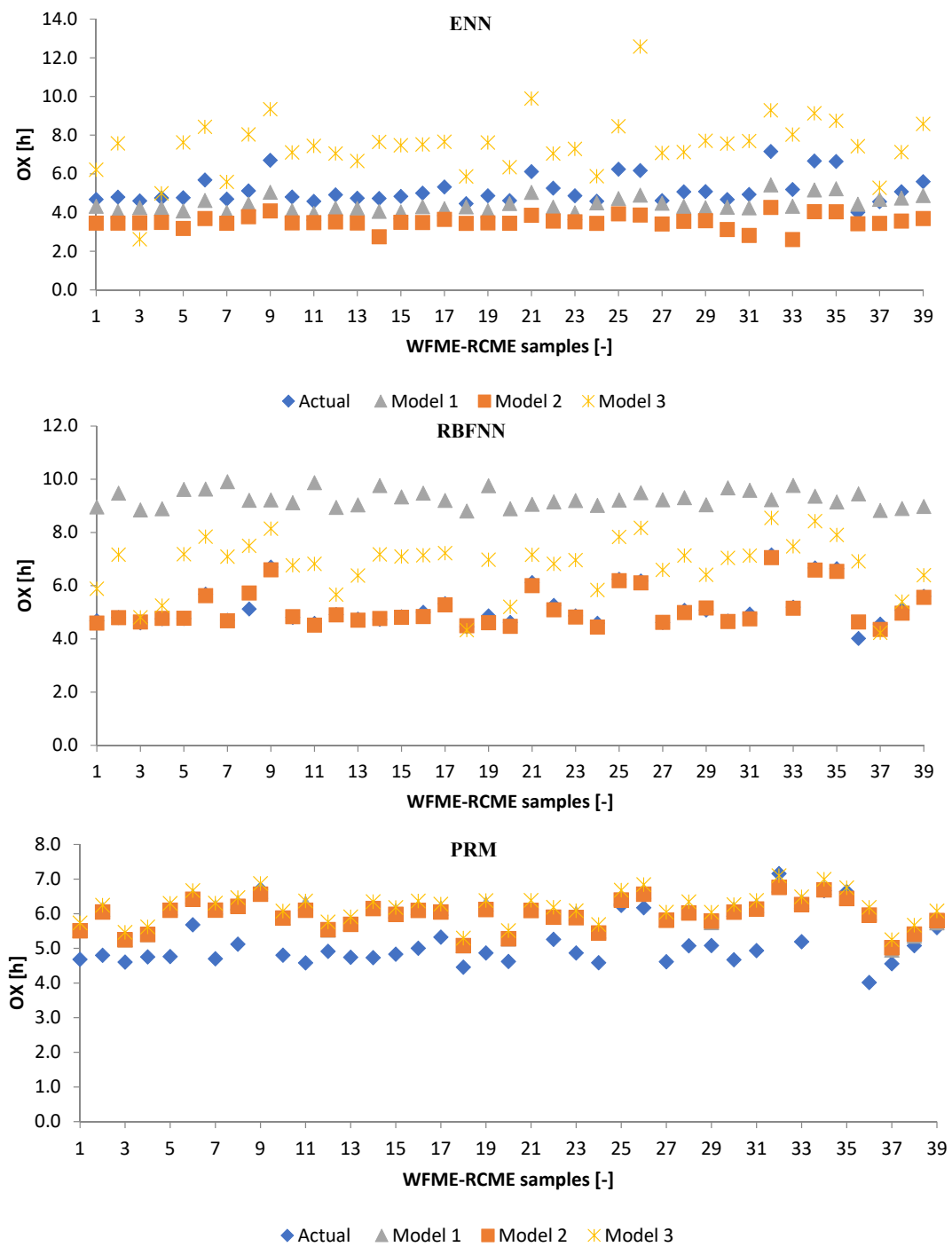


Figure 8. Cont.



**Figure 8.** Comparison of the predicted and observed values of the OX values of WFME-RCME (40–60%).

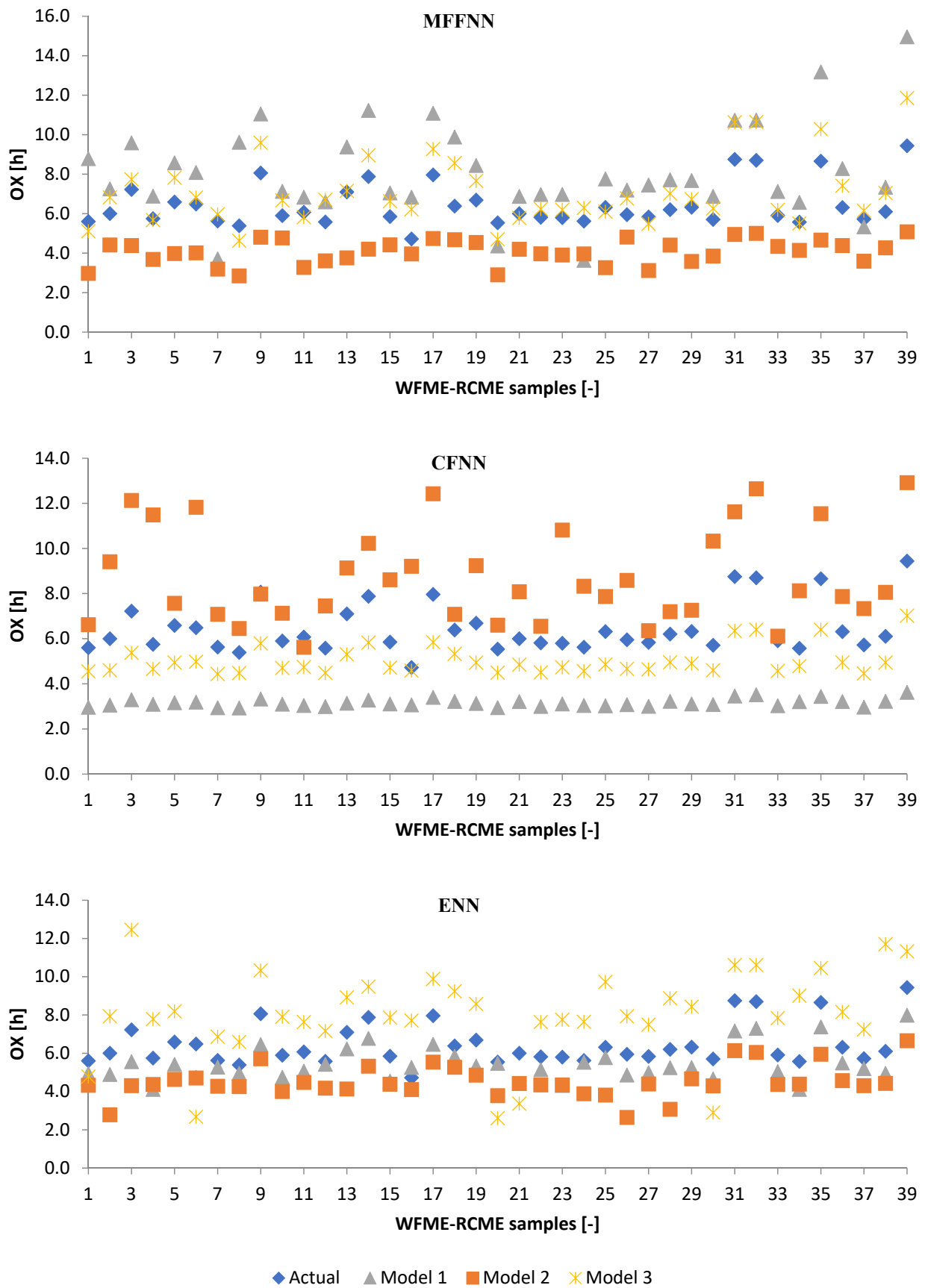
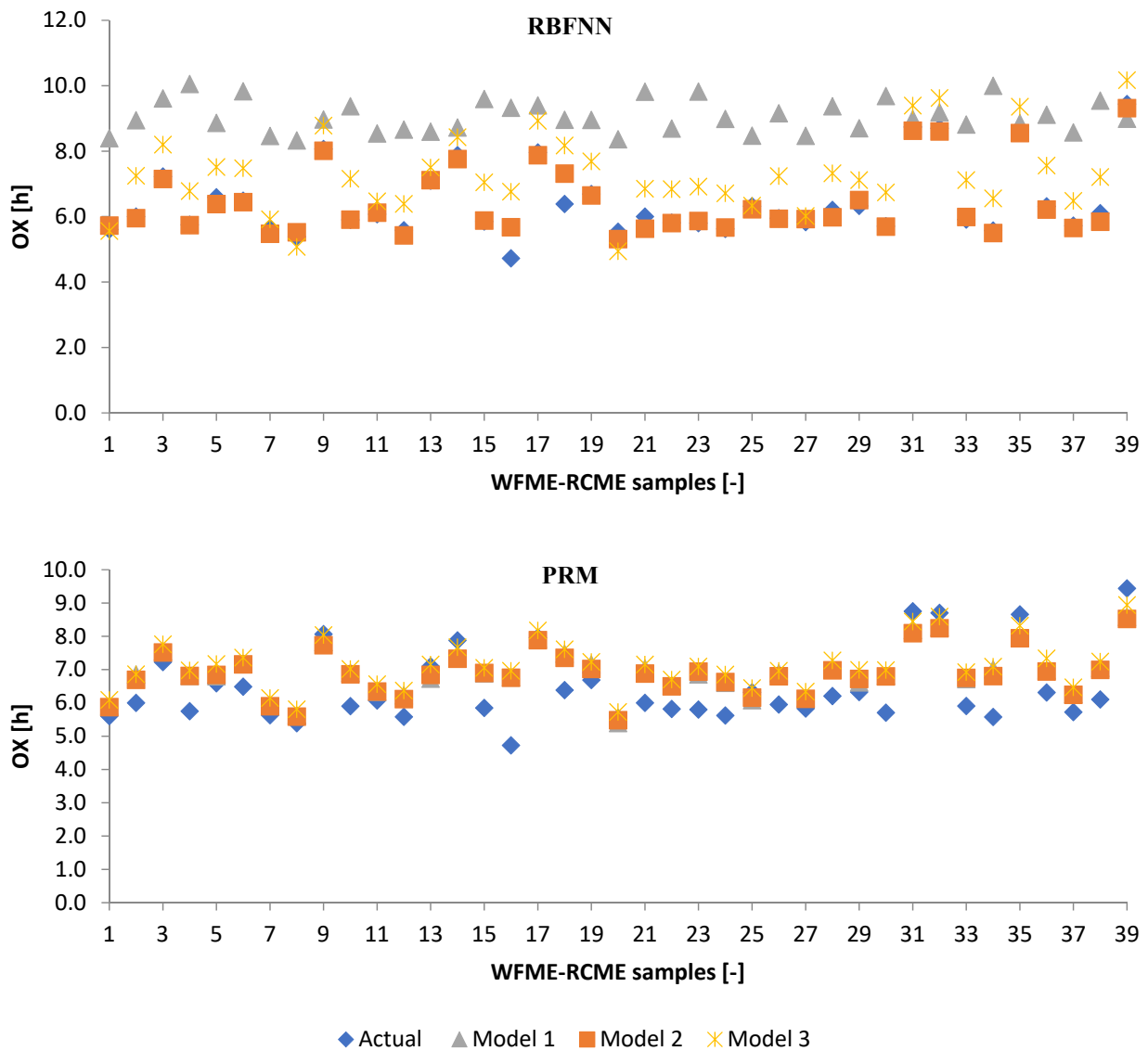
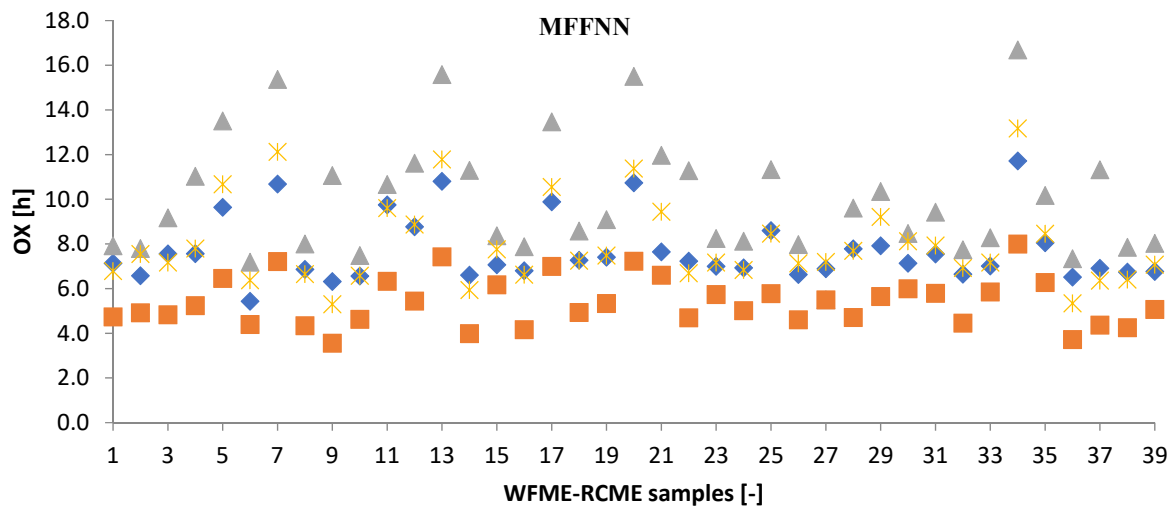


Figure 9. Cont.



**Figure 9.** Comparison of the predicted and observed values of the OX values of WFME-RCME (60–40%).



**Figure 10.** Cont.

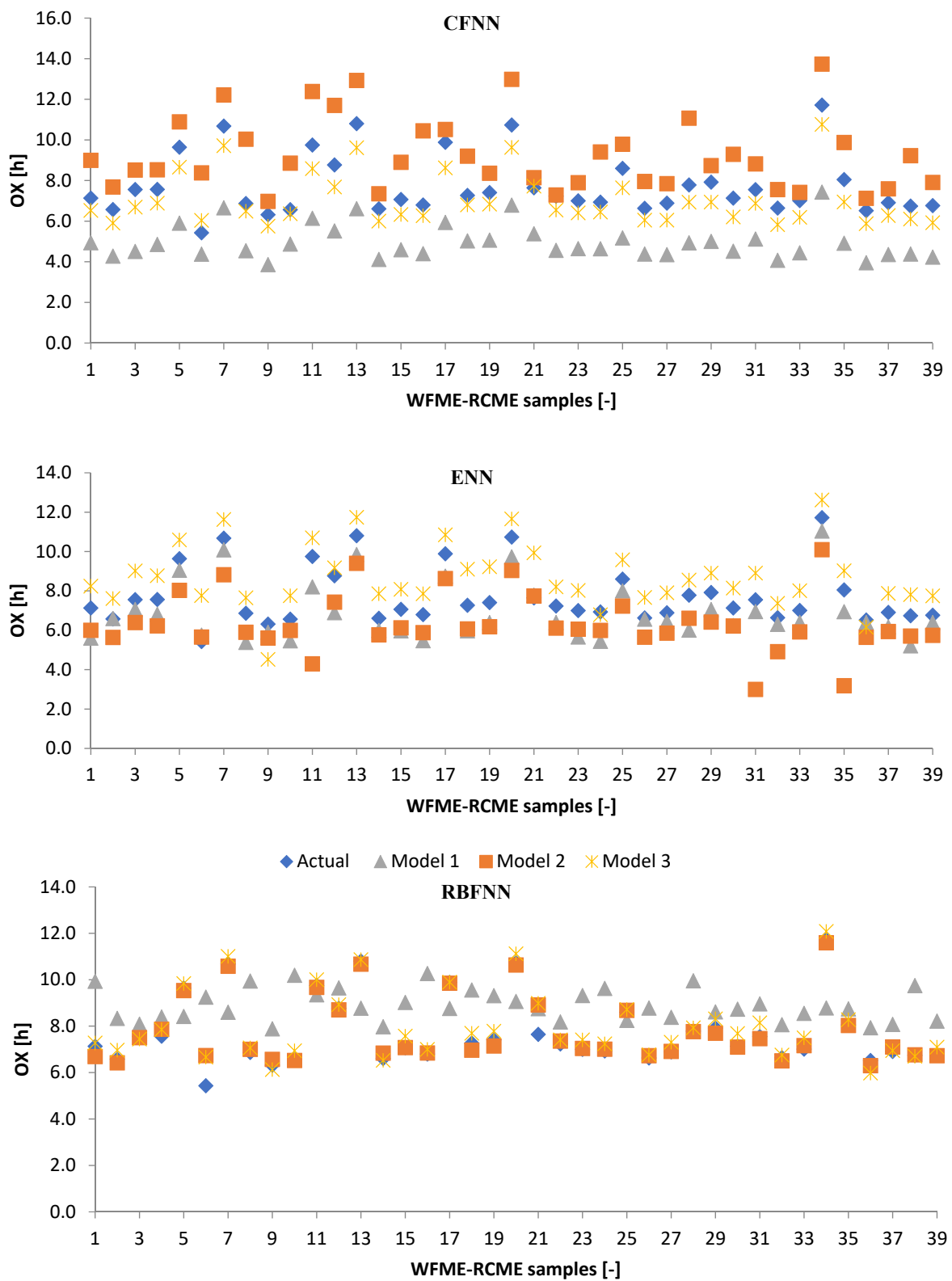
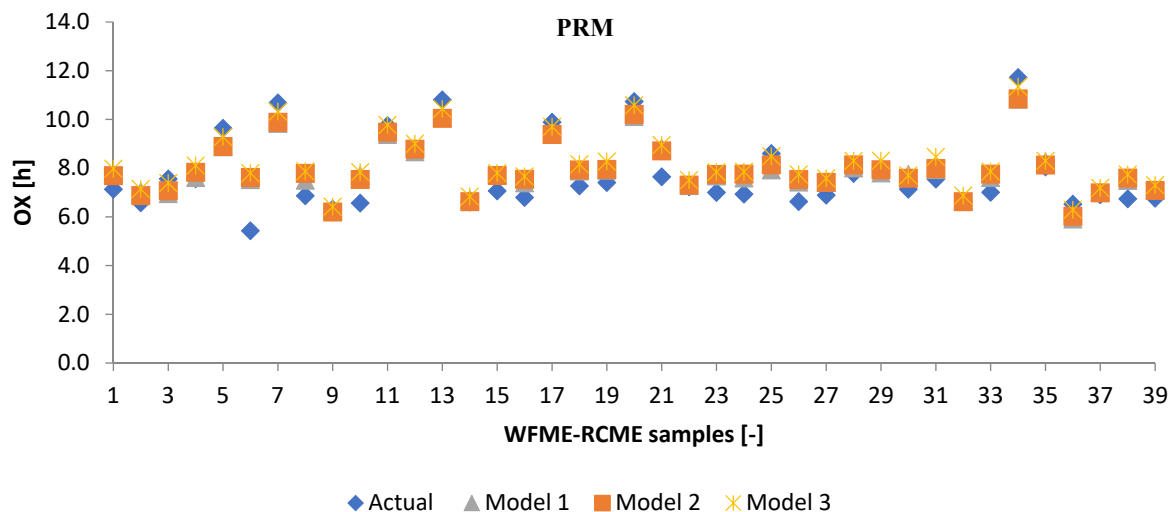


Figure 10. Cont.



**Figure 10.** Comparison of the predicted and observed values of the OX values of WFME-RCME (80–20%).

#### 4. Conclusions

In the present study, the potential of using PME and RCME as an additive to improve the stability and cold flow properties of WFME samples was evaluated. The kinematic viscosity, density, cloud point, pour point, and oxidation stability of 39 WFME samples and their blends with various percentages of PME and RCME were experimentally measured. The results demonstrated that adding a high proportion of PME to the WFME samples with low oxidation stability values would help increase the stability of the samples to meet the recommended oxidation stability specification in EN 14214:2014 ( $\geq 8$  h). In addition, mixing WFME18 with RCME helped increase the OX stability from 2.60 h (RCME) to 11.70 (RC20WFME18) and improve the cold flow properties of the WFME and WFME-PME samples. Moreover, this study evaluated the accuracy of Poisson Regression Model (PRM) and Multilayer Feed-Forward Neural Network (MFFNN), Cascade Feed-forward Neural Network (CFNN), Radial Basis Neural Network (RBNN), and Elman neural network (ENN) with different combinations of input parameters. The parameters include concentration amount of WFME, PME, and RCME in the mixture, the value of total saturated, total monounsaturated, total polyunsaturated, very-long-chain fatty acid, degree of unsaturation, long-chain saturated factor, kinematic viscosity, density, cloud point, and pour point. The results demonstrated that the RBFNN model combined  $X1, X2, X3, \sum SFAMs, \sum MUFAMs,$  and  $\sum PUFAMs$ .  $VLCA, DU, LCSF, \frac{\sum MUFAMs + \sum PUFAMs}{\sum SFAMs}, KV,$  and  $D$  had the lowest value of Root Mean Squared Error and Mean Absolute Error. In the end, the results demonstrated that the RBFNN model performed well and presented high accuracy in estimating the value of OX for the biodiesel samples compared to PRM, MFFNN, CFNN, and ENN.

An interesting future study might evaluate the accuracy of the proposed models on other combinations of different biodiesel samples having similar physical and chemical properties. Moreover, future research should focus on assessing the effects of the storage period and storage conditions on the properties of biodiesel, mainly oxidation stability, kinematic viscosity, and density, to find a suitable sample that can be used for vehicle engines in Northern Cyprus.

**Supplementary Materials:** The following are available online at <https://www.mdpi.com/article/10.3390/en15020407/s1>, Figure S1: Properties of WFME-PME with various volume of ratio, Figure S2: Properties of WFME-RCME with various volume of ratio, Figure S3: Properties of WFME-PME-RCME with various volume of ratio.

**Author Contributions:** A.M.R.A.-A. measured the physicochemical properties of the fuel. H.Ç. analyzed the data and wrote the paper. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research received no external funding.

**Institutional Review Board Statement:** Not applicable.

**Informed Consent Statement:** Not applicable.

**Data Availability Statement:** Not applicable.

**Conflicts of Interest:** The authors declare no conflict of interest.

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