Optimal Design of a Distillation System for the Flexible Polygeneration of Dimethyl Ether and Methanol Under Uncertainty



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All images and source material are from the following work:

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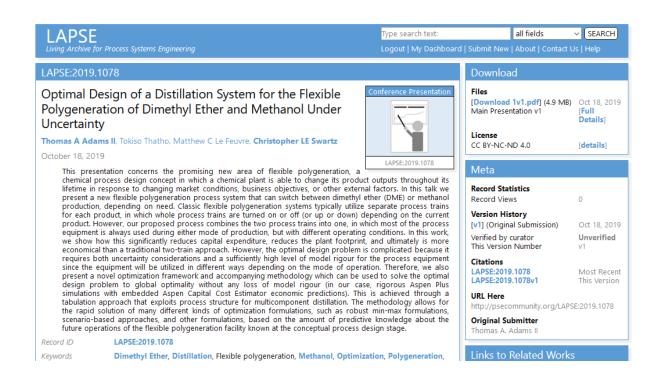
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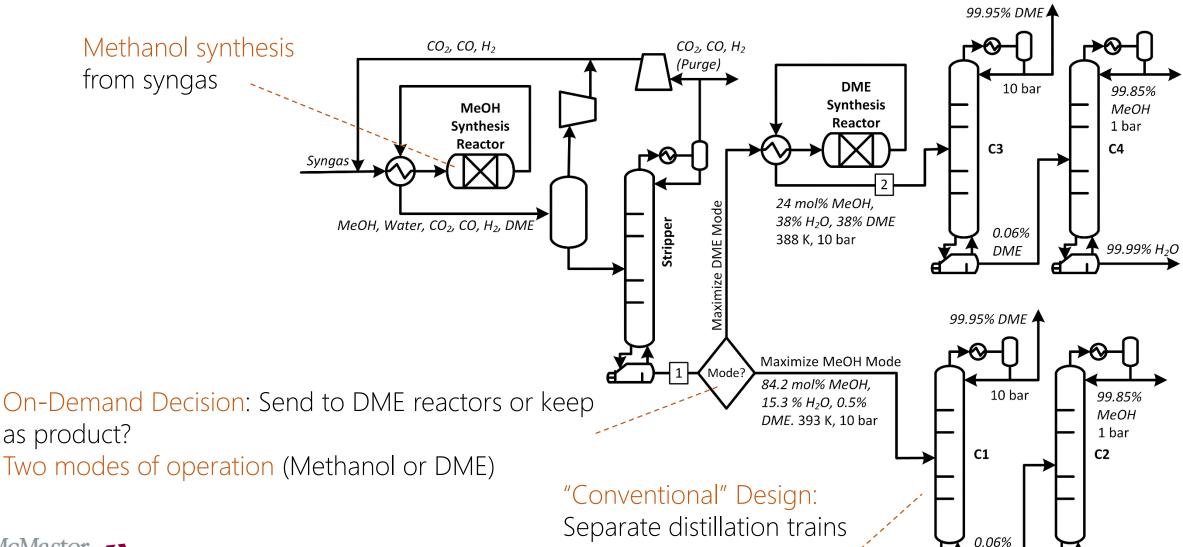
- Links to articles cited in the study
- Links to data sets and simulations used in cited studies







Basic Premise: Flexible Production



optimized to each mode

99.99% H₂O



Design Under Uncertainty

- Operating policy: Operators will choose either DME or Methanol Mode depending on prevailing market conditions at that time.
- Uncertainty: Can only guess during the design phase what that proportion will be.
- Design Implications: If you think you will spend most of your time in Methanol Mode:
 - Invest in more capital to ensure lower operating costs for the Methanol section
 - Want less efficient DME section to save capital, since high energy costs will be brief



Optimization Strategy (Naïve Approach)

Decision variables are number of stages above and below feed for each column.

$$TAC_{BaseCase,Exp} = \sum_{c=c_{1..c_4}} Z_c$$

$$Z_c = \min_{N_{A,c}, N_{B,c}} TAC_{c,Exp}$$

s.t. $TAC_{c,Exp} = a_f TDC_c + AOC_{c,Exp}$

Minimize TAC of each column separately. Because each column must meet a design spec by definition, they can be split into the sum of four minimization problems.

Surface area of condenser / reboiler for column c

$$AOC_{c,Exp} = h(Q_{H,c}U_{H,c} + Q_{C,c}U_{C,c})(1 - \phi_{Exp,D})(1 - \delta_{c}) + h(Q_{H,c}U_{H,c} + Q_{C,c}U_{C,c})(\phi_{Exp,D})\delta_{c}$$

$$\delta_{c} = \begin{cases} 0 \text{ for } c = C1, C2 \text{ (MeOH Mode)} \\ 1 \text{ for } c = C3, C4 \text{ (DME mode)} \end{cases}$$

 $TDC_c = f_1(A_{C,c}) + f_2(A_{H,c}) + f_3(N_{A,c} + N_{B,c}, D_c)$

Key uncertainty parameter. The amount of time we expect to operate in DME mode over the 15 year life time.

Diameter of column c

$$A_{C,c} = f_{4,c}(N_{A,c}, N_{B,c})$$

 $A_{H,c} = f_{5,c}(N_{A,c}, N_{B,c})$

Capital cost models (can be equations or table lookups)

Reboiler/condenser duties of $Q_{H,c} = f_{7,c}(N_{A,c}, N_{B,c})$ column c

$$D_c = f_{6,c}(N_{A,c}, N_{B,c})$$

$$Q_{H,c} = f_{7,c}(N_{A,c}, N_{B,c})$$

$$Q_{C,c} = f_{8,c}(N_{A,c}, N_{B,c})$$

All of these can be exhaustively pre-tabulated with rigorous models in Aspen Plus. Implemented as table lookup.

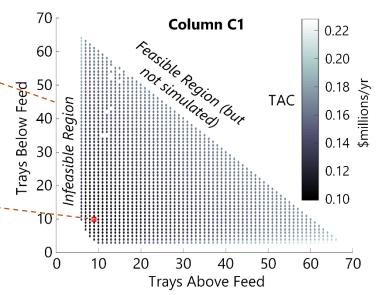
Solve quickly through exhaustive search

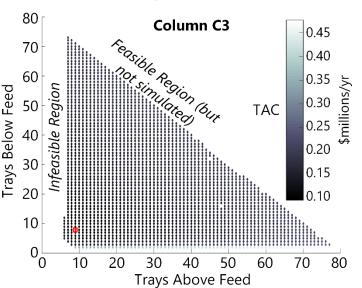
Easy to identify infeasible regions.

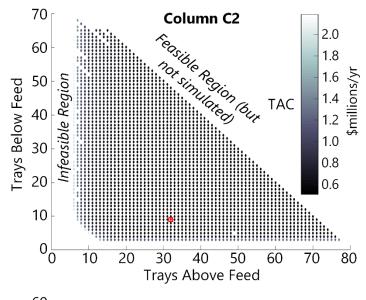
Minimum EXPECTED TAC for each column can be chosen by exhaustive search.

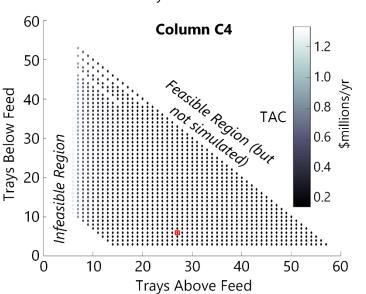
This example is for $\phi_{EXP, D} = 0.5$

Different optimums for different values of $\phi_{\text{EXP.D}}$





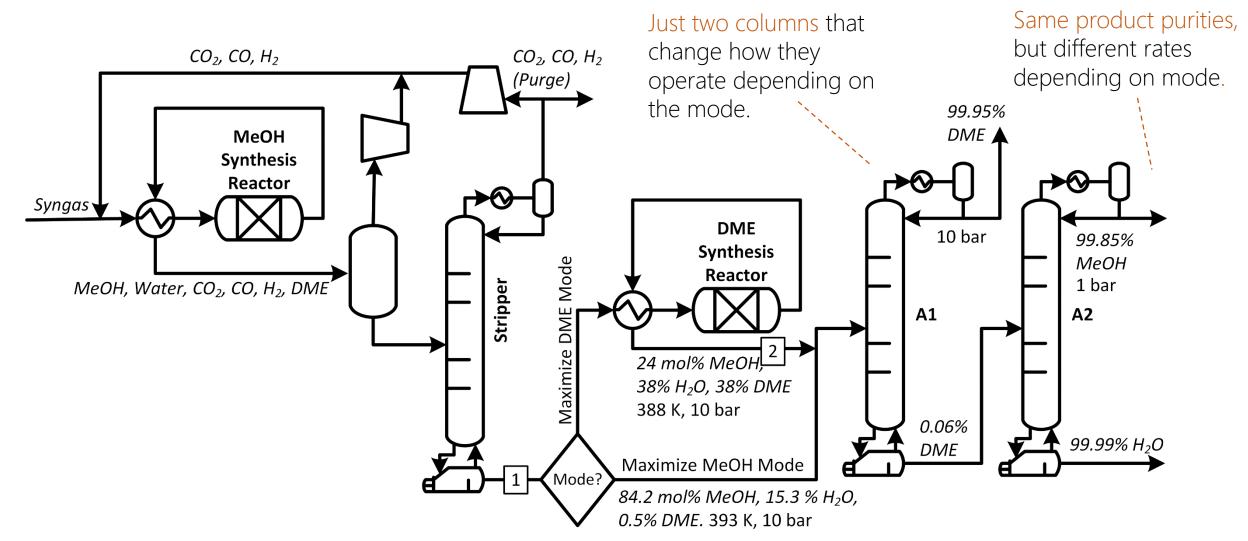








Alternative Design Strategy



Very quick optimization, trivial extra work

Only 4 decision variables

instead of 8.

$$TAC_{CaseA,Exp} = \sum_{c=A1,A2} Z_{c}$$

$$Z_{c} = \min_{N_{A,c}, N_{B,c}} TAC_{c,Exp} \qquad \text{Still have the uncertainty factor.}$$

$$s.t. \quad TAC_{c,Exp} = a_{f}TDC_{c} + AOC_{c,Exp}$$

$$AOC_{c,Exp} = h(Q_{H,c,MeOH}U_{H,c} + Q_{C,c,MeOH}U_{C,c})(1 - \phi_{Exp,D}) + h(Q_{H,c,DME}U_{H,c} + Q_{C,c,DME},U_{C,c})(\phi_{Exp,D})$$

$$TDC_{c} = f_{1}(A_{C,c}) + f_{2}(A_{H,c}) + f_{3}(N_{A,c} + N_{B,c}, D_{c})$$

$$A_{C,c} = \begin{cases} \max_{A,C_{1}} f_{4,C_{1}}(N_{A,c}, N_{B,c}), f_{4,C_{3}}(N_{A,c}, N_{B,c}) \end{bmatrix} for c = A1 \\ \max_{A,C_{2}} f_{4,C_{2}}(N_{A,c}, N_{B,c}), f_{4,C_{3}}(N_{A,c}, N_{B,c}) \end{bmatrix} for c = A2$$

The max function ensures that the equipment is large enough to handle both modes.

$$A_{H,c} = \begin{cases} \max[f_{5,C1}(N_{A,c}, N_{B,c}), f_{5,C3}(N_{A,c}, N_{B,c})] & for \ c = A1 \\ \max[f_{5,C2}(N_{A,c}, N_{B,c}), f_{5,C4}(N_{A,c}, N_{B,c})] & for \ c = A2 \end{cases}$$

$$D_{c} = \begin{cases} \max[f_{6,C1}(N_{A,c}, N_{B,c}), f_{6,C3}(N_{A,c}, N_{B,c})] & for \ c = A1 \\ \max[f_{6,C2}(N_{A,c}, N_{B,c}), f_{6,C4}(N_{A,c}, N_{B,c})] & for \ c = A2 \end{cases}$$

$$Q_{H,c,MeOH} = \begin{cases} f_{7,C1}(N_{A,c}, N_{B,c}) & for \ c = A1 \\ f_{7,C2}(N_{A,c}, N_{B,c}) & for \ c = A2 \end{cases}$$

$$Q_{H,c,DME} = \begin{cases} f_{7,C3}(N_{A,c}, N_{B,c}) & for \ c = A2 \\ f_{7,C4}(N_{A,c}, N_{B,c}) & for \ c = A2 \end{cases}$$

$$Q_{C,c,MeOH} = \begin{cases} f_{8,C1}(N_{A,c}, N_{B,c}) & for \ c = A2 \\ f_{8,C2}(N_{A,c}, N_{B,c}) & for \ c = A2 \end{cases}$$

Can reuse the tabulated data from the Aspen Plus simulations without needing to rerun.



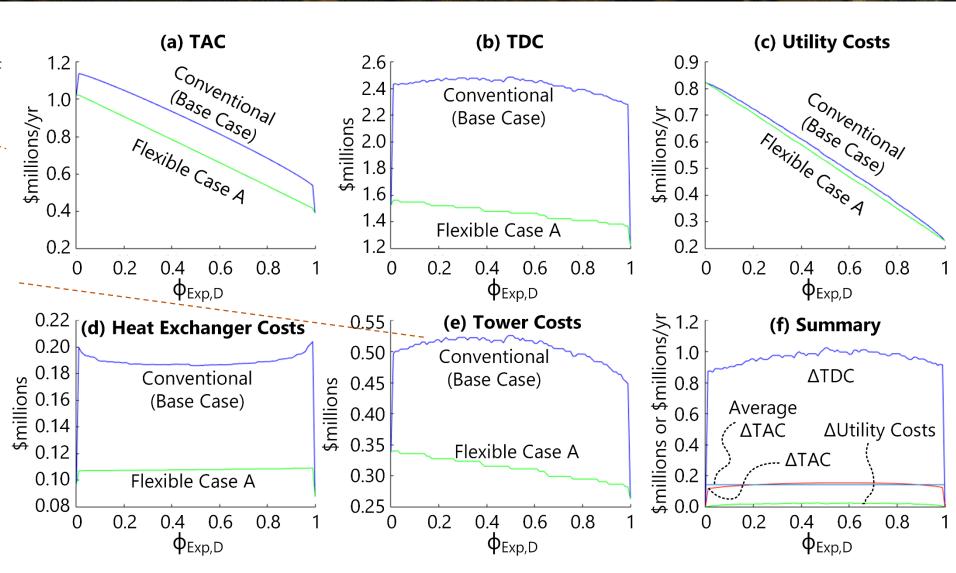
Quantify the Value of Flexibility.

Basically, my EXPECTED TAC is about 20% lower if I am flexible, regardless of what I expect.

"Noise" in equipment costs is expected and due to the impact of discrete decisions (# stages, discrete column diameters).

These are globally optimal.

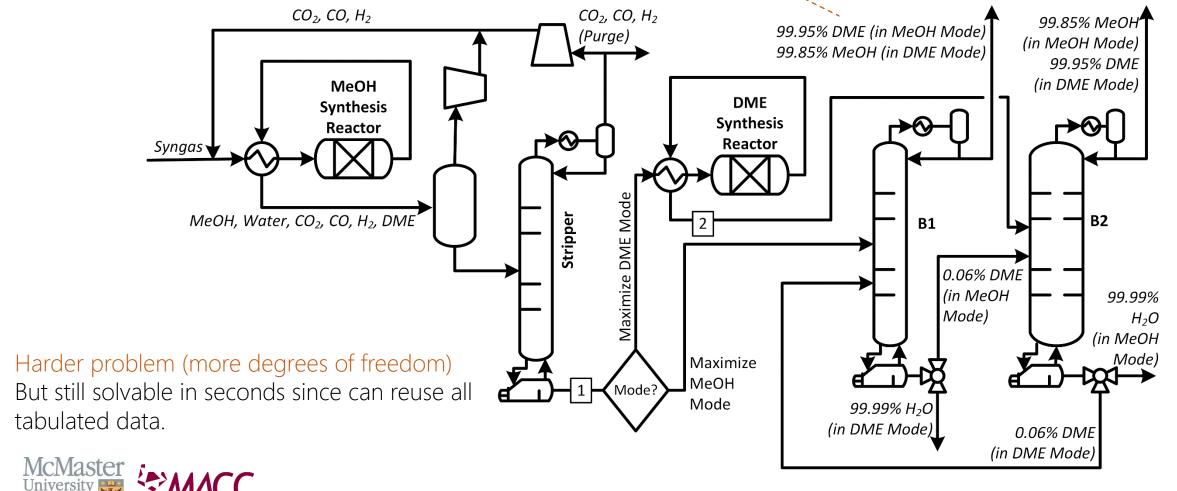




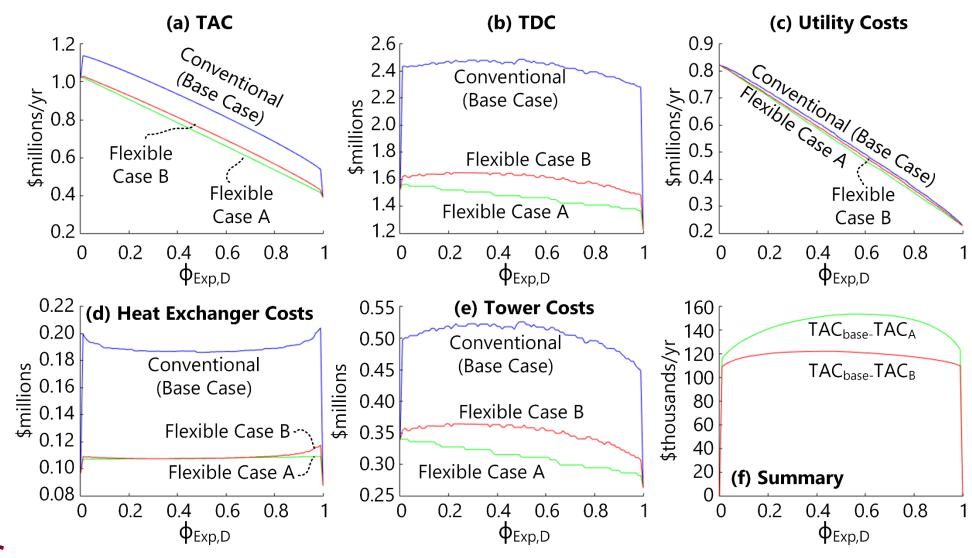
Option B: "Fat / Skinny" columns

The column receiving the product feed, and the feed location changes with the mode.

Maybe I can save money by having one column for large loads and one column for small loads.

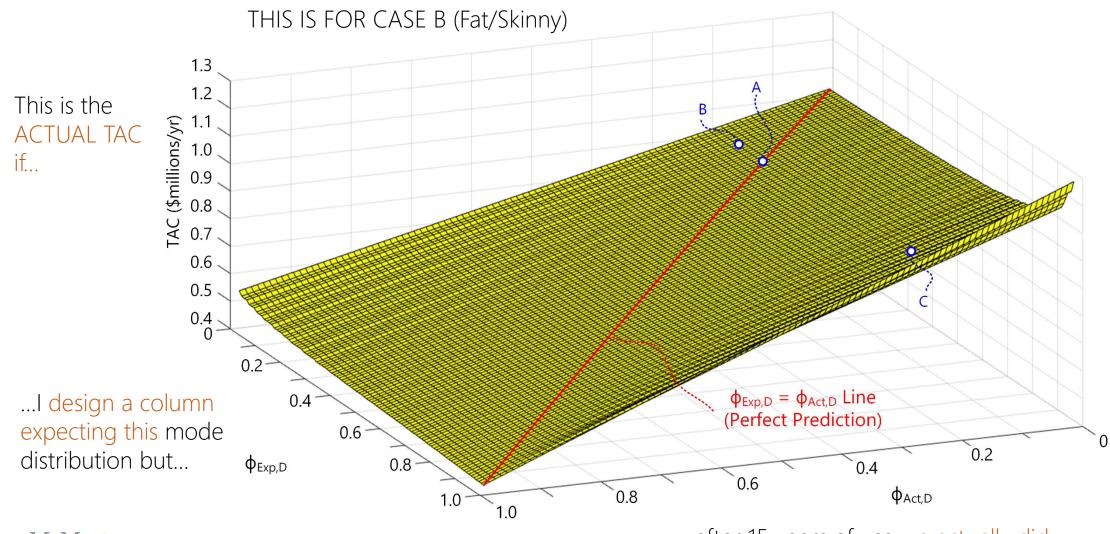


Well, ok, not as good.





Ok, but what if my predictions are wrong?



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...after 15 years of use we actually did
this.

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Design Under Uncertainty Options

Probability Distribution Functions

Find the design that minimizes Expected TAC

$$TAC_{CaseB,Exp} = \sum_{c=B1,B2} Z_c$$

$$Z_{c} = \min_{N_{A,c,MeOH}, N_{B,c,MeOH}N_{A,c,DME}} \sum_{i=1}^{i=S} P(\phi_{Exp,D,i}) TAC_{c,Exp,i}(\phi_{Exp,D,i})$$

Robust (Min Max) Formulation

Find the design that minimizes the worst case TAC of any outcome

$$TAC_{CaseB,Exp} = \sum_{c=B1,B2} Z_c$$

$$Z_c = \min_{N_{A,c,MeOH}, N_{B,c,MeOH}N_{A,c,DME}} \max_{i=1..S} TAC_{c,Exp,i}(\phi_{Exp,D,i})$$

Example: Normal distribution around a guessed $\phi_{\text{EXP, D}}$

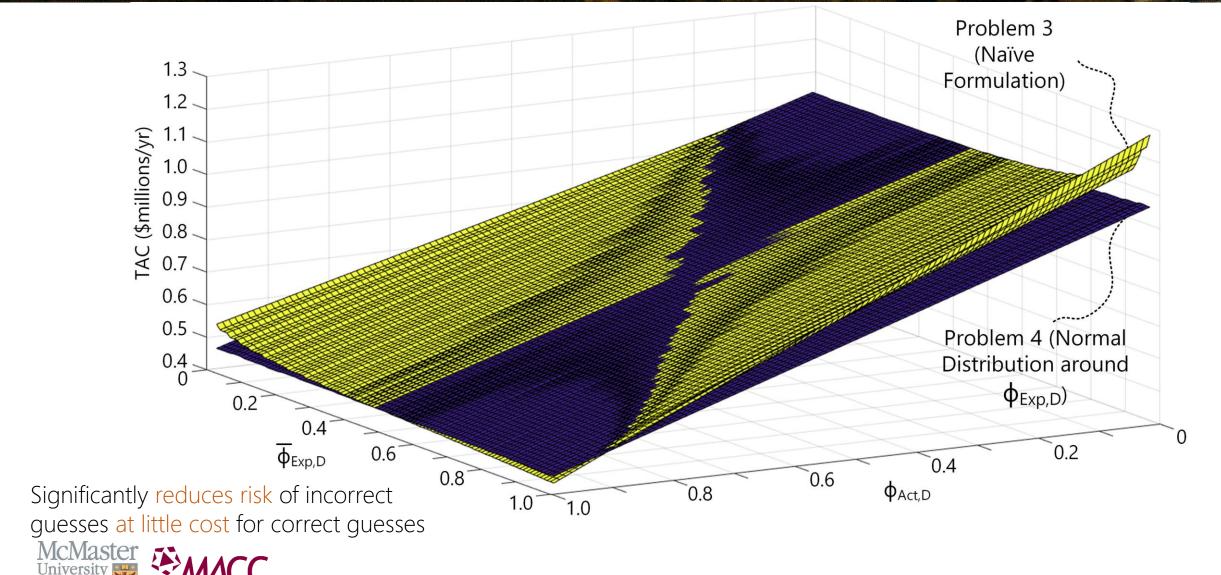
Example: Uniform distribution of $\phi_{EXP, D}$ (i.e. no predictive knowledge at all).

Example: Also useful with no predictive knowledge at all.

All of these can be solved to global optimality with no loss of fidelity in a few seconds.

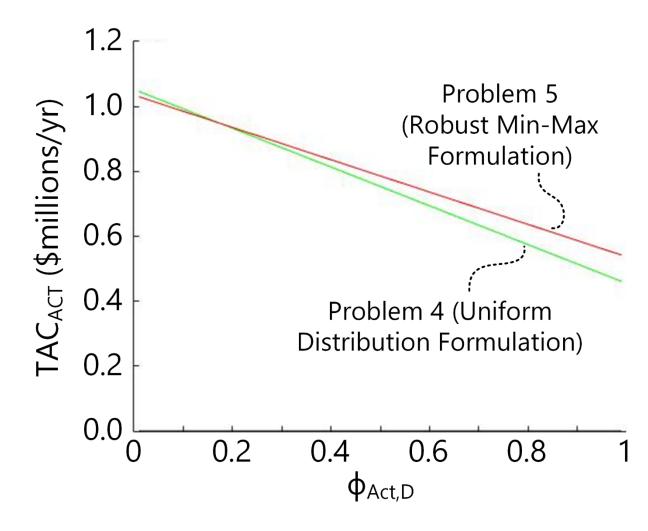


Uncertainty formulation comparison



Design Under Uncertainty with No Predictions

- Both methods result in a single design without making assumptions.
- This is the Actual TAC depending on the outcome.
- Neither is better in all cases, but uniform distribution happens to be better more often.
- Both are very good





Conclusions

- Strategic tabulation and problem decoupling makes for very fast optimal design under uncertainty solutions with many scenarios to global optimality
- Can re-use design tables for many case studies
- Uniform distribution recommended (requires no knowledge of the final outcomes) to minimize overall risk at little cost

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