



Dynamics of Pressure Variation in Closed Vessel Explosions of Diluted Fuel/Oxidant Mixtures

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Abstract: Nitrous oxide is widely used as oxidizer or nitriding agent in numerous industrial activities such as production of adipic acid and caprolactam and even for production of some semiconductors. Further, it is used as an additive in order to increase the power output of engines, and as an oxidizer in propulsion systems of rockets, because it has a large heat of formation (+81.6 kJ mol⁻¹). N₂O is highly exothermic, and during its decomposition a supplementary heat amount is released, so it needs special handling conditions. The combustion of fuels in nitrous oxide atmosphere can lead to high unstable and turbulent deflagrations that speedily self-accelerate and therefore a deflagration can change to a detonation. The peak explosion pressure and the maximum rate of pressure rise of explosions in confined spaces are key safety parameters to evaluate the hazard of processes running in closed vessels and for design of enclosures able to withstand explosions or of their vents used as relief devices. The present study reports some major explosion parameters such as the maximum (peak) explosion pressures p_{max} , explosion times θ_{max} , maximum rates of pressure rise $(dp/dt)_{max}$ and severity factors K_G for ethylene-nitrous oxide mixtures (lean and stoichiometric) diluted with various amounts of N₂, at various initial pressures ($p_0 = 0.50-1.50$ bar), in experiments performed in a spherical vessel centrally ignited by inductive-capacitive electric sparks. The influence of the initial pressure and composition on p_{max} , θ_{max} and $(dp/dt)_{max}$ is discussed. The data are compared with similar values referring to ethylene-air mixtures measured in the same initial conditions. It was found that at identical C/O ratios with ethylene-air, ethylene-N₂O-N₂ mixtures develop higher explosion pressures and higher rates of pressure rise, due to the exothermic dissociation of N₂O under flame conditions.

Keywords: ethylene; nitrous oxide; nitrogen dilution; pressure dynamics; confined explosions

1. Introduction

Combustion is the major energy production process, so the study of flammability features of gaseous combustible mixtures at various initial conditions still represents a major challenge for researchers. Fuel–air combustion has been intensively studied, but in recent years an important concern has been raised: not only to find alternative fuels to substitute the conventional fuels, but also to find alternative oxidizers to replace oxygen. Nitrous oxide (N₂O, also known as laughing gas) is a strong oxidizing agent, roughly equivalent to hydrogen peroxide, and much stronger than oxygen gas. It was used as oxidizer in the semiconductors industry and as a rocket propulsion system [1–3]. On the other hand, N₂O is highly exothermic and during its decomposition a supplementary heat amount is released, so its handling is critical.

As an oxidizer, N₂O can easily decompose to oxygen and nitrogen at elevated pressures and temperatures [2,4]. Numerous studies were published on fuel-N₂O mixtures in terms of flammability parameters such as flammability limits, ignition energy, flame speeds, etc. The explosion ignition and propagation in H₂-CH₄-NH₃-N₂O-O₂-N₂ mixtures was studied by Pfahl et al. [5]. They reported flammability limits, ignition energies and flame speeds



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). in combustion vessels at initial pressure of 1 bar and initial temperature of 295 K. Some investigations on N_2O flames focused on the flammability domain of different fuel- N_2O mixtures (flammability limits) in the presence of inert gases [6,7].

The explosion parameters of toluene/N₂O at initial pressure of 1 or 6 bar and initial temperature of 343 K from measurements in an 8 L spherical vessel were reported by Vandebroek et al. [6]. The explosion features of volatile organic vapours, such as n-pentane, diethyl ether and diethyl amine, and of C₁-C₈ n-alkanes in N₂O atmosphere in a cylindrical explosion vessel were studied by Koshiba et al. [2,8] and compared with those of mixtures containing O₂.

Vandooren et al. [9] conducted a study on the flame structure of stoichiometric methane-N₂O-Ar and methane-O₂-Ar by means of the molecular beam sampling and mass spectroscopy methods. The propagation parameters and laminar burning velocities of CH_4 -N₂O in the presence of various inert gases (e.g., He, Ar, N₂ and CO₂) obtained from experiments in a 0.52 L spherical vessel, at initial pressures from 0.3 to 1.8 bar were recently investigated by Razus et al. [10,11]. The authors reported that the maximum explosion pressure as well as the maximum rates of pressure rise present a linear dependence on the initial pressure. The additive efficiency on the explosion parameters decreased starting with CO₂, followed by N₂, Ar and He. The overall activation energy of methane oxidation by N₂O, which is lower than the overall activation energy when O₂ from air is used as an oxidant, can be due to N₂O dissociation.

Ethylene-N₂O flame was less studied despite the safety concerns raised from handling and storage of nuclear waste, where these mixtures can form, as well as due to their use in aerospace applications. Ethylene is a high-reactivity fuel used in the chemical industry, but previous investigations focused on explosion of ethylene-air (oxygen) mixtures [12–16]. However, ethylene–N₂O mixtures have recently been proposed as a promising propellant for hydrazine replacement [17,18] due to their advantages: similar vapor pressures, which allow a good miscibility, and high vapor pressure, which allows a self-pressurizing without an external pressure supply. Additionally, ethylene–N₂O mixtures are not carcinogenic, have a relatively low cost and a low toxicity and after their combustion, no ammonia results in comparison with hydrazine. Therefore, ethylene–N₂O mixtures represent a green propellant and thus, the studies related to these mixtures are always necessary.

Shen et al. [19] experimentally investigated the explosion dynamics of inert-diluted C_2H_4 -N₂O explosions in a standard 20-L spherical vessel at sub-atmospheric pressure (inerts: N₂ and CO₂). For inert concentrations lower than 30% they found a correspondence between the maximum explosion pressure experimentally measured and the corresponding Chapman–Jouguet (CJ) detonation pressure, meaning the activation of a DDT (Deflagration-to-Detonation) mechanism during the explosion process, also demonstrated by Bane et al. [20] for nitrogen-diluted hydrogen–nitrous oxide flames. The explosion characteristics of C_2H_4 -N₂O-N₂ mixtures measured in various cylinders (0.17 L, 1.18 L and 2.0 L), at different initial pressures, were reported by Movileanu et al. [21]. They found a linear dependence of the maximum explosion pressure (as well as of the maximum rise of pressure rise) on the initial pressure, similar to that reported for fuel-air mixtures [16]. In smaller volume explosion vessels, no DDT occurred. The DDT in long tubes, the explosion limits, and the ignition delay times of explosions in C₂H₄-N₂O and C₂H₄-O₂ mixtures were also investigated in the previous studies [22–26].

From the above literature review it can be concluded that researchers have focused their interest mostly on studying the explosion characteristics of other fuel– N_2O flames rather than that of ethylene- N_2O flames. Therefore, these latter flames must be studied in detail to cover the gap that exists regarding them in literature.

In the present study, the dynamics of closed-vessel explosion of nitrogen-diluted C_2H_4/N_2O mixtures is examined by means of the maximum (peak) explosion pressures, explosion times, maximum rate of pressure rise and severity factors. Lean and stoichiometric C_2H_4/N_2O mixtures diluted with various nitrogen amounts were examined using a 0.52 L vessel with spherical aspect and central ignition at different initial pressures. The nitrogen

was chosen as diluent because it is frequently used as an inert gas in the case of explosion inhibition. The data and conclusions from the present research could contribute to a better understanding of explosions occurring in N_2O atmosphere, providing new insights of these processes.

2. Materials and Methods

The experimental system consists of a 0.52 L stainless steel spherical vessel, the ignition device, the data acquisition system and a vacuum line. A schematic representation of the experimental set-up is presented in Figure 1.



Figure 1. Experimental system.

The explosion vessel has several ports for the gas feed/evacuation valve, pressure transducers, ionization probes, and ignition electrodes. The explosion vessel was tested for static pressures of minimum 40 bar. The ignition, centrally located inside the vessel, was done using inductive-capacitive sparks of high voltage. A piezoelectric pressure transducer (Kistler 601A), in line with a Charge Amplifier Kistler 5001 SN is used for monitoring the pressure evolution. The signals provided by the ionization probe and pressure transducer were acquired using a Tektronix digital oscilloscope type TDS 2014B connected to a PC, usually at 2500 signals/channel and maximum 1 GS/s sampling rate. Details regarding the experimental setup and procedure can be found in other published works [16,27,28]. Before each experiment, the experimental vessel was evacuated to a pressure down to 5×10^{-4} bar, then the explosive mixture was admitted and allowed 3 min. to become quiescent. After that, the gaseous mixture was ignited and then evacuated.

The C₂H₄–N₂O–N₂ gaseous mixtures were prepared in a metallic cylinder using the partial pressure method at a total pressure of 4 bar. Each investigated mixture was used 24 h after mixing their components. For every examined mixture, the equivalence ratio of the C₂H₄–N₂O mixture was given, together with the added nitrogen amount, as the volumetric N₂ concentration in the end mixture (C₂H₄ + N₂O + N₂).

Ethylene (99.99% from SIAD, Bergamo, Italy), N₂O and N₂ (both 99.999% from SIAD, Bergamo, Italy) were used, without any purification. Ethylene–N₂O mixtures having equivalence ratios from 0.8 to 1.0, diluted by 40–60% N₂, were studied. For concerns of laboratory operation safety, C_2H_4 –N₂O–N₂ explosions were examined at total initial pressures from 0.5 to 1.50 bar. For each initial condition of the explosive mixture, a minimum of 3 experiments were performed (using fresh C_2H_4 –N₂O–N₂ mixture each time) to minimize the operational errors. At the end, the obtained results were averaged.

3. Computing Programs and Data Evaluation

The 0-D COSILAB package [29] allowed the calculation of the adiabatic explosion pressures and adiabatic flame temperatures. This program is based on an algorithm that allows the calculation of the equilibrium composition of the products of a fuel–oxidizer gaseous mixture according to the thermodynamic criterion of chemical equilibrium: the minimum of Gibbs energy (keeping constant the temperature and pressure) or minimum of Helmholtz energy (keeping constant the temperature and volume). As combustion products we considered a total of fifty-three compounds. The runs were performed for lean and stoichiometric ethylene-N₂O mixtures, various nitrogen concentrations (40 to 60 vol.%), at ambient initial temperature and at different initial pressures (0.50–1.50 bar).

The p(t) curves were smoothed by Savitzky–Golay method in order to obtain the rates of pressure rise. Utilisation of the Savitzky–Golay method means the analysis of a number of points (e.g., 500–700 points) registered from the ignition to the time necessary to reach the maximum explosion pressure and provide a smoothed first derivative without filtering the data. This method implies the least squares quartic polynomial fitting across a moving window within the data. A 10% smoothing level was used for each curve, since a higher value of smoothing level (e.g., 20%) leads to a reduction of the noise and to a signal distortion.

4. Results

An example of pressure-time record for stoichiometric C_2H_4 - N_2O - N_2 mixture explosion in spherical vessel with central ignition at 1 bar initial pressure and ambient initial temperature is presented in Figure 2 and compared with that obtained for stoichiometric C_2H_4 -air explosion registered under the same initial conditions [30]. The comparison can be performed since the examined mixtures have close flame temperatures.



Figure 2. Comparison of pressure-time records for stoichiometric C_2H_4 - N_2O - N_2 (60 vol.% N_2) and stoichiometric C_2H_4 -air [30] explosions in a spherical vessel having central ignition at $p_0 = 1$ bar and $T_0 = 298$ K.

It can be observed that for equivalent initial conditions the use of N_2O for replacing O_2 as oxidizer entails the increase of the maximum explosion pressure and the decrease of the explosion time. This shows us that the fuel– N_2O mixtures are more reactive when compared with the mixtures with air with the same flame temperature. This behaviour is due to the additional heat amount released from the exothermal decomposition of N_2O when N_2O is used as oxidizer instead of air (O_2).

For all pressure–time trajectories, the pressure first increases progressively, and then decreases once the maximum values are reached, this fact indicating that a complete combustion has taken place.

The pressure evolutions of C_2H_4 -N₂O-N₂ explosions at initial pressure of 1 bar and various amounts of nitrogen are presented in Figure 3 as examples. The comparison presented in this figure shows that, for the same initial pressure, temperature and fuel:oxidizer ratio, the explosion pressure decreases when the inert concentration increases. It can

be seen that, starting with 40 vol.% dilution, the pressure inside the explosion vessel rises up smoothly after mixture ignition. This behaviour has been widely reported by other researchers [16,31,32].



Figure 3. Pressure trajectories of stoichiometric $C_2H_4/N_2O/N_2$ mixtures at $p_0 = 1$ bar.

The initial pressure is one of the parameters that influence the maximum (peak) explosion pressure. An example of maximum (peak) explosion pressures' variation against initial pressures for stoichiometric C_2H_4 - N_2O - N_2 mixtures is presented in Figure 4 for various N_2 dilution ratios and ambient initial temperature. Such variations were also observed for lean C_2H_4 - N_2O - N_2 mixtures. As expected, the maximum explosion pressure during the explosion of C_2H_4 - N_2O - N_2 mixtures increases as the initial pressure increases.



Figure 4. Maximum explosion pressures of stoichiometric C₂H₄-N₂O-N₂ at various initial pressures.

Due to the lack of experimental data reported in literature for explosions of C₂H₄-N₂O-N₂ mixtures in spherical vessels at initial pressures $p_0 \ge 1$ bar, we can only compare our data with those reported at sub-atmospheric pressures. Our data registered at $p_0 = 0.5$ bar are: $p_{max} = 6.50$ bar for stoichiometric C₂H₄-N₂O mixture diluted with 40 vol.% N₂ and $p_{max} = 5.70$ bar for stoichiometric C₂H₄-N₂O mixture diluted with 50 vol.% N₂. These results are higher than those reported by Shen et al. [19] for mixtures with the same composition and initial pressure obtained from experiments in a 20 L spherical vessel ($p_{max} = 5.70$ bar for stoichiometric C₂H₄-N₂O mixture diluted with 40 vol.% N₂ and $p_{max} = 5.00$ bar for stoichiometric C₂H₄-N₂O mixture diluted with 40 vol.% N₂ and $p_{max} = 5.00$ bar for the stoichiometric C₂H₄-N₂O mixture diluted with 50 vol.% N₂ and $p_{max} = 5.00$ bar for stoichiometric C₂H₄-N₂O mixture diluted with 50 vol.% N₂ and $p_{max} = 5.00$ bar for the stoichiometric C₂H₄-N₂O mixture diluted with 50 vol.% N₂ and $p_{max} = 5.00$ bar for stoichiometric C₂H₄-N₂O mixture diluted with 50 vol.% N₂ and $p_{max} = 5.00$ bar for stoichiometric C₂H₄-N₂O mixture diluted with 50 vol.% N₂.

Linear correlations of maximum explosion pressures with initial pressures of the mixture were found for all examined systems. The correlation could be described using the following equation:

$$p_{max} = a + b \cdot p_0 \tag{1}$$

The coefficients *a* and *b* from Equation (1) are necessary to find the unknown values of the explosion pressures at a certain value of the initial pressure in the studied pressure range without experimental measurements, as long as the combustion is propagating as a deflagration. They depend on a series of parameters such as: initial temperature, nature of the mixture, vessel shape, and aspect ratio. The coefficients of linear regressions for stoichiometric and lean C_2H_4 - N_2O - N_2 mixtures are presented in Table 1.

φ	[N ₂] (vol.%)	-a (bar)	b	<i>r</i> _n
	60	0.198 ± 0.103	10.70 ± 0.09	0.999
1.0	50	0.252 ± 0.055	12.03 ± 0.05	0.999
	40	0.298 ± 0.040	13.50 ± 0.04	0.999
	60	0.332 ± 0.065	10.11 ± 0.06	0.999
0.8	50	0.334 ± 0.125	11.52 ± 0.12	0.999
	40	0.342 ± 0.066	12.98 ± 0.07	0.999

Table 1. Slope and intercept of p_{max} vs. p_0 linear regressions.

Such linear correlations between explosion pressures and initial pressures were observed not only for fuel–air mixtures [16], but also when other fuel– N_2O inert mixtures were examined [10].

Besides the initial pressure, the shape and size of the explosion vessel influence the explosion pressure. Thus, in cylindrical vessels, the explosion pressures are smaller in comparison with those registered in spherical vessels due to higher heat losses that occur in these cylindrical enclosures. On the other hand, the higher vessel size is, the smaller the explosion pressure is. The influence of the size and aspect of the explosion vessels on this parameter can be observed from Table 2, where data referring to stoichiometric C_2H_4 -N₂O-N₂ diluted with 60 vol.% N₂ measured in a cylinder with L/D = 1.0 and in a cylinder with L/D = 1.5 measured at initial pressures between 0.50 and 1.50 bar collected from [21] are given along with the present data. All data from Table 2 refer to experiments with central ignition.

Table 2. Influence of vessel shape and size on the maximum explosion pressures of C_2H_4 -N₂O mixtures diluted with 60% N₂.

Vessel Volume (L)		p_0 (bar)	p_{max} (bar)	Reference
		0.50	5.22	
		0.75	7.72	
Spherical	0.52	1.00	10.54	Present data
		1.25	13.18	
		1.50	15.87	
		0.50	3.94	
		0.75	4.51	
Cylindrical L/D = 1.0	0.17	1.00	6.36	[21]
2		1.25	8.10	
		1.50	-	
		0.50	-	
		0.75	5.00	
Cylindrical L/D = 1.5	1.18	1.00	6.84	[21]
-		1.25	8.89	
		1.50	10.75	

The presence of an inert diluent affects the maximum explosion pressures as can be seen in Figure 5, where data referring to both studied mixtures (lean and stoichiometric) at ambient initial conditions are given. As expected, the higher the nitrogen amount is, the smaller the explosion pressure is. Adding an inert (such as nitrogen) to a gaseous flammable



mixture leads to an alteration of both thermodynamics and kinetics of the combustion process, so that a higher inert concentration leads to a small explosion pressure.

Figure 5. Maximum explosion pressure as a function of inert concentrations at ambient initial temperature and pressure.

The kinetic effect due to N_2 addition on C_2H_4 - N_2O mixtures can be assigned mainly to N_2 participation in the following reaction:

$$O + N_2 (+M) \rightarrow N_2 O (+M) \tag{R1}$$

The study undertaken by Shen et al. [19] pointed out that, at high initial pressures, nitrogen acts as both as a reactant and a third body, and thus reaction (R1) becomes important. Therefore, although the N_2O undergoes an energetic decomposition through the reaction (R2) written below, nitrogen can effectively inhibit N_2O decomposition, as described in [19].

$$N_2O(+M) \to N_2 + O(+M)$$
 (R2)

Furthermore, the nitrogen addition can lead to a decrease in the branching ratio of the following reaction (R3) over reaction (R1), by its third-body collisional effect [19]:

$$H + O_2 \rightarrow O + OH$$
 (R3)

Besides the kinetic effect, nitrogen addition contributes to the reduction of the flame temperature and flame speed, acting as a heat sink.

For all studied mixtures, a linear dependency of explosion pressure on inert concentration was observed. This dependency can be described using a correlation proposed by Oancea et al. [33,34] based on heat balance of the isochoric combustion of a fuel–air mixture in non-adiabatic conditions:

$$p_{max} = p_0 \left(\xi + \frac{r_l}{\nu_l} \cdot \frac{\Delta_c U'}{\overline{C_{e,V}} \cdot T_0} \right) - q_{tr} \cdot \frac{\gamma_e - 1}{V_0}$$
(2)

where p_{max} represents the maximum explosion pressure attained at pressure p_0 ; $\xi = n_e/n_0$ is the ratio between the final (n_e) and initial (n_0) mole numbers; $r_l = n_l/n_0$ represents the ratio between the number of moles corresponding to the limiting component of the mixture and the total initial number of moles; v_l represents the stoichiometric coefficient of the limiting component in the mixture; $\Delta_c U'$ represents the heat of combustion (at temperature T_0 and constant volume) corrected by taking into account the accompanying secondary reactions; $\overline{C_{e,V}}$ represents the molar heat capacity of the end gaseous mixture, averaged for the end components and for the temperature range T_0 to $T_{e,V}$; q_{tr} represents the amount of heat transferred by the gas to the vessel before the end of combustion; and γ_e represents the adiabatic coefficient of the burned gas, at the end of combustion.

For the isochoric combustion of a gaseous fuel-oxidizer mixture, Equation (2) holds as long as it is assumed that the studied gas behaves like an ideal gas and that p_{max} is approximately equal to the pressure at the combustion end. However, in the real cases, the gaseous fuels are made up from polyatomic molecules, having many degrees of freedom, and their heat capacities are high and depend on temperature, which leads to explosion pressures which differ from those obtained with this equation. Keeping constant the initial temperature, the maximum explosion pressures of N₂-diluted C₂H₄-N₂O mixtures depend on initial pressures (influencing the molar heat capacity of the end gaseous mixture and the adiabatic coefficient of the burned gas, at the end of combustion) and on the amount of heat transferred by the gas to the vessel before the end of combustion. Therefore, we can observe that N₂ addition to C₂H₄-N₂O mixtures influences both the slope and intercepts of p_{max} versus p_0 plots.

Over a well-defined initial pressure domain, we can assume that ξ , $\Delta_c U'$ and $\overline{C_{e,V}}$ do not depend on p_0 (or that their variations compensate each other) and therefore, the amount of heat transferred from the burned gas to the explosion vessel before the combustion ends, can be obtained using the intercepts of the linear correlations p_{max} vs. p_0 , whose values are presented in Table 1. Representative results regarding the amount of heat transferred by the stoichiometric and lean ethylene-N₂O-N₂ flames to the vessel's walls are presented in Table 3. In the present case, q_{tr} was calculated following [16], as:

$$q_{tr} = -\frac{a \cdot V_0}{\gamma_e - 1} \tag{3}$$

N2 (vol.%)	γe		q_{tr}	· (J)	F		
112 (1011/0) =	$\varphi = 1.0$	$\varphi = 0.8$	$\varphi = 1.0$	$\varphi = 0.8$	$\varphi = 1.0$	$\varphi = 0.8$	
40	1.3097	1.3139	0.333	0.550	0.020	0.036	
50	1.3078	1.3119	0.426	0.557	0.023	0.032	
60	1.3080	1.3121	0.503	0.570	0.024	0.029	

Table 3. Transferred heat amount, q_{tr} , and fraction of heat lost, F, by stoichiometric and lean ethylene-N₂O-N₂ flames to vessel's walls.

From Table 3 it is seen that an increase of the nitrogen concentration leads to larger amounts of heat being lost to the vessel's wall due to the longer explosion times and lower propagation speeds for both lean and stoichiometric ethylene-N₂O-N₂ mixtures.

Another important parameter that describes the heat transferred during explosions in closed vessels is the fraction (F) of the heat transferred (lost) from the total released heat. This property depends, on one hand, on the corrected heat of combustion and the average heat capacity of burned gas (factors influenced by the composition of fuel and oxidizer) and, on the other hand, on the initial pressure of the studied mixture. In this study, the fractions F of transferred heat were calculated using the following equation [35], derived also from Equation (2):

$$F = \frac{-a}{p_0(b-1)}$$
(4)

Their values calculated at $p_0 = 1$ bar are also presented in Table 3. At constant inert composition, lower *F* values were obtained for the stoichiometric C₂H₄-N₂O flames compared to the lean flames. This is due to the fact that the stoichiometric mixtures have shorter explosion times and higher burning velocities when compared to the lean mixtures.

When a certain amount of inert (molar fraction: x_i) is added to a fuel-air mixture, it is expected that the heat transferred from the burned gas to the vessel, before the combustion

ends, to be a function of mixture composition. Therefore, the term q_{tr} from Equation (2) becomes $q_{tr}^* = f(r_l, x_i)$ and Equation (2) is rewritten as:

$$p_{max} = \left[p_0 \left(\xi + \frac{r_l}{\nu_l} \cdot \frac{\Delta_c U'}{\overline{C_{e,V}} \cdot T_0} \right) - q_{tr}^* \cdot \frac{\gamma_e}{V_0} \right] - \left(p_0 \frac{r_l}{\nu_l} \cdot \frac{\Delta_c U'}{\overline{C_{e,V}} \cdot T_0} \right) \cdot x_i = m - n \cdot x_i$$
(5)

When the composition of fuel-oxidizer mixture as well as the initial pressure p_0 are constant, we can assume that the coefficients *m* and *n* (characterized by ξ , r_l and v_l) are constant. This is true only for a restricted domain of inert gas concentrations. Only when these conditions are fulfilled, the explosion pressure present a linearly dependence on the molar fraction of added inert gas. In this case, a linear dependence of explosion pressure on the molar fraction of added inert gas is observed, as shown by the data from Figure 5.

Even if explosions occur in a spherical vessel, where the explosion is considered to propagate as close as possible to the ideal case, the differences between experimental and ideal adiabatic explosion pressures are significant, as it can be seen from Figure 5. This behaviour shows once more that in the real case, the heat transferred (by convection, conduction or radiation) from the flame front to the vessel walls influences the explosion's propagation. In the present research, the flame was monitored by means of an ionization probe. The ionization probe signal, reaching its peak value at the same time with the peak of the pressure rise rate, can be seen in Figure 6. The observed differences between the experimental and adiabatic values of the explosion pressures can be attributed not only to the heat losses during experiments, but also to the aspect and volume of the explosion vessel, the position of the ignition source or the appearance of turbulences in the gaseous mixture before ignition, which may lead to a decrease in explosion pressure. In the case of an adiabatic process when there are no heat losses, the explosion pressures are influenced only by the initial pressure and temperature and by the composition and the nature of the studied mixture. The differences between the experimental and calculated (adiabatic) explosion pressure are useful to obtain with approximation the amount of lost energy in the course of the combustion process. This was already noted by Kunz in his study on combustion characteristics of H₂- and hydrocarbon-air mixtures in closed vessels [36]. Kunz concluded that the larger the differences between the calculated and experimental explosion pressures are, the higher the thermal losses are that occur during the explosion.



Figure 6. Pressure evolution for deflagration of stoichiometric C_2H_4 - N_2O - N_2 with 60 vol.% N_2 , at ambient initial conditions.

The adiabatic explosion pressures have the same behaviour as the experimental explosion pressures does. At a constant amount of nitrogen, higher values of the adiabatic explosion pressures were observed for stoichiometric C_2H_4 - N_2O mixture compared to

lean C₂H₄-N₂O mixture. Keeping the equivalence ratio constant, the adiabatic explosion pressures decreased with an increase in initial pressure.

Set as the zero point (0 s) on an X-axis the moment of ignition. Considering this, the explosion time, θ_{max} , which represents another important combustion parameter, is defined as the explosion duration between the ignition and the moment when the maximum explosion pressure is reached. Adding an inert to a gaseous fuel–oxidizer mixture influences not only the maximum explosion pressure, but also the explosion times. Obviously, with increasing N₂ dilution, the explosion duration θ_{max} increases, as it can be observed from Table 4.

Table 4. Time to reach the maximum explosion pressures, θ_{max} (ms), for ethylene-N₂O-N₂ mixtures in spherical vessel.

φ		1.0			0.8		
	[N ₂] (vol.%)	40	50	60	40	50	60
p_0 (bar)							
1.5		-	17.1	33.3	-	21.7	43.4
1.25		10.6	17.6	32.8	13.2	22.2	43.6
1		10.7	18	33.2	13.7	22.5	44.6
0.75		11.1	18.2	34.2	13.6	22.8	46
0.5		11.4	18.4	34.9	13.9	23.3	51.4

It was found that for stoichiometric ethylene-air mixture at $p_0 = 1$ bar, the maximum time to reach p_{max} is $\theta_{max} = 14.6$ ms, higher that for an ethylene-N₂O-N₂ mixture with the same flame temperature ($\theta_{max} = 10.7$ ms). Lower values of characteristic parameters θ_{max} were obtained for a stoichiometric C₂H₄-N₂O-N₂ mixture compared to the lean mixture. This behaviour is in accordance with their burning velocities.

The maximum rate of pressure rise represents a safety parameter important for assessing the hazard of a process and, together with the explosion pressure, is used for design of enclosures able to withstand explosions, or of vents used as relief devices for these vessels to avoid the damages caused by explosions occurring in the gaseous phase [37–39]. For explosions of nitrogen-diluted ethylene-N₂O mixtures linear dependences of the form:

$$(dp/dt)_{max} = \alpha + \beta \cdot p_0 \tag{6}$$

were obtained from the graphic representation of the maximum rates of pressure rise versus initial pressures, as can be observed in Figure 7a,b. The coefficients α and β depend, on one hand, on the equivalence ratio of studied mixture, and, on the other hand, on the nature and of amount of inert added to the gaseous mixture.

Similar dependences as those given in Figure 7 were reported earlier for fuel–air mixtures such as propane–air [40], LPG–air [41] or propylene–air [42] and for fuel–air–diluent mixtures (e.g., H₂–air–steam [43,44], CH₄–air–N₂, CH₄–air–CO₂ [45], natural gas–air–CO₂ [46]) obtained at sub-atmospheric initial pressures or at initial pressures above 1 bar (with the obvious limitation to deflagrative combustions).

Such diagrams as those depicted in Figure 7 are useful to calculate the maximum rates of pressure rises at any initial pressures different from the ambient one, but within the studied pressure range. This is valid only as long as the explosion propagates as deflagration.

At $p_0 = 0.5$ bar and stoichiometric equivalence ratio of $C_2H_4-N_2O-N_2$ mixtures, Shen et al. [19] reported $(dp/dt)_{max} = 20$ bar/s for a nitrogen amount of 40 vol.% and $(dp/dt)_{max} = 10$ bar/s for a nitrogen amount of 50 vol.%. As a comparison, the present data are: $(dp/dt)_{max} = 21.0$ bar/s for a nitrogen amount of 40 vol.% and $(dp/dt)_{max} = 14.8$ bar/s for a nitrogen amount of 50 vol.%.



Figure 7. Maximum rates of pressure rise for stoichiometric (**a**) and lean (**b**) C₂H₄-N₂O-N₂ mixtures with various amount of N₂.

As shown by the above data, the presence of an inert influences the rates of pressure rise. From Figure 7 it is observed that, for constant equivalence ratio, the higher the amount of inert added is, the lower the pressure rise rates are, for both lean and stoichiometric ethylene-N₂O flames. When the amount of N₂ is kept constant, it is noticed that the pressure rise rates of lean ethylene-N₂O mixtures are lower compared to the pressure rise rates of stoichiometric mixture. This behaviour was already reported for CH_4 -N₂O-N₂ flames [10].

The severity factor is an efficient scaling parameter able to predict the failure effect of enclosures where an explosion occurs. In this study, the severity factors (K_G) of C_2H_4 - N_2O - N_2 flames were determined by means of the rates of pressure rise obtained from measurements in the spherical vessel with central ignition and are given in Figure 8 versus the initial pressure. The greater the amount of inert is, the lower the severity factors are, a fact observed for both stoichiometric and lean C_2H_4 - N_2O mixtures when the equivalence ratio is kept constant. As expected, when the inert concentration is kept constant, the higher values of the severity factors are observed for the stoichiometric C_2H_4 - N_2O mixture compared to lean C_2H_4 - N_2O mixture.



Figure 8. Severity factors for N₂ diluted lean and stoichiometric C₂H₄-N₂O-N₂ mixtures.

As already reported for CH₄-air mixture [47], and as seen from Figure 8, the severity factors are strongly affected by the initial pressure. As expected, the severity factors present

the same linear dependence on the initial pressure as previously observed for the maximum explosion pressures and the rates of pressure rise.

Therefore, the severity of an explosion in fuel–oxidizer mixtures can be reduced by using inert additives which have the role of taking over some of the heat released from the combustion reaction and thereby lowering the temperature in the flame front. The decrease of the flame temperature has as a major effect the decrease of the explosion pressure, accompanied by the decrease of the reaction rate resulting in the decrease of maximum rates of pressure rise and thus of the severity factors.

The maximum explosion pressures and maximum rates of pressure rise of stoichiometric C_2H_4 - N_2O mixtures diluted with various amounts of N_2 or CO_2 were studied at various initial pressures using a standard-volume vessel [19]. The authors of this paper concluded that, in the case of the aerospace applications where the dilution degree is small, a N_2 dilution contributes better to safety and power efficiency when compared to CO_2 . On the other hand, in the case of nuclear or other hazardous waste which contains N_2O , the nitrogen presents almost the same dilution effect as CO_2 due to its presence in large quantities. Therefore, for a better use of these mixtures that present a high explosive risk, specialized scientific studies are always necessary.

5. Conclusions

The present paper presents the characteristic parameters of confined explosions $(p_{max}, \theta_{max} \text{ and } (dp/dt)_{max})$ in a spherical vessel with central ignition for lean and stoichiometric C₂H₄-N₂O mixtures diluted with various amounts of nitrogen between 40–60 vol.%. The results are examined in correlation with the composition and initial pressure of these flammable mixtures.

The explosion pressures and rates of pressure rise are higher and the times to achieve peak explosion pressures are shorter for nitrogen-diluted C_2H_4 -N₂O mixtures in comparison to C_2H_4 -air mixtures with the same flame temperature. The exothermal dissociation of nitrous oxide in C_2H_4 -N₂O-N₂ flames is the reason of that behaviour, due to the supplementary heat amount released in fuel–N₂O flames compared to fuel–air flames.

The computed adiabatic explosion pressures are higher in comparison with the measured peak explosion pressures for all flammable mixtures due to the heat losses which take place during the late period of flame propagation.

For all studied flammable mixtures, it was observed that the peak explosion pressures depend linearly on the initial pressures of these mixtures and that the slope as well as the intercept of such dependencies are influenced by the composition of the flammable mixtures.

Linear correlations of the maximum rates of pressure rise and severity factors against the initial pressures were also obtained for all studied C_2H_4 - N_2O - N_2 mixtures.

At constant equivalence ratio, the severity factors decrease when the nitrogen amount is increased. At a constant nitrogen amount, the severity factors of stoichiometric C_2H_4 - N_2O-N_2 mixture are higher compared to those of lean $C_2H_4-N_2O-N_2$ mixture.

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