

Article

The Research on Complex Lithology Identification Based on Well Logs: A Case Study of Lower 1st Member of the Shahejie Formation in Raoyang Sag

Zhaojing Song ^{1,2}, Dianshi Xiao ^{1,2,*}, Yongbo Wei ³, Rixin Zhao ^{1,2}, Xiaocheng Wang ^{1,2} and Jiafan Tang ^{1,2}¹ Shandong Provincial Key Laboratory of Deep Oil and Gas, Qingdao 266580, China² School of Geosciences, China University of Petroleum (East China), Qingdao 266580, China³ Exploration and Development Research Institute of Daqing Oilfield Co., Ltd., Daqing 163712, China

* Correspondence: xiaods@upc.edu.cn

Abstract: Lithology identification is the basis for sweet spot evaluation, prediction, and precise exploratory deployment and has important guiding significance for areas with low exploration degrees. The lithology of the shale strata, which are composed of fine-grained sediments, is complex and varies regularly in the vertical direction. Identifying complex lithology is a typical nonlinear classification problem, and intelligent algorithms can effectively solve this problem, but different algorithms have advantages and disadvantages. Compared were the three typical algorithms of Fisher discriminant analysis, BP neural network, and classification and regression decision tree (C&RT) on the identification of seven lithologies of shale strata in the lower 1st member of the Shahejie Formation (Es_1^L) of Raoyang sag. Fisher discriminant analysis method is linear discriminant, the recognition effect is poor, the accuracy is 52.4%; the accuracy of the BP neural network to identify lithology is 82.3%, but it belongs to the black box and can not be visualized; C&RT can accurately identify the complex lithology of Es_1^L , the accuracy of this method is 85.7%, and it can effectively identify the interlayer and thin interlayer in shale strata.

Keywords: lithology identification; intelligent algorithms; well logs; shale strata; Raoyang sag



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1. Introduction

The majority of continental shale formations were generated by lake basin sedimentation and are characterized by a variety of rock types and frequent lithological shifts in the longitudinal direction. Lithology contains much geological information, which can reflect the geological characteristics of the reservoir [1]. The lithology of rocks can be accurately determined by analyzing the characteristics of rock samples. However, rock sample analysis is expensive and time-consuming. As a result, this method cannot be widely used in oil and gas exploration [2]. Well logs are an effective means of reservoir evaluation and an important way of lithology identification. It can quantitatively characterize depositional processes and reflect stratigraphic information at different depths based on precise vertical resolution [3].

In the traditional interpretation of well logs data, lithology definition is usually performed by experts with relevant professional knowledge, which greatly limits the development of the industry. Well logs are composed of a large amount of formation information, and data statistics can effectively sort out this information. Combining well logs and data statistics is an effective method to solve the problem. Density, neutron, and sonic logs are used to describe porosity. The lithology of conventional reservoirs can be identified based on using porosity logs to build cross plots separately [4]. With the change in exploration target, the lithology of the target interval becomes more complex, and the conventional mathematical statistics method can no longer meet the research needs. Principal component analysis, linear discriminant analysis, and Bayesian classifier were used to process

multi-dimensional well logs data and identify lithology [5–7]. In unconventional oil and gas exploration, especially in the continental shale formations dominated by fine-grained sediments, the boundaries for dividing lithology are not obvious [8] and the well logs responses are similar. In addition, fluid type and saturation, salinity, fractures, and diagenesis can also produce log responses similar to those caused by lithology [9,10]. All the above are unfavorable factors for lithology identification.

Intelligent algorithms are more prominent in solving complex nonlinear recognition problems, and many scholars have also carried out related research. These algorithms include support vector machines (SVMs) [11–13], random forests (RFs) [7,14], boosted trees [15,16], decision trees (DTs) [17], K-means clustering algorithms [18], artificial neural networks (ANNs) [19,20], and fuzzy theory [21]. Some scholars have combined multiple algorithms to solve the identification problem of complex lithology [2,3,22,23]. Ren et al. (2022) processed logging data, including cluster analysis based on the K-means clustering algorithm and fuzzy processing based on triangular membership function, and then used the decision tree algorithm to build a model for lithology identification. Some scholars also believe that intelligent algorithms are black boxes that cannot be visualized to some extent [24]. Dong et al. [10,25] improved the linear discriminant analysis to maintain the characteristics of visualization and solve the complex lithology identification problem.

Fisher discriminant analysis (FDA) can identify the lithology of carbonate reservoirs with nonlinear characteristics [10]. The back propagation (BP) neural network has self-learning ability, particularly promotion, and generalization [26]. It can also be used for lithology identification. Lithology identification is a classification problem that can be efficiently solved by decision tree algorithms [23]. Most of the previous applications of the above methods are based on conventional reservoirs, and there is a lack of research on terrestrial shale formations where shale oil and gas resources are developed. The main rock type of the continental shale strata of fine-grained sedimentary rocks (FGSRs). Fine-grained sedimentary rocks have small particle size and complex mineral composition characteristics and are widely developed in the lower 1st member of the Shahejie Formation (Es_1^L) [26,27]. This study identifies the lithology of FGSR based on FDA, BP neural network, and decision tree algorithm. By comparing the identification accuracy of the three methods, the lithology identification method suitable for the Es_1^L is preferred. It is expected that accurately identifying the lithology of the Es_1^L can provide some guidance for oil and gas exploration and development. In addition, this research approach can also be applied to the lithology identification of other strata.

2. Geological Setting and Sample

The Raoyang Sag is located in the Bohai Bay Basin in eastern China [28]. The Es_1^L is the target interval of the study. It was formed during the sedimentary period of the extension of the lake basin. Shallow water deltas and deep lakes and semi-deep lakes are the main sedimentary microfacies in the Es_1^L [26,27] (Figure 1a). The shallow water delta is located in the lower part of the Es_1^L , and coarse-grained clastic rocks dominate its lithology. The lithology of deep and semi-deep lake microfacies includes dark gray mudstone, oil shale, biological limestone, argillaceous limestone, dolomite, calcareous mudstone, and thin sandstone [27] (Figure 1b). These lithologies frequently interstratify, making lithology identification much more challenging and restricting the development of shale oil and gas exploration. The lithology of 147 core samples from 13 wells was determined by core observation, thin section identification, and X-ray diffraction analysis. According to the needs of the production site, the lithology of the Es_1^L is divided into sandstone (37), sandy mudstone (6), mudstone (24), Calcareous mudstone (12), dolomite (17), limestone (3), and shale (48) (Figure 2). In addition, the logging curves used in this study include acoustic velocity wave (AC), spontaneous potential (SP), natural gamma logging (GR), caliper logging (CAL), resistivity logging, compensated neutron porosity logging (CNL), and density logging (DEN).

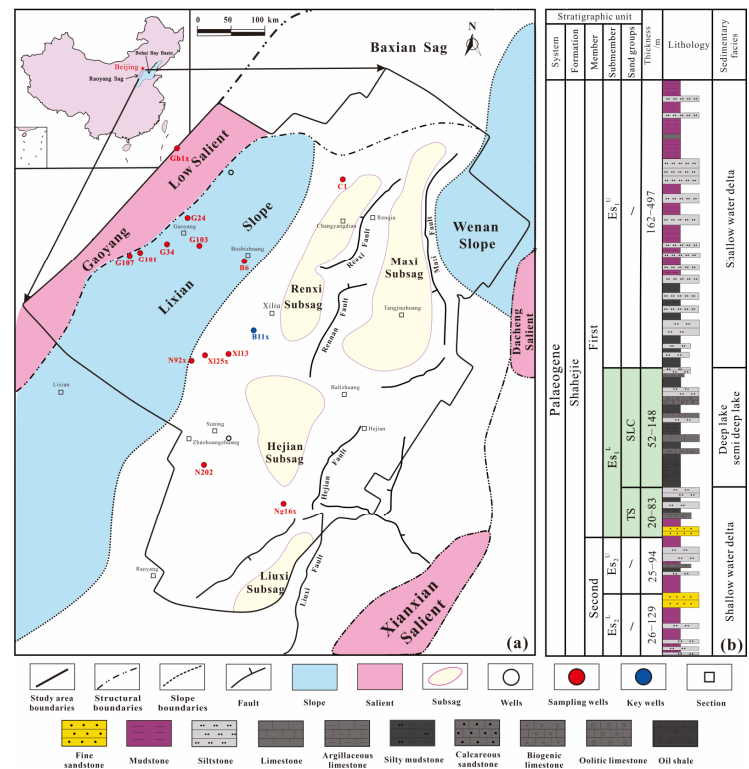


Figure 1. (a) Map showing the structural characteristic within and surround the Raoyang sag and distribution of sampling wells. (b) Stratigraphic column of the Shahejie Formation (modified after Wei et al., 2021 [27]).

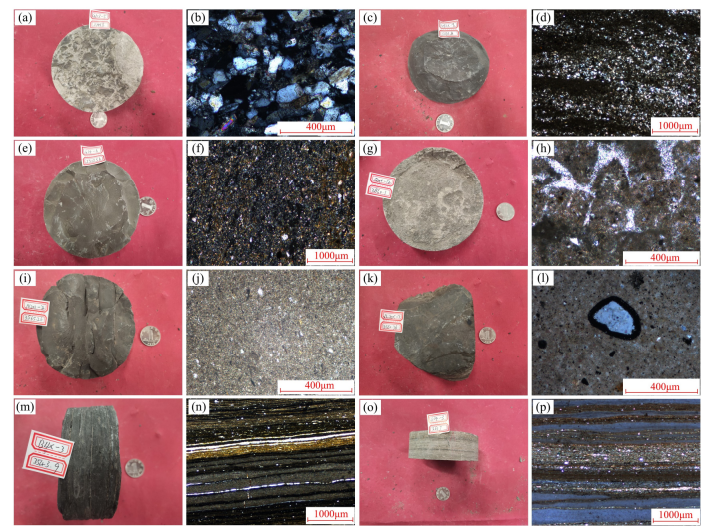


Figure 2. (a,b): sandstone, well G103, 2479.80 m, the mineral composition is dominated by quartz and feldspar; (c,d): sandy mudstone, well N92x, 3276.00 m, silty quartz and feldspar particles are unevenly distributed; (e,f): mudstone, well G34, 2517.56 m, clay structure, the main component is fine scaly clay minerals; (g,h): calcareous mudstone, well Q46, 2860.10 m, the main component is dolomite, a small amount of terrestrial quartz and feldspar, bright crystal dolomite filling between sand debris; (i,j): dolomite, well N202, 3565.26 m, the main component is dolomite, and a small amount of terrigenous fine-grained quartz and feldspar are unevenly distributed; (k,l): limestone, well XL25x, 3550.36 m; (m,n): shale, well B11x, 3543.90 m, development of page bedding structure; (o,p): shale, well G24, 2617.00 m, fine scaly clay minerals, silty quartz, feldspar and iron bands are interbedded with unequal thickness.

3. Method

3.1. Preprocessing

The quality of the training samples affects the accuracy of the prediction results [29]. The depth does not match the actual sampling point depth and the different correlations, splicing, and difference in the order of magnitude of the logging curves are all unfavorable factors that affect the prediction results. Core sample depth homing and logging curve splicing are preprocessing methods used in logging evaluation. Input curves have different units and degrees of variation, leading to large differences in predictions. To eliminate the influence of the dimension and the various size and magnitudes of the variable itself and to make the curves comparable, the input curves need to be standardized [23,30]. The log curve with approximate linear characteristics is processed by linear normalization, and the processing formula is expressed as:

$$X_i = \frac{X_i^* - X_{min}^*}{X_{max}^* - X_{min}^*} \tag{1}$$

Logarithmic normalization is used for logging curves of nonlinear characteristics such as resistivity, and the formula is expressed as:

$$X_i = \frac{\lg X_i^* - \lg X_{min}^*}{\lg X_{max}^* - \lg X_{min}^*} \tag{2}$$

where X_i is the normalized logging curve value; X_i^* is the original logging value; X_{max}^* and X_{min}^* are the maximum and minimum values of the logging curve in the study interval.

Different types of logs have different responses to lithology, and selecting a log with a good response has a better effect on lithology identification [10]. The degree of correlation between categorical variables (lithology) and interval variables (logging curve) can be expressed by correlation ratios (E^2). The formula for calculating E^2 is expressed as:

$$E^2 = \frac{\sum (Y - \bar{Y})^2 - \sum (Y - \bar{Y}_k)^2}{\sum (Y - \bar{Y})^2} \tag{3}$$

where Y represents the value of the interval variable, \bar{Y} represents the mean of the interval variable, Y_k represents the mean of the k -th category-spaced variable.

Usually, when E^2 is less than 0.06, the two variables are weakly correlated, and when E^2 is greater than 0.16, they are strongly correlated. From Figure 3, it can be found that the E^2 of the different logging curves of the Es_1^L is quite different, and AC, SP, and CNL are strongly correlated with lithology. The E^2 of the 2.5 m bottom gradient (R25) is 0.15, close to a strong correlation. The resistivity has reference significance for the identification of lithology. Therefore, AC, SP, CNL, and R25 are used as input parameters for lithology identification.

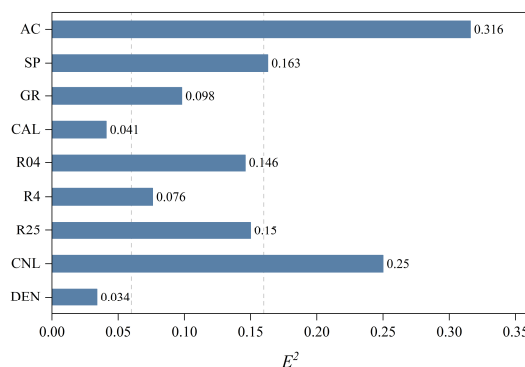


Figure 3. Correlation characteristics of conventional logging curves.

3.2. The FDA Principle

FDA, also known as linear discriminant analysis, is a classic classification discriminant method. It transforms data from multi-dimensional to low-dimensional through specific mathematical methods [25,31,32]. The core idea of the FDA is to minimize the distance between the same group and maximize the distance between different groups (Figure 4). Converting the idea into a mathematical formula can be expressed as:

$$J(w) = \frac{w^T S_b w}{w^T S_w w} \quad (4)$$

where w is the projection vector, S_b is the between-class scatter matrix, S_w is the within-class scatter matrix, and their mathematical expressions are as follows:

$$S_b = \sum_i^{p-1} \sum_{k=i+1}^p \frac{N_i}{N} \frac{N_k}{N} (m_i - m_k)(m_i - m_k)^T \quad (5)$$

$$S_w = \sum_{i=1}^p \sum_{j=1}^{n_i} \frac{1}{N} (x_j^i - m_i)(x_j^i - m_i)^T \quad (6)$$

where $x_j^{(i)}$ represents the j -th sample in the i -th category; there are P elements in the vector $x^{(i)}$; n_i is the number of samples in the i -th category and it satisfies $\sum_{i=1}^p n_i = N$; and m_i represents the centroid of the i -th sample, $m_i = \frac{1}{n_i} \sum_{j=1}^{n_i} x_j^{(i)}$.

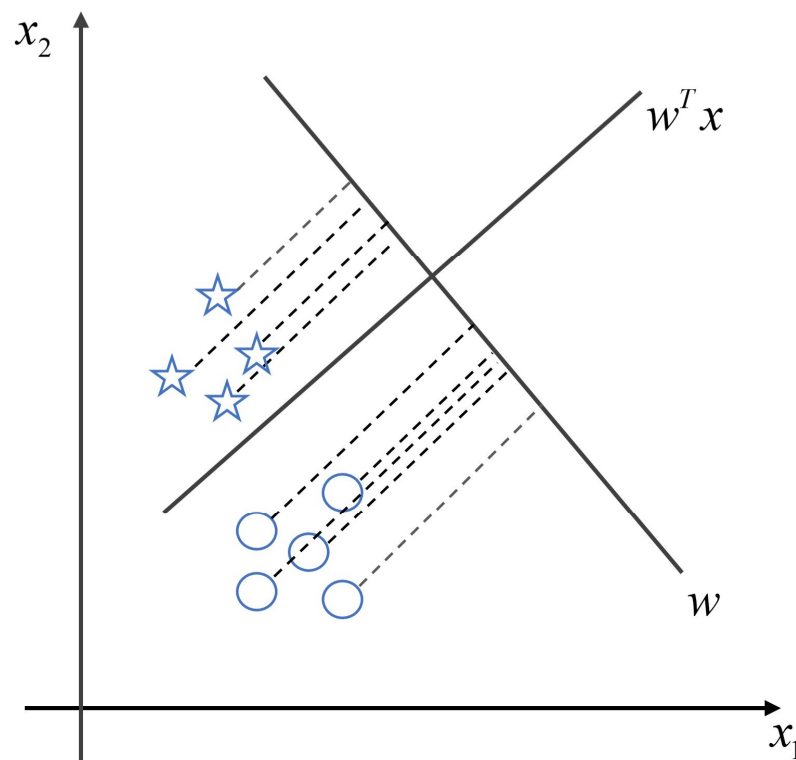


Figure 4. Diagram of the FDA.

Previous research [25] has proved that the optimal solution of m is equivalent to finding the eigenvector of $S_b u = \lambda S_w u$. The expression $J(w)$ can be obtained by bringing the eigenvector corresponding to the largest eigenvalue into the Formula (4).

There are seven lithologies to be identified in this study, and AC, SP, CNL, and R25 are used as input parameters. For each sample, $x_j^{(i)} = (AC, SP, R25, CNL)^T$, $i =$

1, 2, ..., 7; $j = 1, 2, \dots, n_{147}, p = 4$. The eigenvalues and the corresponding canonical functions are determined, and the two canonical functions with the largest eigenvalues are selected as the eigenvectors for lithology discrimination. $w_1 = (w_{11}, w_{12}, w_{13}, w_{14})^T$, and $w_2 = (w_{21}, w_{22}, w_{23}, w_{24})^T$ are the eigenvectors corresponding to the eigenvalues. Then, the projection vector is $z_j^i = (w_1^T x_i^j, w_2^T x_i^j)^T$. Here

$$z_1 = AC \times w_{11} + SP \times w_{12} + R25 \times w_{13} + CNL \times w_{14} \quad (7)$$

$$z_2 = AC \times w_{21} + SP \times w_{22} + R25 \times w_{23} + CNL \times w_{24} \quad (8)$$

So far, the discriminant functions of seven kinds of lithology are established, and the logging curve is brought into the discriminant function. The one with the largest function value is this kind of lithology.

3.3. The BP Neural Network

The BP neural network is a multi-layer feedforward neural network trained by the error backpropagation algorithm, comprising an input layer, output layer, and hidden layer [33]. It has self-learning ability, particularly promotion, generalization, and self-adaptive ability, and is one of the most widely used neural network models [26]. The basic principle of the BP neural network for predicting mineral components is to find a mapping relationship by continuously modifying the network weights and correction threshold until a satisfactory accuracy is obtained [34,35]. The most basic algorithm of the BP neural network is the steepest descent method, including the forward propagation of the signal and the backpropagation of the error.

In the multi-layer forward propagation process, the output formula of each hidden layer unit is as follows:

$$Y_j = f \left(\sum_{i=1}^n (w_{ij} \cdot x_i) + b_j \right) \quad (9)$$

where $f = \frac{1}{1+e^{-x}}$ is the activation function, w_{ij} represents the input weight, b_j represents the offset, x_i represents the output of the input layer, and Y_j represents the output result of the j -th layer.

In the multi-layer forward propagation process, the output formula of each unit of the output layer is as follows:

$$Y_k = f \left(\sum_{i=1}^n (w_{ik} \cdot x_i) + b_k \right) \quad (10)$$

where Y_k represents the output result of the output layer, w_{jk} is the weight from the j -th hidden layer neuron to the k -th output layer neuron, x_j represents the output of the hidden layer, and b_k represents the neuron offset of the hidden layer.

In error backpropagation, the output error signal of each layer of neurons is calculated from the output layer to the input layer. Through the error gradient descent method, the weights and thresholds of each layer are adjusted to minimize the mean square error (MSE). MSE can be expressed as:

$$MSE = \frac{1}{2n} \sum_i^n E_i^2 \quad (11)$$

where E_i is the error of the i -th input data, and n represents the amount of input data.

The adjustment formula of weight is as follows:

$$w_{i(j+1)} = \phi \cdot \delta_j \cdot Y_k \cdot Y_i + a \cdot \Delta w_{ij} \quad (12)$$

where $w_{i(j+1)}$ represents the weights from the i -th input layer to the $j+1$ -th hidden layer, ϕ represents the learning step, δ_j represents the error, Y_i represents the result of the input layer, and a represents the momentum factor. Δw_{ij} is the output result from the i -th input layer

to the j -th hidden layer. The momentum factor a is to prevent partial error minimization, using momentum to slide past these minima.

The adjustment formula for the threshold is as follows:

$$b_{j+1} = a \cdot b_j + \phi \cdot \delta_{j+1} \quad (13)$$

where b_{j+1} is the threshold of the $j+1$ -th hidden layer, and b_j represents the threshold of the j -th hidden layer.

AC, SP, CNL, and R25 are used as input parameters. Seven lithologies are coded separately: sandstone is 1, sandy mudstone is 2, mudstone is 3, calcareous mudstone is 4, dolomite is 5, limestone is 6, and shale is 7. A total of 128 sets of data are randomly selected as training samples, and the weights are continuously updated for training to determine the network structure. In this study, the hidden layer contains ten neurons, and the value of the momentum factor is 0.95. The process of identifying lithology based on the BP neural network is shown in Figure 5. The remaining data are used as a test sample to test the model's accuracy independently.

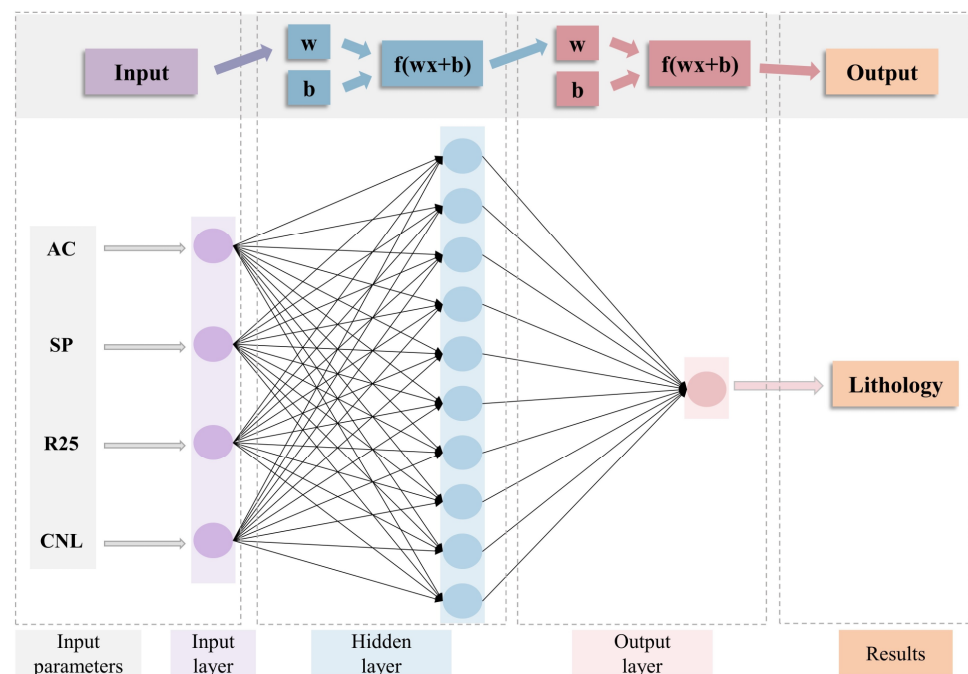


Figure 5. Schematic diagram of the principle of lithology recognition by BP neural network.

3.4. The Classification and Regression Tree (C&RT)

C&RT, as a classification model, was proposed by Breiman et al. in 1984 [36], and it is an efficient method for solving classification problems. The branch criterion is the core criterion of decision tree classification, and the change in the branch criterion produces different types of decision trees. The branching criterion of C&RT is established based on the Gini coefficient. The Gini (G) coefficient represents the probability that a randomly selected sample in the sample set is misclassified. It can be expressed as:

$$G(p) = 1 - \sum_{k=1}^k p_k^2 \quad (14)$$

where k represents the number of categories, P_k is the frequency with which the k -th class appears in the classification results.

For a given sample set, D , its Gini coefficient is expressed as:

$$G(D) = 1 - \sum_{k=1}^k \left(\frac{|C_k|}{|D|} \right)^2 \tag{15}$$

where C_k is the number of samples in D that belong to class k .

When feature A takes the value of a , D is divided into two parts, D_1 and D_2 . Under the condition of feature A , the G of D is defined as:

$$G(D, A) = \frac{|D_1|}{|D|} G(D_1) + \frac{|D_2|}{|D|} G(D_2) \tag{16}$$

Overfitting is an unavoidable problem of C&RT, and pruning is the primary solution [17,37]. Pruning includes pre-pruning and post-pruning. Pre-pruning means stopping the tree from growing before the decision tree is fully formed. Post-pruning generates an initial decision tree according to the largest scale and prunes layer by layer from bottom to top according to certain rules.

The schematic diagram of C&RT identifying lithology is shown in Figure 6. Log data and lithology data of 147 samples were used as input variables and target parameters, respectively. To prevent overfitting, stopping rule was set, where the minimum number of records in the parent branch is 2%, and the maximum risk difference is 1 and set the depth of the tree to 5. The samples were randomly divided into a training set (131) and a test set (16).

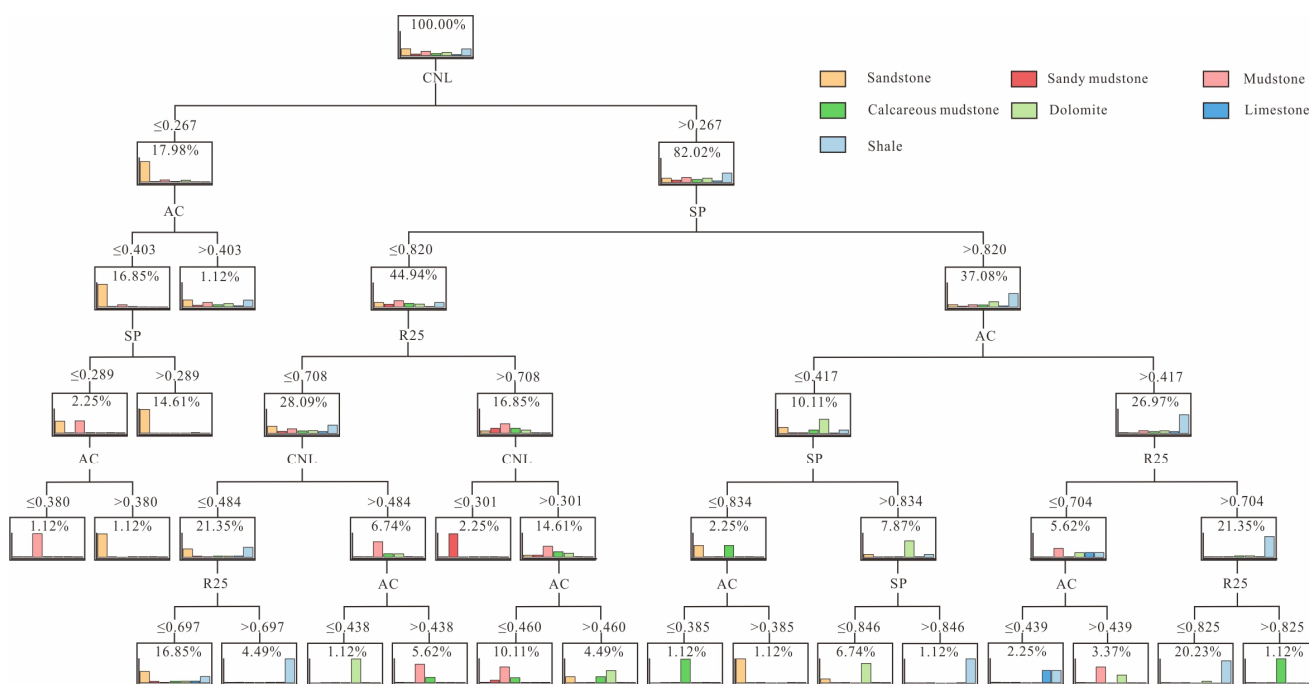


Figure 6. Schematic diagram of C&RT to identify lithology.

4. Results

The canonical function characteristics of the Es_1^L are shown in Table 1. The eigenvalues of function 1 and function 2 are high, and the cumulative contribution rate is 92.7%, which contains most of the lithological information. As a result, function 1 and function 2 are selected as the characteristic variables of lithology discrimination, and the discriminant function of lithology is constructed. The discriminant function is as follows:

$$\left\{ \begin{array}{l}
 y_{sandstone} = 198.445 \times AC + 13.132 \times SP + 149.108 \times R25 - 30.769 \times CNL - 89.227 \\
 y_{sandy,mudstone} = 203.262 \times AC + 3.529 \times SP + 157.391 \times R25 - 24.92 \times CNL - 94.781 \\
 y_{mudstone} = 211.363 \times AC + 11.009 \times SP + 155.451 \times R25 - 22.273 \times CNL - 100.783 \\
 y_{calcareou,smudstone} = 222.459 \times AC + 13.391 \times SP + 159.739 \times R25 - 24.898 \times CNL - 110.158 \\
 y_{dolomite} = 213.758 \times AC + 12.752 \times SP + 163.179 \times R25 - 25.559 \times CNL - 107.449 \\
 y_{limestone} = 223.749 \times AC + 6.023 \times SP + 151.782 \times R25 - 30.619 \times CNL - 100.398 \\
 y_{shale} = 225.139 \times AC + 12.258 \times SP + 167.792 \times R25 - 25.159 \times CNL - 114.750
 \end{array} \right. \quad (17)$$

Table 1. Canonical function eigenvalue contribution rate statistics table.

| Function | Eigenvalues | Percent Variance (%) | Cumulative Percentage (%) | Canonical Correlation |
|----------|-------------|----------------------|---------------------------|-----------------------|
| 1 | 0.731 | 74.6 | 74.6 | 0.65 |
| 2 | 0.178 | 18.1 | 92.7 | 0.388 |
| 3 | 0.054 | 5.5 | 98.2 | 0.226 |
| 4 | 0.018 | 1.8 | 100 | 0.131 |

The lithology identification results of FDA are shown in the Table 2 and Figure 7a, the identification effect of shale and sandstone is good, and the accuracy is 83.3% and 81.1%, respectively. Sandy mudstone and limestone have lower accuracy, both below 50%. The identification of other lithologies is not suitable. Calcareous mudstone and dolomite were not correctly classified. A total of 66.7% of calcareous mudstone and 70.6% of dolomite were wrongly classified as shale. The FDA’s overall accuracy in identifying lithology was 52.4%.

Table 2. Lithology of samples and results of three methods to predict lithology.

| No. | Lithology | FDA | BP Neural Network | | C&RT | |
|-----|-----------|-------------------------|-------------------------|-------------|-------------------------|-------------|
| | | Prediction of Lithology | Prediction of Lithology | Sample Type | Prediction of Lithology | Sample Type |
| 1 | sandstone | sandstone | sandstone | training | sandstone | training |
| 2 | sandstone | sandy mudstone | sandstone | test | sandstone | training |
| 3 | sandstone | sandy mudstone | sandstone | training | sandstone | training |
| 4 | sandstone | sandstone | sandstone | training | sandstone | training |
| 5 | sandstone | sandstone | sandstone | test | sandstone | training |
| 6 | sandstone | sandstone | sandstone | training | sandstone | training |
| 7 | sandstone | sandstone | sandstone | training | sandstone | training |
| 8 | sandstone | sandstone | sandstone | training | sandstone | training |
| 9 | sandstone | sandstone | sandstone | training | sandstone | training |
| 10 | sandstone | sandstone | sandstone | training | sandstone | training |
| 11 | sandstone | sandstone | sandstone | training | sandstone | training |
| 12 | sandstone | sandstone | sandstone | training | sandstone | training |
| 13 | sandstone | sandstone | dolomite | test | sandstone | training |
| 14 | sandstone | sandstone | sandstone | training | sandstone | training |
| 15 | sandstone | sandstone | sandstone | test | sandstone | training |
| 16 | sandstone | sandstone | sandstone | training | sandstone | training |
| 17 | sandstone | sandstone | sandstone | test | sandstone | training |
| 18 | sandstone | sandstone | sandstone | training | mudstone | training |
| 19 | sandstone | shale | sandstone | training | sandstone | training |
| 20 | sandstone | sandstone | sandstone | training | sandstone | training |
| 21 | sandstone | shale | sandstone | training | sandstone | test |
| 22 | sandstone | sandstone | sandstone | training | sandstone | training |
| 23 | sandstone | sandstone | sandstone | training | sandstone | training |
| 24 | sandstone | sandstone | sandstone | training | sandstone | training |
| 25 | sandstone | sandstone | sandstone | training | sandstone | training |
| 26 | sandstone | sandstone | sandstone | training | sandstone | training |
| 27 | sandstone | sandstone | sandstone | training | sandstone | training |
| 28 | sandstone | sandstone | sandstone | training | sandstone | training |
| 29 | sandstone | mudstone | sandstone | training | sandstone | training |
| 30 | sandstone | sandstone | sandstone | training | sandstone | training |

Table 2. Cont.

| No. | Lithology | FDA | BP Neural Network | | C&RT | |
|-----|---------------------|-------------------------|-------------------------|-------------|-------------------------|-------------|
| | | Prediction of Lithology | Prediction of Lithology | Sample Type | Prediction of Lithology | Sample Type |
| 31 | sandstone | sandstone | sandstone | training | sandstone | training |
| 32 | sandstone | shale | sandstone | test | sandstone | training |
| 33 | sandstone | sandstone | sandstone | training | sandstone | training |
| 34 | sandstone | shale | sandstone | training | sandstone | training |
| 35 | sandstone | sandstone | sandstone | training | sandstone | training |
| 36 | sandstone | sandstone | sandstone | training | sandstone | training |
| 37 | sandstone | sandstone | sandstone | training | sandstone | training |
| 38 | sandy mudstone | limestone | sandy mudstone | training | sandy mudstone | training |
| 39 | sandy mudstone | shale | dolomite | training | dolomite | training |
| 40 | sandy mudstone | sandstone | sandy mudstone | training | sandy mudstone | training |
| 41 | sandy mudstone | sandy mudstone | sandy mudstone | training | sandstone | training |
| 42 | sandy mudstone | sandy mudstone | sandstone | training | sandstone | test |
| 43 | sandy mudstone | shale | sandy mudstone | training | sandy mudstone | training |
| 44 | mudstone | shale | mudstone | training | mudstone | training |
| 45 | mudstone | mudstone | mudstone | training | mudstone | training |
| 46 | mudstone | mudstone | mudstone | training | mudstone | training |
| 47 | mudstone | mudstone | mudstone | training | mudstone | training |
| 48 | mudstone | mudstone | mudstone | training | mudstone | training |
| 49 | mudstone | shale | mudstone | test | mudstone | training |
| 50 | mudstone | shale | mudstone | training | mudstone | training |
| 51 | mudstone | sandstone | mudstone | training | mudstone | training |
| 52 | mudstone | sandstone | mudstone | training | sandstone | training |
| 53 | mudstone | sandy mudstone | mudstone | test | shale | training |
| 54 | mudstone | sandy mudstone | mudstone | training | mudstone | test |
| 55 | mudstone | sandy mudstone | sandstone | training | mudstone | training |
| 56 | mudstone | sandy mudstone | mudstone | training | mudstone | training |
| 57 | mudstone | sandstone | sandstone | training | mudstone | training |
| 58 | mudstone | sandstone | mudstone | training | mudstone | training |
| 59 | mudstone | shale | shale | training | mudstone | training |
| 60 | mudstone | shale | mudstone | training | mudstone | training |
| 61 | mudstone | shale | mudstone | training | mudstone | training |
| 62 | mudstone | sandstone | mudstone | training | mudstone | training |
| 63 | mudstone | shale | mudstone | training | mudstone | training |
| 64 | mudstone | shale | Calcareous mudstone | training | mudstone | training |
| 65 | mudstone | shale | mudstone | training | sandstone | training |
| 66 | mudstone | shale | mudstone | training | mudstone | training |
| 67 | mudstone | shale | shale | training | mudstone | training |
| 68 | Calcareous mudstone | mudstone | Calcareous mudstone | training | mudstone | training |
| 69 | Calcareous mudstone | mudstone | Calcareous mudstone | test | Calcareous mudstone | training |
| 70 | Calcareous mudstone | sandstone | Calcareous mudstone | training | Calcareous mudstone | training |
| 71 | Calcareous mudstone | shale | shale | training | shale | training |
| 72 | Calcareous mudstone | shale | Calcareous mudstone | training | Calcareous mudstone | training |
| 73 | Calcareous mudstone | shale | shale | training | Calcareous mudstone | test |
| 74 | Calcareous mudstone | shale | sandstone | training | Calcareous mudstone | training |
| 75 | Calcareous mudstone | sandstone | sandstone | training | sandstone | training |
| 76 | Calcareous mudstone | shale | shale | training | mudstone | training |
| 77 | Calcareous mudstone | shale | mudstone | test | Calcareous mudstone | training |
| 78 | Calcareous mudstone | shale | mudstone | training | Calcareous mudstone | training |
| 79 | Calcareous mudstone | shale | Calcareous mudstone | training | Calcareous mudstone | test |
| 80 | dolomite | shale | dolomite | training | dolomite | test |
| 81 | dolomite | shale | shale | training | dolomite | training |
| 82 | dolomite | shale | shale | training | dolomite | training |
| 83 | dolomite | shale | dolomite | training | dolomite | training |
| 84 | dolomite | sandstone | dolomite | training | shale | training |
| 85 | dolomite | shale | dolomite | training | dolomite | training |
| 86 | dolomite | shale | dolomite | training | dolomite | training |
| 87 | dolomite | shale | dolomite | test | dolomite | training |
| 88 | dolomite | sandstone | dolomite | training | sandstone | training |
| 89 | dolomite | sandstone | dolomite | training | dolomite | training |
| 90 | dolomite | sandstone | dolomite | training | dolomite | training |

Table 2. Cont.

| No. | Lithology | FDA | BP Neural Network | | C&RT | |
|-----|-----------|-------------------------|-------------------------|-------------|-------------------------|-------------|
| | | Prediction of Lithology | Prediction of Lithology | Sample Type | Prediction of Lithology | Sample Type |
| 91 | dolomite | shale | dolomite | training | dolomite | training |
| 92 | dolomite | shale | shale | training | shale | test |
| 93 | dolomite | shale | dolomite | test | dolomite | training |
| 94 | dolomite | shale | dolomite | training | dolomite | training |
| 95 | dolomite | shale | shale | training | shale | training |
| 96 | dolomite | mudstone | dolomite | training | dolomite | test |
| 97 | limestone | sandy mudstone | limestone | training | limestone | training |
| 98 | limestone | limestone | limestone | training | shale | training |
| 99 | limestone | shale | limestone | training | limestone | training |
| 100 | shale | sandstone | Calcareous mudstone | training | shale | training |
| 101 | shale | shale | shale | training | shale | training |
| 102 | shale | shale | shale | training | shale | training |
| 103 | shale | shale | dolomite | training | shale | training |
| 104 | shale | shale | shale | test | shale | training |
| 105 | shale | shale | shale | training | shale | training |
| 106 | shale | shale | shale | training | shale | training |
| 107 | shale | shale | shale | test | shale | training |
| 108 | shale | shale | dolomite | training | shale | training |
| 109 | shale | shale | dolomite | training | dolomite | training |
| 110 | shale | shale | shale | test | shale | training |
| 111 | shale | shale | shale | training | shale | training |
| 112 | shale | shale | shale | training | shale | training |
| 113 | shale | shale | shale | training | shale | training |
| 114 | shale | shale | shale | training | shale | training |
| 115 | shale | shale | shale | training | shale | training |
| 116 | shale | shale | dolomite | training | shale | training |
| 117 | shale | shale | shale | training | shale | training |
| 118 | shale | shale | shale | training | shale | training |
| 119 | shale | shale | shale | training | shale | training |
| 120 | shale | shale | shale | training | shale | training |
| 121 | shale | shale | shale | training | shale | training |
| 122 | shale | shale | shale | training | shale | training |
| 123 | shale | shale | shale | training | shale | training |
| 124 | shale | shale | shale | test | shale | training |
| 125 | shale | shale | shale | training | shale | training |
| 126 | shale | shale | shale | training | shale | training |
| 127 | shale | shale | shale | test | shale | training |
| 128 | shale | sandstone | Calcareous mudstone | training | shale | training |
| 129 | shale | shale | shale | training | shale | training |
| 130 | shale | shale | shale | training | shale | training |
| 131 | shale | sandy mudstone | shale | training | shale | training |
| 132 | shale | limestone | shale | training | shale | training |
| 133 | shale | shale | dolomite | training | shale | training |
| 134 | shale | sandy mudstone | shale | training | limestone | training |
| 135 | shale | shale | shale | training | mudstone | training |
| 136 | shale | shale | shale | training | shale | training |
| 137 | shale | shale | shale | training | shale | training |
| 138 | shale | shale | shale | training | shale | training |
| 139 | shale | shale | shale | training | shale | training |
| 140 | shale | shale | shale | training | mudstone | training |
| 141 | shale | sandstone | shale | training | shale | training |
| 142 | shale | sandstone | shale | training | shale | training |
| 143 | shale | shale | shale | training | shale | training |
| 144 | shale | shale | shale | test | shale | training |
| 145 | shale | shale | shale | training | shale | training |
| 146 | shale | shale | shale | training | shale | training |
| 147 | shale | sandstone | shale | test | sandstone | training |

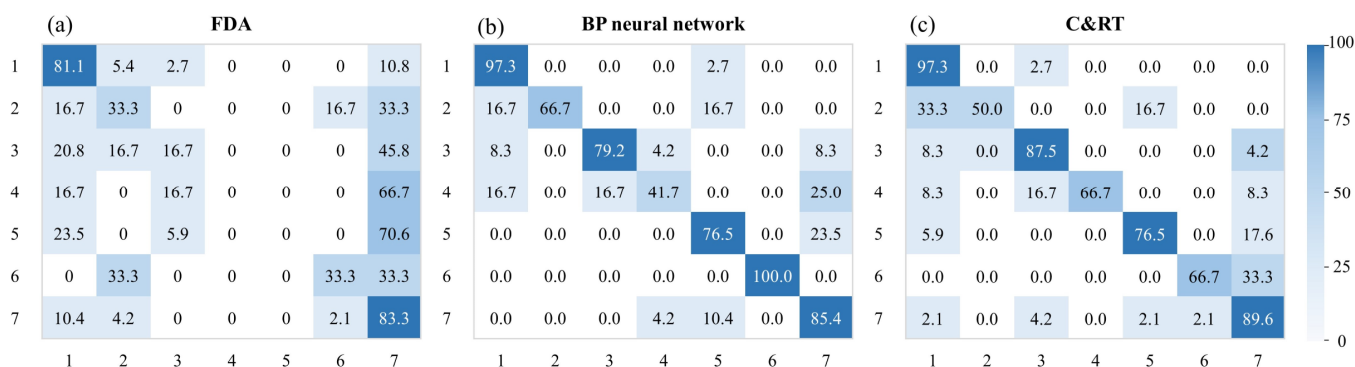


Figure 7. Confusion matrix of three lithology identification models.

The accuracy rate of the BP neural network in identifying the Es_1^L was 82.3%. The accuracy rate of 19 of these test samples was 89.4%. Limestone and sandstone can be accurately identified by BP neural network with an accuracy of 100% and 97.3%, respectively, and shale, mudstone, and dolomite have an accuracy of 85.4%, 79.2%, and 76.5%, respectively, which can be well-identified. The calcareous mudstone has a poor recognition effect. The calcareous mudstone is wrongly divided into sandstone, mudstone, and shale (Figure 7b).

In the C&RT model, sandstone, shale, mudstone, and dolomite can be well-identified, with an accuracy of more than 75%, and the highest accuracy of sandstone is 97.3% (Figure 7c). Only half of the sandy mudstone is correctly identified, and the wrong part is mainly classified as sandstone. A total of 16 test samples were used, including sandstone, sandy mudstone, mudstone, calcareous mudstone, and dolomite. The CR&T model’s prediction accuracy was 88%. The accuracy rate of the C&RT model in identifying lithology was 85.7%.

5. Discussion

5.1. Logging Characteristics of Lithology

Lithology describes the physical properties of rock, such as color, texture, grain size, and composition [38]. Differences in these physical properties produce different response characteristics in logging, and analyzing these characteristics can invert the distribution of various subsurface lithologies [39,40]. The following is a brief description of the response characteristics of the well logs used in this study:

(1) AC is the recorded time it takes for a sound wave to travel at a fixed interval between formations. The formation contains not only rock but also water, CO_2 , CH_4 , and hydrocarbon fluids (oil and bitumen) in the pores of the rock [41–44]. Sound waves travel faster in solids such as rocks and minerals than in other fluids such as water and oil. Even the difference in lithology in the rock affects the propagation velocity of sound waves [10]. The P-wave velocity of mudstone, sandstone, limestone, and dolomite is 1800 m/s, 2130~5180 m/s, 3950~4900 m, 4000~5650 m/s, and 4600~6100 m/s, respectively [45], among which the porosity of sandstone, limestone, and dolomite is between 5% and 20%.

(2) SP represents the natural potential difference between the trajectory of the wellbore and the ground [46]. SP has a good effect in identifying sandstone with developed pores and mudstone. Tight rocks such as calcareous mudstone and shale often have higher electrical resistance than mudstone. However, SP is also affected by the type of reservoir fluid, salinity, and saturation. Using SP to judge lithology often needs to be combined with other logging.

(3) GR is recording the total natural gamma radiation intensity in the rock with a gamma-ray detector [47]. Uranium, thorium, and potassium play a decisive role in natural gamma radioactivity in rocks. Minerals such as gypsum ($CaSO_4 \cdot H_2O$), anhydrite ($CaSO_4$), quartz (SiO_2), dolomite ($CaMgCO_3$), and calcite ($CaCO_3$) in sedimentary rocks have low radioactivity, and with the increase in clay content, the radioactivity becomes stronger.

Among the clay minerals, montmorillonite has a large surface area, a strong ability to adsorb radioactive substances, and contains more uranium oxide, which is the main contributor to radioactivity; potassium in illite can also adsorb uranium oxide and is radioactive.

(4) CAL measures the change in borehole diameter with depth, which is related to lithology and the mud used for drilling [48]. The well diameter of sandstone with good permeability is smaller than that of the drill bit. On the contrary, the well diameter of easily collapsed mudstone and carbonate rock with developed pores is larger than the drill bit. Lithology is classified based on these features. As a result, the change in well diameter is also related to cementing quality and wellbore azimuth, and lithology identification needs to be combined with other well logs.

(5) In general, sandstone with high resistance is sandstone, mudstone with low resistance, and reservoirs containing fluids are also low resistivity. However, many factors affect resistivities, such as mud invasion, electrode spacing, and wellbore inclination [49]. Therefore, it is mainly used for qualitative analysis, and further analysis needs to be combined with other data.

(6) CNL measures the amount of hydrogen because hydrogen slows down high-energy and fast neutrons [46]. Sandstone, dolomite, limestone, and migmatites are commonly found in reservoirs. The minerals that make up these rocks have no hydrogen, and most of the hydrogen is in the fluids in the pores of the rocks. Among them, the deceleration capacity of saturated freshwater sandstone is less than that of limestone, and the deceleration capacity of saturated freshwater limestone is lower than that of dolomite [9]. The pores of mudstone and shale contain bound water, and clay minerals contain crystal water. The higher the clay content, the higher the hydrogen content.

(7) DEN irradiates the formation with gamma rays and measures the bulk density of the formation according to the Compton effect [47]. The density of a liquid is much lower than that of solid minerals. The densities of several common minerals are quartz (2.65 g/cm^3), calcite (2.71 g/cm^3), dolomite (2.87 g/cm^3), gypsum (2.32 g/cm^3), and anhydrite (2.96 g/cm^3). The reference densities of the corresponding rocks for these minerals are sandstone (2.644 g/cm^3), limestone (2.710 g/cm^3), dolomite (2.877 g/cm^3), gypsum (2.355 g/cm^3), and anhydrite (2.960 g/cm^3). The porosity of these rocks is close to zero.

The logging characteristics of the lithology described above are ideal, but the actual formation is often more complex. In particular, the continental lake basins are affected by severe sedimentation and diagenesis, with strong inorganic heterogeneity [26,50], mostly mixed rocks, and blurred lithologic boundaries. Mudstone and shale strata are widely developed in the Es_1^L , mainly mudstone and shale, with dolomite, limestone, sandstone, and migmatite interlayers. Therefore, the rock density, radioactive element content, and well diameter of the whole section have little change. Combined with mathematical analysis, AC, SP, CNL, and R25 were selected as input parameters. The direct relationship between the four logging curves is poor, and the lithology is not classified on the intersection of the four logging curves (Figure 8). Clay minerals are rich in crystalline water, adsorbed water, and oil in the pores of mudstone [51], and mudstone has a high CNL value. Shale, calcareous mudstone, and some mudstones have a high degree of overlap, and the mineral compositions of the three are similar and difficult to distinguish. Effective identification of complex lithologies is therefore required with the help of some other measures.

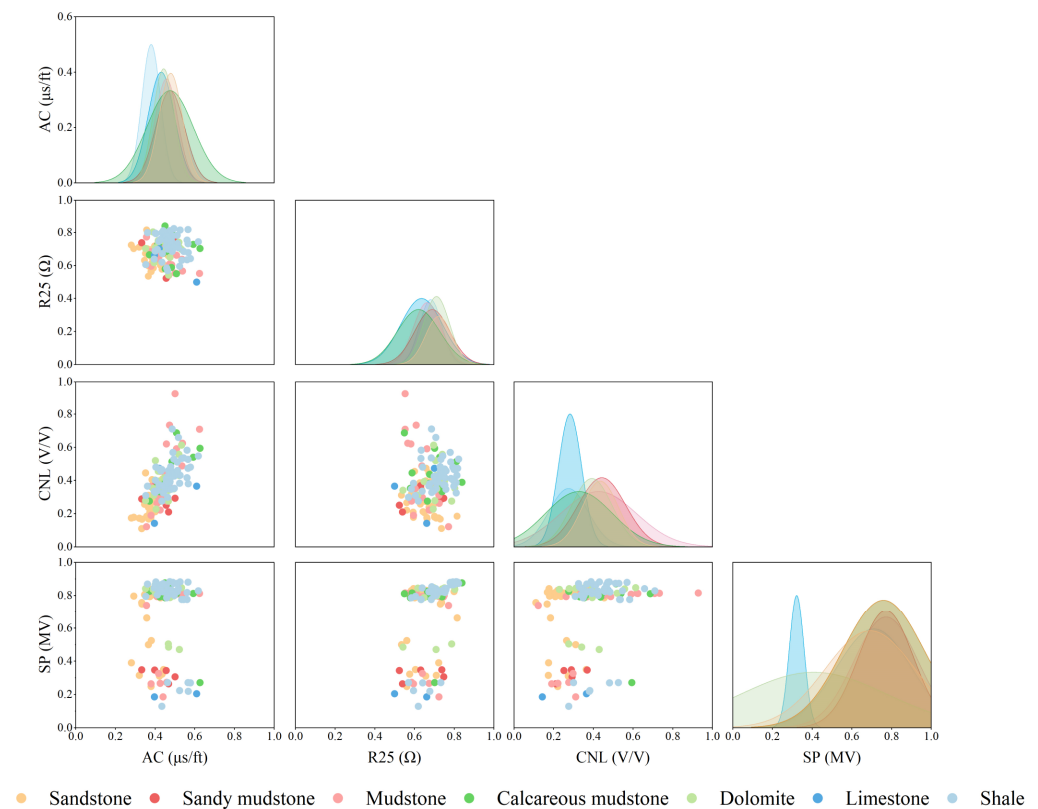


Figure 8. Cross plots of well logs against lithology labels.

5.2. Comparison of the Three Models

Table 2 shows the differences in the prediction results of the three methods. Shale and sandstone can be accurately identified by FDA, BP neural network, and C&RT, and the identification accuracy is above 80% (Figure 7). Sandy mudstone and calcareous mudstone are mixed rocks with poor recognition effects. C&RT has the highest accuracy in identifying sandy mudstone and calcareous mudstone, with 50.0% and 66.7% accuracy rates, respectively (Figure 7). BP neural network and C&RT have the same results in identifying dolomite, while FDA cannot identify dolomite. The lithology recognition accuracies of FDA, BP neural network, and C&RT models are 52.4%, 82.3%, and 85.7%, respectively (Figure 7). FDA cannot be effectively applied to the identification of complex lithology. The complicated lithology of continental shale formations can be more accurately identified by BP neural network and C&RT; however, BP neural network is a “black box” and cannot be seen. This issue can be solved more effectively with C&RT since each step of the identification process can be presented and adjusted to the demands. C&RT is a lithology identification method therefore suitable to the Es_1^L .

5.3. Application

Well B11x is located in the Xiliu area of Raoyang sag. It is a typical shale oil exploration well in Raoyang sag. Using the established BP neural network and C&RT model to identify lithology, the lithology distribution characteristics of the Es_1^L of well B11x were analyzed. The Es_1^L of well B11x is dominated by mudstone and shale, with interlayers of calcareous mudstone, sandstone, and dolomite. The core lithology in Figure 9 is obtained from mud logging data. These data are greatly influenced by artificial subjective, especially in the continental shale strata with heterogeneity and strength, and the accuracy of the data remains to be discussed. Nonetheless, it can also be used as a reference point to advise on some geological work. The lithological identification results of the BP neural network show that sandstone can be effectively identified. However, shale, mudstone, calcareous mudstone, and dolomite with similar mineral compositions cannot be distinguished. At

3512.91~3513.13 m, the rock core shows mudstone, while the prediction result of the BP neural network is shale. The bedding fractures of shale have larger storage space [52], which reduces the value of AC. The natural potential of this section does not change much, and the value of AC is high. Combined with the photos of the rock core (Figure 10), the rock of this section is mudstone. Figure 10b shows that the upper bedding at 3547.90~3548.06 m is developed as shale, and the lower part is dolomite. At 3564.06~3564.36 m, the rock has a blocky structure without bedding.

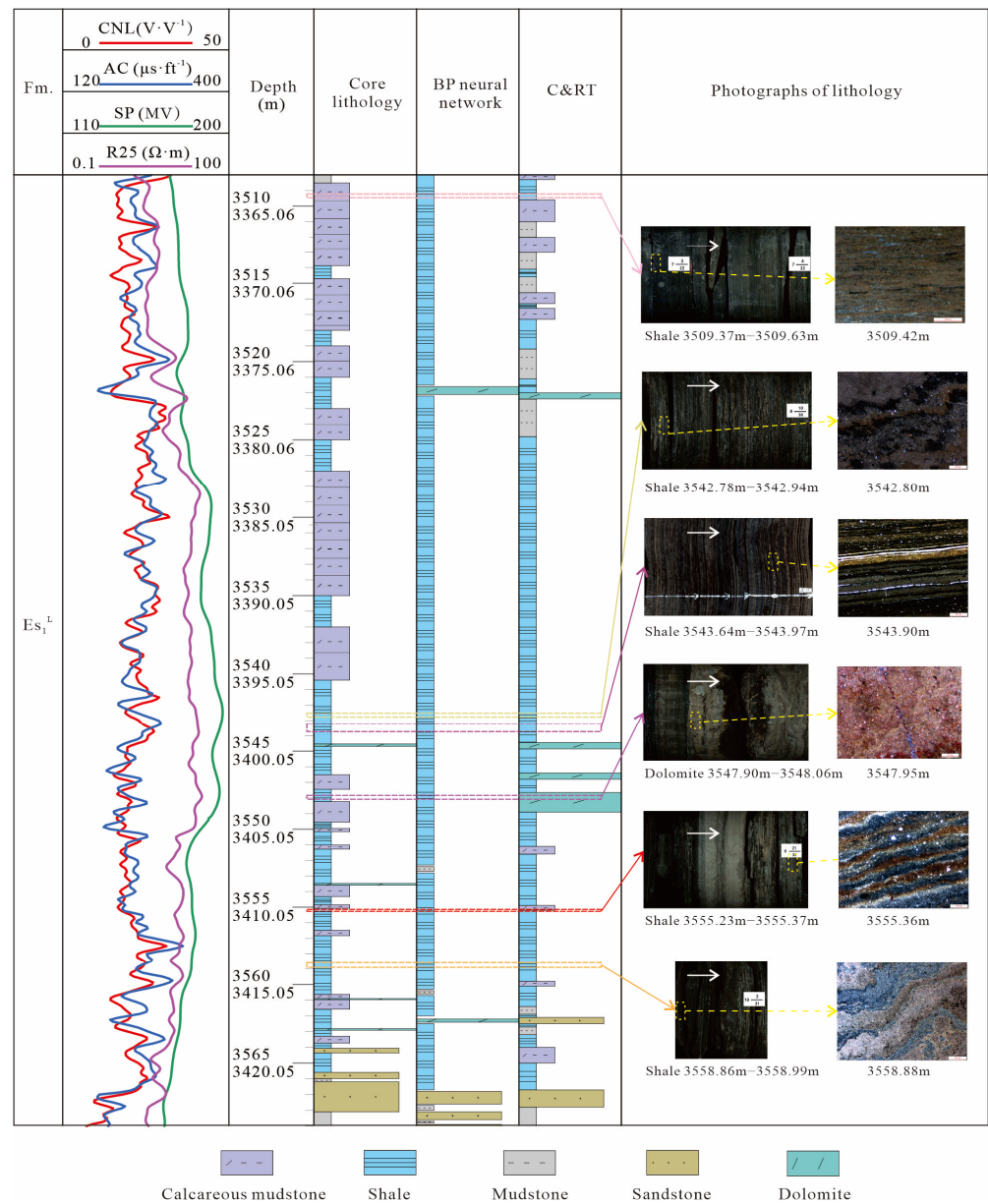


Figure 9. Lithology identification of well B11x by BP neural network and C&RT.

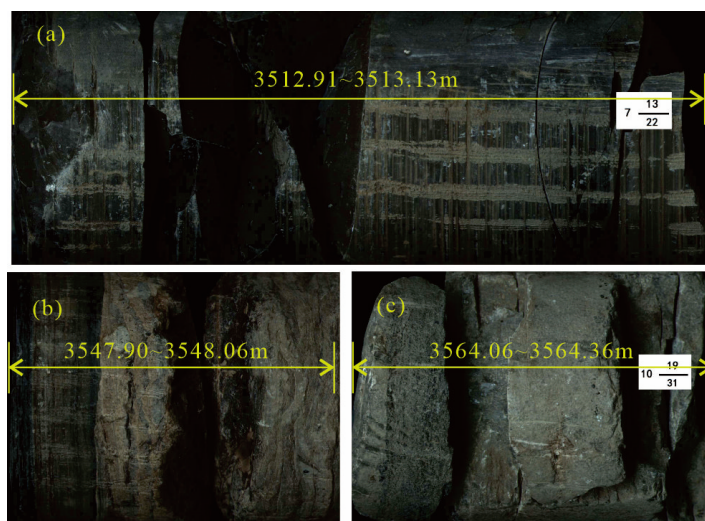


Figure 10. Rock core of well B11x. (a) At 3512.91~3513.13 m, the rock core shows mudstone; (b) The upper bedding at 3547.90~3548.06 m is developed as shale, and the lower part is dolomite; (c) At 3564.06~3564.36 m, the rock has a blocky structure without bedding.

The recognition result of C&RT is better than that of the BP neural network, especially in the recognition of interlayers and thin interlayers, which are usually favorable intervals for the exploration and development of shale oil. The lithology identified by C&RT is highly similar to the lithology obtained from mud logging, but there are also differences. For example, at 3509.37~3509.63 m, the core lithology shows calcareous mudstone, while the thin section identification result is shale, and the recognition result of C&RT is the same. The acoustic transit time of this section is small, the resistivity is low, and the value of CNL is high, indicating that it has a larger storage space and more water. This response is usually due to interlayer fractures in the shale in tight reservoirs. The acoustic time difference of carbonate rocks is higher than that of tight shale. Carbonate rocks can form reservoir spaces containing fluids due to dissolution [53]. Fluids and primary spaces increase the hydrogen content and reduce resistivity. At 3547.90~3548.06m, the values of AC and CNL are high, and the resistivity is low. Combined with thin section identification, the lithology is dolomite.

The accuracy of the BP neural network identification lithology model is lower than that of the C&RT model in identifying mixed lithology. Although the accuracy of the two models differs by only 3.4%, it can be found in the process of model application that identifying each lithology by C&RT is reasonable. Therefore, it is practical to use C&RT to identify lithology, and it can provide a reference for the exploration and development of shale oil in shale intervals.

6. Conclusions

The identification of complex lithology is a typical nonlinear classification problem. Intelligent algorithms can effectively solve this problem. Different algorithms have different identification effects on different lithologies. Through FDA, BP neural network, and C&RT to identify the complex lithology of the mudstone and shale strata in the Es_1^L of Raoyang Sag, the following conclusions are drawn:

(1) Each logging has a different sensitivity to lithology. The four logs AC, SP, CNL, and R25 of the Es_1^L the Raoyang sag have the highest sensitivity to seven lithologies and are used as input parameters for lithology identification.

(2) The intersection graph method cannot distinguish complex lithology. FDA, BP neural network, and C&RT have an accuracy of 52.4%, 82.3%, and 85.7%, respectively, in identifying the Es_1^L . The accuracy of the BP neural network in identifying mixed lithology

is lower than that of C&RT, and the accuracy of C&RT in identifying sandstone, shale, and mudstone is 97.3%, 89.6%, and 87.5%, respectively.

(3) C&RT can identify interlayers and thin interlayers in shale strata. The C&RT identification results of well B11x show that the lithology is dominated by shale, with mudstone, sandstone, calcareous mudstone, and dolomite interlayers.

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