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Keywords: split ratio, exhaust heat recovery ratio, thermal efficiency, pressure, supercritical

Abstract:

Waste heat recovery of the internal combustion engine (ICE) has attracted much attention, and the supercritical carbon dioxide (S-CO2) cycle was considered as a promising technology. In this paper, a comparison of four S-CO2 cycles for waste heat recovery from the ICE was presented. Improving the exhaust heat recovery ratio and cycle thermal efficiency were significant to the net output power. A discussion about four different cycles with different design parameters was conducted, along with a thermodynamic performance. The results showed that choosing an appropriate inlet pressure of the compressor could achieve the maximum exhaust heat recovery ratio, and the pressure increased with the rising of the turbine inlet pressure and compressor inlet temperature. The maximum exhaust heat recovery ratio for recuperation and pre-compression of the S-CO2 cycle were achieved at 7.65 Mpa and 5.8 MPa, respectively. For the split-flow recompression cycle, thermal efficiency first increased with the increasing of the split ratio (SR), then decreased with a further increase of the SR, but the exhaust heat recovery ratio showed a sustained downward trend with the increase of the SR. For the split-flow expansion cycle, the optimal SR was 0.43 when the thermal efficiency and exhaust heat recovery ratio achieved the maximum. The highest recovery ratio was 24.75% for the split-flow expansion cycle when the total output power, which is the sum of the ICE power output and turbine mechanical power output, increased 15.3%. The thermal performance of the split-flow expansion cycle was the best compared to the other three cycles.

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Article

Thermodynamic Analysis of Supercritical Carbon Dioxide Cycle for Internal Combustion Engine Waste Heat Recovery

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Abstract: Waste heat recovery of the internal combustion engine (ICE) has attracted much attention, and the supercritical carbon dioxide (S-CO₂) cycle was considered as a promising technology. In this paper, a comparison of four S-CO₂ cycles for waste heat recovery from the ICE was presented. Improving the exhaust heat recovery ratio and cycle thermal efficiency were significant to the net output power. A discussion about four different cycles with different design parameters was conducted, along with a thermodynamic performance. The results showed that choosing an appropriate inlet pressure of the compressor could achieve the maximum exhaust heat recovery ratio, and the pressure increased with the rising of the turbine inlet pressure and compressor inlet temperature. The maximum exhaust heat recovery ratio for recuperation and pre-compression of the S-CO₂ cycle were achieved at 7.65 Mpa and 5.8 MPa, respectively. For the split-flow recompression cycle, thermal efficiency first increased with the increasing of the split ratio (SR), then decreased with a further increase of the SR, but the exhaust heat recovery ratio showed a sustained downward trend with the increase of the SR. For the split-flow expansion cycle, the optimal SR was 0.43 when the thermal efficiency and exhaust heat recovery ratio achieved the maximum. The highest recovery ratio was 24.75% for the split-flow expansion cycle when the total output power, which is the sum of the ICE power output and turbine mechanical power output, increased 15.3%. The thermal performance of the split-flow expansion cycle was the best compared to the other three cycles.

Keywords: supercritical; pressure; thermal efficiency; exhaust heat recovery ratio; split ratio

1. Introduction

The internal combustion engine (ICE) has become a primary power source which has been widely applied in vehicles, industrial machineries, agricultural machineries and stationary power units [1]. Improving the total thermal efficiency of the ICE has been widely researched since last century to reduce fossil fuel consumption and CO_2 emissions. Different ways have been explored to increase ICE efficiency; for example, turbochargers, diesel oxidation catalysts (DOC), homogeneous charge compression (HCCI), variable valve timing (VVT) and exhaust gas recirculation (EGR). However, more than 50% of the energy from air-fuel mixture combustion cannot be fully utilized [2]. Therefore, more and more attention has focused on how to recover the waste heat of the ICE from waste gas.

The organic rankine cycle (ORC) can use low temperature heat, which has some advantages, such as simple structure, high reliability and easy maintenance. Therefore, many researchers are studying on the ORC to recover ICE waste heat [3,4]. The exergy analysis of a two-parallel step ORC for waste heat recovery from an ICE was performed, and R123 was considered as the best working fluid [4].



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Wang et al. [5] compared the part-load performance of four different ORC forms with dynamic math models. The output of electrical power was even improved up to 30% when using integrally the ORC system for a diesel engine [6]. The ICE thermal efficiency increased by 1.2%–3.7% when the engine-ORC system was used [7]. In addition to the ORC, there are many new thermodynamic cycles to use for waste heat. He et al. [8] provided a combined thermodynamic cycle, which consisted of the ORC and Kalina cycle. Compared to the conventional cycle, the cycle had a higher efficiency. Morgan et al. [9] provided a novel intracycle waste heat recovery methodology, enhancing the thermal efficiency.

However, the waste heat of an ICE usually has a relative high temperature, which leads to a low recovery efficiency of the ORC. The supercritical CO_2 (S- CO_2) cycle, which is used for ICE waste heat recovery, is considered as a promising alternative. The S- CO_2 has many advantages over the ORC, such as compactness, simplicity, sustainability and superior economy [10]. Song et al. [11] combined an ORC with the S- CO_2 cycle for heat recovery to utilize the residual heat, leading to increased thermal efficiency. Wu et al. [12] analyzed the effects of a recuperator on the performances of a CO_2 transcritical power cycle for low temperature geothermal plants. The results showed that the overall net power and thermal efficiency of regenerative system were higher than that of the basic system. However, a single recuperated S- CO_2 could not fully use the available waste heat. The specific heat of the cold side flow was far more than that of the hot side flow in the recuperator, and it is important for the layout design of the S- CO_2 [10]. Therefore, various cycle layouts have been designed and researched to reduce the internal irreversible losses in the recuperator and increase thermal efficiency.

A thermodynamic comparison of five S-CO₂ cycle layouts was conducted by Fahad et al. [13], and the results showed that the recompression Brayton cycle could achieve the highest thermal efficiency with a value of 52%. Energy and exergy analyses of four different supercritical CO₂ Brayton cycle layouts (simple, recompression, partial cooling with recompression and recompression with main compression intercooling) were performed by Padilla et al. [14], and the results indicated recompression with the main compression intercooling Brayton cycle performed the best. The performance of single recuperated and recompression S-CO₂ cycles for recovering low temperature waste gas heat was discussed by Mohagheghi [15]. The results suggested that the performance of the recompression cycle was not the best one in terms of net power output. According to the above descriptions, the S-CO₂ cycle has been applied in various heat sources such as geothermal power [12,16], nuclear power [17,18], concentrated solar power [13,14], fuel cells [19] and combustion [20,21]. However, there were few studies on waste heat recovery, especially for ICE waste heat.

In this paper, a comparison of four S-CO₂ cycles (recuperation, pre-compression, split-flow recompression and split-flow expansion) for ICE waste heat recovery was presented. The exhaust heat recovery ratio and cycle thermal efficiency were very important to the net output power. A discussion on the cycle design parameters for four different cycles was conducted, and the major influencing parameters on the thermal efficiency and exhaust heat recovery ratio of each cycle layout were analyzed.

2. System Description

2.1. ICE System

Exhaust gas of a 6-cylinder 4-stroke supercharged diesel-oil fired engine was selected as the waste heat source. The main parameters of the engine were introduced in Table 1. The thermodynamic performance of the S-CO₂ cycle, which was used to recover waste heat from the ICE, was researched; thus, the engine was considered to work at the rated condition. The mass fraction of the exhaust gases could be calculated as: $CO_2 = 15.10\%$, $H_2O = 5.37\%$, $N_2 = 73.04\%$ and $O_2 = 6.49\%$, which was used to evaluate the waste gas thermal parameters. The S-CO₂ cycles mentioned in this paper were mainly classified into four cycles: recuperation S-CO₂ cycle, pre-compression S-CO₂ cycle, split-flow recompression S-CO₂ cycle and split-flow expansion S-CO₂ cycle, and their operating principle was introduced in the following section.

Parameter	Values
Power output	235.8 kW
Torque	1500 Nm
Fuel consumption	47.79 kg/h
Combustion air mass flow	943 kg/h
Exhaust temperature	519 °C
Exhaust mass flow	990.79 kg/h

Table 1. Main parameters of the internal combustion engine (ICE).

2.2. Recuperation S-CO₂ Cycle

The operating principle and temperature-entropy (T-s) diagram of recuperation of the S-CO₂ cycle were shown in Figures 1 and 2, respectively. The cycle consisted of five main devices: compressor (CP), recuperator (RCP), heater, turbine (TB) and cooler (C). For the ICE exhaust gas, the hot from the ICE rejects heat in the heater and then discharges it to the atmosphere. The temperature of the exhaust decreases from $T_{g,in}$ to $T_{g,out}$. The S-CO₂ cycle can be identified as 1-2-3-4-5-6-1 and described as follows: generated high-pressure S-CO₂ (point 1) in the heater flows into the turbine, and its enthalpy is converted into output power. The process 1 to 2 means an isentropic expansion, which is ideal and impossible. The real expansion process in the turbine is process 1 to 2. The low-pressure CO₂ (point 2) discharged from the turbine flows into the recuperator, where it rejects heat to cold working fluid. Then, the CO₂ (point 3) flows into the cooler, where it is cooled by supplied cooling water. The low temperature CO₂ (point 4) is compressed into high-pressure gas (point 5) by the compressor. High pressure CO₂ flows into the recuperator, where it is preheated to a medium temperature (point 6) and then flows into the heater, where it is heated to a high temperature (point 1) by the ICE exhaust.



Figure 1. Operating principle of the recuperation of a supercritical- CO_2 (S- CO_2) cycle. ICE: internal combustion engine, RCP: recuperator, TB: turbine and $T_{g,in}$ and $T_{g,out}$: temperature increase and decrease.



Figure 2. Temperature-entropy (T-s) diagram of the recuperation of a S-CO₂ cycle.

2.3. Pre-Compression of the S-CO₂ Cycle

A single recuperation S-CO₂ cycle used for a high temperature heat source cannot fully utilize the available waste heat. The turbine exhaust S-CO₂ has a low specific heat, while the compressor exit S-CO₂ has a high specific heat. As a result, there is a big heat transfer temperature difference in the recuperator, which will lead to large internal irreversibility. Therefore, the recuperator is divided into a low temperature recuperator (LTR) and a high temperature recuperator (HTR) in other S-CO₂ cycle layouts.

Figures 3 and 4 show the layout of the pre-compression S-CO₂ cycle and its T-s diagram. The compression is completed in the pre-compressor (PC) and main compressor (MC), successively. The working fluid exiting the HTR is compressed from state 3 to state 4 in the PC. Compared to recuperation of the S-CO₂ cycle, the working fluid pressure can be adjusted conveniently, because the pressure of the MC inlet at state 6 can be adjusted by the working fluid pressure of the turbine outlet at state 2 and the compression ratio. The pressure difference between the heat fluid and cool fluid in the LTR can be decreased, which can reduce the pinch point in the heater and decrease the internal irreversible loss.



Figure 3. Operating principle of pre-compression S-CO₂ cycle. MC: main compressor, LTR: low temperature recuperator, PC: pre-compressor and HTR: high temperature recuperator.



Figure 4. T-s diagram of pre-compression S-CO₂ cycle.

2.4. Split-Flow Recompression S-CO₂ Cycle

The layout and T-s diagram of the split-flow recompression S-CO₂ cycle are shown in Figures 5 and 6, respectively. In a recompression S-CO₂ cycle, the flow is split at state 4, and CO₂ in the cold side with high specific heat is matched to the hot side large flow with lower specific heat in the low LTR to maximize the cycle efficiency. The fluid flow is divided into two parts at state 4, one part working fluid flows through the cooler (C), main compressor (MC), LTR, HTR and heater, successively. The other part working fluid is drawn into the re-compressor (RC) without cooling. Then, the working fluid from the MC at state 7 and LTR at state 8 are mixed at state 9. The ratio of the mass flow in the RC present in the total mass flow in the cycle is defined as the split ratio (SR).



Figure 5. Operating principle of the split-flow recompression S-CO₂ cycle. RC: re-compressor.



Figure 6. T-s diagram of the split-flow recompression S-CO₂ cycle.

2.5. Split-Flow Expansion of the S-CO₂ Cycle

The layout of the split-flow expansion S-CO₂ cycle and its T-s diagram are shown in Figures 7 and 8, respectively. In this cycle, the flow is split at state 6 and then mixed at state 4. One part working fluid flowing through the LTR and heater can achieve the highest cycle temperature at state 1. Then, it flows into the turbine 1 (TB-1), and the enthalpy of working fluid is converted into work. The exhaust steam is cooled in the HTR and cooler, successively. The other part working fluid is heated in the HTR and then flows into the turbine 2 (TB-2) to do work. The exhaust gas of the TB-2 is cooled in the LTR and mixed with the first part working fluid at state 4. The ratio of the mass flow in the TB-2 present in the total mass flow in the cycle is defined as the split ratio (SR).



Figure 7. Operating principle of the split-flow expansion S-CO₂ cycle. TB-1 and TB-2: turbine 1 and 2.



Figure 8. T-s diagram of the split-flow expansion cycle.

3. Thermodynamic Modeling

Before establishing the mathematical model of this system, some general assumptions should be formulated, as follows: (1) All devices operate at a steady state or nearly at a steady state; the property variations with time are small enough to ignore. (2) The kinetic and potential energies are neglected. (3) The heat losses in each component and pipe are also neglected. (4) The pressure drop and entropy increase in each component and pipe are ignored for simplicity. The basic thermal physical parameters of the cycles, which are based on previous works, are shown in Table 2 [22,23]. According to those assumptions, the change of working fluid is ideal in turbomachinery, and many losses in turbomachinery are ignored so the efficiency of the turbomachinery is kept constant.

Parameter	Values
Turbine inlet pressure	21–29 MPa [22,23]
Turbine inlet temperature	500 °C [22,23]
Compressor inlet pressure	7–10.5 MPa [22,23]
PC inlet pressure	5.6–6.8 MPa [22,23]
Compressor inlet temperature	32–38 °C [22,23]
Surrounding temperature	25 °C [22,23]
Isentropic efficiency of turbine	0.88 [22,23]
Isentropic efficiency of compressor	0.85 [22,23]
Heat exchanger effectiveness	0.95 [22,23]

Table 2. Thermal physical parameters of the cycles.

The thermal parameters of CO_2 can be calculated through two independent parameters, and some parameters at a special state must be decided by iterative calculation. In this study, the thermodynamic calculation model for the recuperation S-CO₂ cycle is introduced in detail, as follows. The set of Equations (1)–(9) correspond to the symbols and states shown in Figure 1 for the simple S-CO₂ recuperation cycle.

The heat absorption capacity of CO₂ is equal to the released heat of ICE exhaust, which is decided by:

$$\Phi = q_{mg}(h_{in} - h_{out}) = q_{mco2}(h_1 - h_6) \tag{1}$$

where q_{mg} is the mass flow rate of the exhaust gas of ICE and the subscripts in and out indicate the inlet and outlet states of the exhaust gas in the heater, respectively. q_{mco2} is the mass flow rate of the CO₂ gas.

Heat rejection in the cooler is

$$\Phi_c = q_{mco2}(h_3 - h_4) \tag{2}$$

The output power of the turbine is

$$W_T = q_{mco2}(h_1 - h_{2s})\eta_{S,T} = q_{mco2}(h_1 - h_2)$$
(3)

The power consumption of the compressor is

$$W_C = q_{mco2}(h_{5s} - h_4) / \eta_{S,C} = q_{mco2}(h_5 - h_4)$$
(4)

where $\eta_{S,T}$ and $\eta_{S,C}$ are the isentropic efficiency of the turbine and compressor, respectively.

The net output power of the recuperation S-CO₂ cycle is

$$W_{net} = W_T - W_C \tag{5}$$

The recuperator effectiveness is defined as

$$\varepsilon = \frac{T_2 - T_3}{T_2 - T_5} or \frac{T_6 - T_5}{T_2 - T_5}$$
(6)

The energy balance equation for the high temperature recuperator is

$$h_2 - h_3 = h_6 - h_5 \tag{7}$$

The thermodynamic performance for the S-CO₂ cycle could be evaluated by two parameters, thermal efficiency and the exhaust heat recovery ratio. Thermal efficiency η_t gauged the extent to which the energy input to the working fluid in the heat exchanger is converted to the net output power.

$$\eta_t = \frac{W_{net}}{\Phi} \tag{8}$$

The exhaust heat recovery ratio η_{re} is defined as the ratio of net power output to the maximum allowable heat rate from the waste heat source [3]. It can be obtained as follows:

$$\eta_{re} = \frac{W_{net}}{q_{mg}(h_{in} - h_0)} \tag{9}$$

where h_0 is the enthalpy of ICE exhaust gas at the environment temperature.

Similarly, the models for other cycle layouts can be obtained through a similar method. However, the heat transfer distribution in the LTR and HTR is unknown for the split cycle, so an iterative subroutine is necessary to obtain the heat distribution in the LTR and HTR. The calculation of the whole split recompression S-CO₂ cycle is shown in Figure 9.

First, the turbine outlet parameters are calculated by isentropic efficiency. Then, presuming the inlet temperature T_{99} at the cold side combining with the heat exchanger effectiveness ε are used to calculate the parameters of the PC, MC and LTR. Meanwhile, the new inlet temperature of the cold fluid in the HTR, T_{9} , is calculated and compared with T_{99} . If the difference between T_{9} and T_{99} is lower than 0.1 K, the T_{99} is right, else the T_{99} is replaced by T_{9} . Finally, the thermal efficiency and waste heat recovery ratio are calculated by those parameters in each equipment. The heat exchanger effectiveness ε is defined as the ratio of the maximum value of cold fluid temperature difference to hot fluid temperature difference and the inlet temperature difference between the cold fluid and the hot fluid. So, when calculating the parameter of the heat exchanger, the heat exchanger effectiveness and

calculation method must be considered. This process is part of the flow chart, and this process also has a judgment statement. First, the hot fluid temperature difference is presumed as the maximum temperature difference. Then, calculating the parameter of the whole system is based on this hypothesis. Finally, comparing the cold fluid temperature difference and the hot fluid temperature difference, the new heat exchanger effectiveness ε' is calculated by the new maximum temperature difference and compared with the fixed heat exchanger effectiveness. If the difference between ε and ε' is lower than 0.001, the hypothetical numerator is right, else the numerator is changed to the cold fluid temperature. The whole three heat exchangers must be calculated as the process including the heater, HTR and LTR. The process of other pre-compression cycles is similar to this flow chart. The recuperation cycle and the split expansion cycle need not consider the temperature of the cold fluid in the HTR.



Figure 9. The flow chart of the whole calculation process in the system.

4.1. Recuperation of the S-CO₂ Cycle

The cycle thermal efficiency η_t and exhaust heat recovery ratio η_{re} of the recuperation of the S-CO₂ cycle for the various compressor inlet conditions are shown in Figures 10 and 11, respectively. The cycle thermal efficiency is the ratio of net power output to cycle heat absorption. The exhaust heat recovery ratio is the ratio of net power output to the maximum allowable heat rate from the waste heat source. The turbine inlet pressure is fixed at 25 MPa. It is found that at the subcritical area where the compressor inlet pressure is lower than the critical pressure 7.38 MPa, η_t and η_{re} increase with the rising of the compressor inlet pressure. When the compressor inlet pressure is higher than the critical pressure, η_t and η_{re} increase and then decrease with the rising of the compressor inlet pressure; there is an optimum compressor inlet pressure leading to the highest η_t and η_{re} .



Figure 10. Thermal efficiency for the various compressor inlet pressures and temperatures.



Figure 11. The exhaust heat recovery ratio for the various compressor inlet pressures and temperatures.

 η_t and η_{re} decrease, whereas the optimum compressor inlet pressure increases with the rising of the compressor inlet temperature, which is caused by the special pressure leading to the great change of the density that increases with the rising of the temperature. For example, the highest η_t are 36.05%, 35.42% and 34.84%, while the compressor inlet temperatures are 32 °C, 35 °C and 38 °C, respectively. Meanwhile, the according optimum compressor inlet pressures are 7.55 MPa, 8.0 MPa and 8.4 MPa, respectively. The available heat is a fixed value which is only related to the temperature of the exhaust gas and environmental temperature, so the trend of η_{re} is same as the trend of the net work. However, the denominator of η_t is related to the cold part outlet temperature of the RCP; the trend of enthalpy in point 6 is similar to the compressor work, which will cause the maximum η_t to appear in advance. So, it is also found that the optimum compressor inlet pressure leading to the highest η_{re} . For example, η_{re} can achieve the highest of 18.12% while the compressor

Therefore, the compressor inlet pressure must be higher than the critical pressure to achieve higher η_t and η_{re} . For the ICE exhaust heat recovery, parameter η_{re} is more important than parameter η_t . So, the optimal inlet conditions are decided to achieve the highest η_{re} in this paper. When the turbine inlet pressure and temperature are fixed at 25 MPa and 500 °C, the optimal compressor inlet parameters of recuperation of the S-CO₂ cycle are 7.65 MPa and 32 °C, respectively.

inlet temperature is 32 °C and the optimum pressure is 7.65 MPa.

However, η_t and η_{re} are not only related to the compressor inlet conditions but also related to the turbine inlet conditions. Figures 12 and 13 give thermal efficiency η_t and exhaust heat recovery ratio η_{re} for various inlet pressures of the compressor and turbine. It is found that η_t and η_{re} increase while the optimal compressor inlet pressure also increases with the turbine inlet pressure, rising from 21 MPa to 29 MPa, but increases more and more slower. It is noticed that the isentropic efficiency of the turbine and compressor will decrease with the rising of pressure in actuality. Therefore, the cycle maximum pressure is limited by many factors which are not considered in this paper.



Figure 12. Thermal efficiency for the various inlet pressures of the compressor and turbine.



Figure 13. Exhaust heat recovery ratio for the various inlet pressures of the compressor and turbine.

The highest η_t , η_{re} and corresponding compressor inlet pressure for the various turbine inlet pressures are shown in Figures 14 and 15. It is shown obviously that η_t , η_{re} and the optimal compressor inlet pressure increase with the rising of the turbine inlet pressure. So, a suitable compressor inlet pressure could be selected to achieve the highest exhaust heat recovery ratio, which is higher than the critical pressure and increases with the rising of the turbine inlet pressure.



Figure 14. The optimal thermal efficiency for various turbine inlet pressures.



Figure 15. The optimal exhaust heat recovery ratio for various turbine inlet pressures.

4.2. Pre-Compression S-CO₂ Cycle

Figures 16 and 17 show the thermal efficiency η_t and the exhaust heat recovery ratio η_{re} of the pre-compression S-CO₂ cycle for various inlet pressures of the PC and MC. η_t changes between 37.88% and 38.80%, while η_{re} changes between 17.26% and 19.0%. Meanwhile, the MC/PC inlet pressures change from 7.5 MPa to 7.9 MPa and 5.6 MPa to 6.8 MPa, respectively. Both η_t and η_{re} increase and then decrease with the rising of the PC inlet pressure; there is an optimum PC inlet pressure leading to the highest η_t and η_{re} . In the calculation of the net output power, the enthalpy decided by the temperature and pressure is the important parameter. So, the net output power is determined by the expansion power in the turbine and compression power in the PC and MC. However, the changing trend of the expansion power is different from that of the compression expansion power, so there is a peak value of net output power. Meanwhile, the inlet pressure of the MC is also an important influencing factor of cycle performance, which is same as the influence of the compressor inlet pressure. The influence of the S-CO₂ cycle. The optimum PC inlet pressure is decided by the MC inlet pressure. The influence of the MC inlet pressure on η_t and η_{re} follows the results of recuperation of the S-CO₂ cycle.



Figure 16. Thermal efficiency for various inlet pressures of the PC and MC.



Figure 17. Exhaust heat recovery for various inlet pressures of the PC and MC.

The highest η_t , η_{re} and corresponding MC/PC inlet pressure for various turbine inlet pressures are shown in Figures 18 and 19. It is found that the highest η_t and η_{re} increase while the optimal MC/PC inlet pressures also increase, with the turbine inlet pressure rising from 21 MPa to 29 MPa. The highest η_t changes from 38.12% to 39.12%, while the corresponding MC/PC inlet pressures change from 7.54 MPa to 7.68 MPa and 6.05 MPa to 6.65 MPa, respectively. The highest η_{re} changes from 17.77% to 19.86%, while the corresponding MC/PC inlet pressures change from 7.66 MPa to 7.70 MPa and 5.4 MPa to 6.15 MPa, respectively. The MC/PC inlet conditions must change with the turbine inlet conditions to achieve the optimal thermodynamic performance for pre-compression of the S-CO₂ cycle.



Figure 18. Optimal thermal efficiency and corresponding MC/PC inlet pressures for various turbine inlet pressures.



Figure 19. Optimal exhaust heat recovery ratios and corresponding MC/PC inlet pressures for various turbine inlet pressures.

When the turbine inlet pressure and temperature are fixed at 25 MPa and 500 °C, the optimal MC/PC inlet pressures are 5.8 MPa and 7.68 MPa, respectively. It can lead to a maximum exhaust heat recovery ratio of 19.0%, while this is 18.12% of the recuperation of the S-CO₂ cycle.

4.3. Split-Flow Recompression S-CO₂ Cycle

For recompression of the S-CO₂ cycle, the split ratio (SR) is an important parameter which can affect the thermal efficiency η_t and exhaust heat recovery ratio η_{re} . For various cycle pressures and temperatures, the influence of the SR on η_t and η_{re} is different, but the optimal cycle pressure and temperature are consistent with the recuperation of the S-CO₂ cycle. Therefore, the following analysis is carried at the optimal pressure and temperature obtained from the above results based on the highest η_{re} .

The thermal efficiency η_t and exhaust heat recovery ratio η_{re} of the recompression of the S-CO₂ cycle for various split ratios (SR) are shown in Figure 20, where the inlet pressures of the compressor and turbine are fixed at 7.65 MPa and 25 MPa, respectively. It is found that η_t increases and then decreases with the rising of the SR, there is an optimum SR of 0.36 leading to the highest η_t . Compared to recuperation of the S-CO₂ cycle, the highest η_t increases from 36.05% to 43.16%. The results show that recompression of the S-CO₂ cycle can improve cycle thermal efficiency observably. On the contrary, the exhaust heat recovery ratio η_{re} decreases with the rising of the SR. Since split-flow recompression has negative effects on the exhaust heat recovery, it improves thermal efficiency. Therefore, split-flow recompression of the S-CO₂ cycle is not suitable to recovery of the ICE exhaust heat.



Figure 20. Thermal efficiency and exhaust heat recovery ratios for various split ratios.

Figures 21 and 22 show the thermal efficiency η_t and exhaust heat recovery ratios η_{re} for various split ratios and turbine inlet pressures. The optimal SR leading to the highest η_t decreases with the rising of the turbine inlet pressure, but the highest η_t is affected little by the turbine inlet pressure. The rising of the turbine inlet pressure contributes positively to the exhaust heat recovery ratio η_{re} , which is consistent with the results of the recuperation of the S-CO₂ cycle. The rising of the turbine inlet pressure of the enthalpy at the turbine inlet, which leads to the increase of the net output power. Meanwhile, the change trend of the net output power and heat absorbed by CO₂ both changes. So, the peak of η_t moves backwards with the decreasing of the turbine inlet pressure.



Figure 21. Thermal efficiency for various split ratios and turbine inlet pressures.



Figure 22. Exhaust heat recovery ratios for various split ratios and turbine inlet pressures.

4.4. Split-Flow Expansion S-CO₂ Cycle

The same as the recompression of the S-CO₂ cycle, the optimal cycle pressure and temperature of the split-flow expansion S-CO₂ cycle are also consistent with the recuperation of the S-CO₂ cycle. Therefore, the thermodynamic performance is analyzed based on the results obtained from the recuperation of the S-CO₂ cycle in this paper. The influence of the SR on the thermal efficiency η_t and exhaust heat recovery ratio η_{re} is shown in Figure 23.



Figure 23. Influence of the split ratio on the thermal efficiency and exhaust heat recovery ratio.

It is found that the changes of η_t and η_{re} with the SR are the same. Both η_t and η_{re} increase and then decrease with the rising of the SR; there is an optimum SR of 0.43 leading to the highest η_t and η_{re} . Compared to recuperation of the S-CO₂ cycle, the highest η_t decreases from 36.05% to 32.99%, but the highest η_{re} increases from 18.09% to 24.75%. As the same as the recompression of the S-CO₂ cycle, the SR will affect the output power of turbine 2 and the efficiency of the LTR and HTR. So, when considering heat exchange effectiveness, the calculations about the efficiency of the LTR and HTR must be checked. So, the curve of η_t and η_{re} have same trend.

Figure 24 shows the exhaust heat recovery ratios η_{re} for various split ratios and turbine inlet pressures. The effect of the SR on η_{re} for different turbine inlet pressures is the same; the η_{re} achieves a maximum while the SR is 0.43.



Figure 24. Influence of split ratios on the exhaust heat recovery ratios for various turbine inlet pressures.

4.5. Performance Comparison of Various S-CO₂ Cycle Layouts

Different S-CO₂ cycle layouts will lead to different cycle thermodynamic performances. The cycle thermal efficiency and exhaust heat recovery ratios of various S-CO₂ cycle layouts at respective optimal operation parameters are compared in Figure 25. It is shown obviously that the efficiency and exhaust heat recovery ratios of four different S-CO₂ cycles have great differences with each other. For recuperation of the S-CO₂ cycle, the highest η_t and η_{re} are 36.05% and 18.12%. For pre-compression of the S-CO₂ cycle, the highest η_t and η_{re} are 38.8% and 19.0%. Compared to recuperation of the S-CO₂ cycle, the highest η_t and η_{re} are 38.8% and 19.0%. For split-flow recompression of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16% and 18.0%. For split-flow expansion of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. Compared to recompression of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. For split-flow expansion of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. For split-flow expansion of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. For split-flow expansion of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. The split-flow expansion of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. Compared to recompression of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. Compared to recompression of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. Compared to recompression of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. Compared to recompression of the S-CO₂ cycle, the highest η_t and η_{re} are 43.16%. Compared to recompression of the S-CO₂ cycle, two turbines provide higher net output powers.



Figure 25. Thermal efficiency and exhaust heat recovery ratios for various S-CO₂ cycle layouts.

In the four S-CO₂ cycle layouts, the recompression cycle and split expansion cycle can achieve the highest thermal efficiency of 43.21% and the lowest thermal efficiency of 32.99%, respectively. However, the exhaust heat recovery ratios for various S-CO₂ cycle layouts are inconsistent with the thermal efficiency. The split expansion cycle and recuperation cycle can achieve the highest recovery ratio of 24.75% and the lowest recovery ratio of 18.09%, respectively. The results indicate that the split expansion S-CO₂ cycle is the best layout for recovery of the internal combustion engine (ICE) exhaust energy, which is inconsistent with the conclusion given by Ahn et al. [10] and Fahad et al. [13]. The reason is that the optimal layout for obtaining the maximum power from the waste heat is different from the layout for obtaining the maximum power from the high temperature heat source. It is more important to maximize the net output power than the thermal efficiency for waste heat recovery, which is proved by Mohagheghi [15].

The output power of the ICE is 235.8 kW. Combined with the ICE and waste heat recovery, the output power of the recuperation, pre-compression, split-flow recompression and expansion S-CO₂ cycles are 262.2 kW, 263.5 kW, 262.4 kW and 271.9 kW, respectively, which are shown in Figure 26. The total output power of the ICE system cycle increases 15.3% when the split expansion S-CO₂ cycle is used to recover the waste heat.



Figure 26. Total output power of the ICE and various S-CO₂ cycle layouts.

According to the comparison, the performance of the split expansion S-CO₂ cycle in waste heat recovery is the best one of the four cycles. So, the split expansion S-CO₂ cycle is chosen for future research, when those parameters which are influencing factors for the cycle, such as the SR, turbine temperature and turbine pressure, are fixed, the influence of pressure loss on the exhaust heat recovery ratio for various heat exchanger effectiveness is shown in Figure 27. The exhaust heat recovery ratio increases with the decrease of the pressure loss and the increase of the heat exchanger effectiveness. Since the pressure loss will result in flow losses in the pipeline, the heat exchanger effectiveness will result in heat losses in the heat exchanger.



Figure 27. Influence of pressure loss on the exhaust heat recovery ratio for various heat exchanger effectiveness.

The split-flow recompression S-CO₂ cycle was better in system thermal efficiency, and thermal efficiency was an important parameter which needed be improved in the power system, so there was lots of research on the split-flow recompression S-CO₂ cycle, while there was little research on the other S-CO₂ cycles. However, in ICE, not only must the thermal efficiency be considered, but the waste heat recovery ratio also must be considered. It was shown that the split-flow expansion S-CO₂

cycle was better in waste heat recovery, so the split-flow expansion S-CO₂ cycle could be considered for ICE. Even if the thermal efficiency of the split-flow expansion S-CO₂ cycle was lower than the other three cycles, it got higher output power than the other three cycles. In exchanging waste heat for output power, the split-flow expansion S-CO₂ cycle had better performance, which confirmed that it was worthwhile to study the system combining the ICE and split-flow expansion S-CO₂ cycle. However, for actual applications of ICE waste heat recovery, the complex cycle layouts will lead to high equipment costs, which may contribute negatively to the total system performance. There is also the waste heat of the ICE that is considered in this research, which will result in some heat losses in the whole ICE, that are not mentioned. So, the ICE waste heat recovery system needs further experimental research and economic analyses.

5. Conclusions

For recovering ICE waste heat effectively, four S-CO₂ cycle layouts are brought out, and their thermodynamic performances are analyzed. The following results can be concluded from this study:

- (1) For the recuperation of the S-CO₂ cycle considered in this study, there is the highest thermal efficiency and exhaust heat recovery ratio at a compressor inlet pressure which is slightly higher than the critical pressure. The optimal efficiency and corresponding compressor inlet pressure increase with the rising of the turbine inlet pressure. When the turbine inlet pressure and temperature are fixed at 25 MPa and 500 °C, the optimal compressor inlet parameters leading to a maximum exhaust heat recovery ratio of 18.12% are 7.65 MPa and 32 °C, respectively.
- (2) The MC/PC inlet pressures will change with the turbine inlet conditions to achieve the optimal thermodynamic performance of the pre-compression S-CO₂ cycle. The optimal MC/PC inlet pressures are 5.8 MPa and 7.68 MPa, respectively, which can lead to a maximum exhaust heat recovery ratio of 19.0%.
- (3) For the split-flow recompression S-CO₂ cycle, thermal efficiency increases and then decreases with the rising of the SR; there is an optimum SR of 0.36 leading to the maximum thermal efficiency of 43.16%. On the contrary, the exhaust heat recovery ratio decreases with the rising of the SR, which indicates that the split-flow recompression S-CO₂ cycle is not suitable for ICE waste heat recovery.
- (4) Both the thermal efficiency and exhaust heat recovery ratio increase and then decrease with the rising of the SR for the split expansion S-CO₂ cycle; there is an optimum SR of 0.43. Compared to recuperation of the S-CO₂ cycle, the maximum highest thermal efficiency decreases from 36.05% to 32.99%, but the maximum exhaust heat recovery ratio increases from 18.09% to 24.75%. Among the four layouts considered in this study, the split expansion S-CO₂ cycle can achieve the highest performance for ICE waste heat recovery, while the total output power can increase 15.3%.

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Abbreviations

Nomenclature	
Т	Temperature (°C)
9	Mass flow rate (kg/h)
W	Power (kw)
h	Enthalpy (kJ/kg)

Greek letters	
η	Efficiency
ε	Effectiveness of recuperator
φ	Amount of transferred heat
subscripts	
g,out	Exhaust gas at the outlet of Heater
1–10	Inlet and outlet of apparatus in the cycle
0	Exhaust gas at the environment temperature
<i>S</i> , <i>T</i>	Turbine isentropic efficiency
S,C	Compressor isentropic efficiency
mco2	Mass flow rate of CO ₂
g,in	Exhaust gas at the inlet of Heater
mg	Mass flow rate of exhaust gas
t	Thermal
re	Waste heat recovery
2 s, 5 s	Ideal state of working fluid at points 2 and 5
Abbreviations	
ICE	Internal combustion engine
S-CO ₂	Supercritical Carbon Dioxide
SR	Split ratio
RCP	Recuperator
ТВ	Turbine
СР	Compressor
С	Cooler
HTR	High temperature recuperator
LTR	Low temperature recuperator
МС	Main compressor
PC	Pre-compressor
RC	Re-compressor

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