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Article

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Abstract: A novel modular arc-linear flux-switching permanent-magnet motor (MAL-FSPM) used for scanning system instead of reduction gearboxes and kinematic mechanisms is proposed and researched in this paper by the finite element method (FEM). The MAL-FSPM combines characteristics of flux-switching permanent-magnet motor and linear motor and can realize the direct driving and limited angular movement. Structure and operation principle of the MAL-FSPM are analyzed. Cogging torque model of the MAL-FSPM is established. The characteristics of cogging torque and torque ripple are investigated for: (1) distance (d_{end}) between left end of rotor and left end of stator is more than two rotor tooth pitch (τ_p); and (2) d_{end} is less than two rotor tooth pitch. Cogging torque is an important component of torque ripple and the period ratio of the cogging torque to the back electromotive force (EMF) equals one for the MAL-FSPM before optimization. In order to reduce the torque ripple as much as possible and affect the back EMF as little as possible, influence of period ratio of cogging torque to back EMF on rotor step skewing is investigated. Rotor tooth width and stator slot open width are optimized to increase the period ratio of cogging torque to back EMF. After the optimization, torque ripple is decreased by 79.8% for $d_{\text{end}} > \tau_p$ and torque ripple is decreased by 49.7% for $d_{\text{end}} < \tau_p$. Finally, 3D FEM model is established to verify the 2D results.

Keywords: modular arc-linear flux-switching permanent-magnet motor (MAL-FSPM); cogging torque; torque ripple; harmonics; period ratio of cogging torque to back electromotive force (EMF); rotor step skewing; finite element method (FEM)

1. Introduction

With the rapid development of society and economy, higher requirements are put forward for energy use, which include being more reliable, flexible, and efficient; adaptive to various actual application situations; *etc.* Electric energy is one preferable form of energy in daily life and industrial production. Electric energy can be transferred into other forms of energy, such as thermal energy, optical energy, mechanical energy, *etc.* As is well known, electromechanical systems play the role as a bridge link for energy conversion between electric energy and mechanical energy, and most of the total electric energy is consumed by electromechanical systems [1–4]. Therefore, improving efficiency of whole electromechanical system is meaningful for energy conversion.

As for an electromechanical system, the actuator is an important factor to influence efficiency of the whole electromechanical system. Since permanent-magnet synchronous motor (PMSM) has advantages of high efficiency, high power density and high power factor, it can be a favorable actuator in the electromechanical system. In [5], two brushless DC motors are used to actuate each of two revolute joints of two degrees of robotic manipulator. In [6], an axial flux permanent-magnet (AFPM) machine

is designed for robot joint module. On the other hand, the complexity of electromechanical system, decided by the application domains, also influences the efficiency of the whole electromechanical system. In many applications, such as antenna scanning system, satellite scan mirror system, robot joint, *etc.*, the driven objects only rotate back and forth within a limited angle range. In traditional implementation system, rotating electric machines plus reduction gearboxes are usually adopted to convert the rotating motion to linear motion where necessary [6–8]. The complex mechanical structure certainly increases power consumption. However, direct drive servomotor can avoid the complex mechanical structure. Figure 1 shows one simple example of Galileo Sphere robot [9]. The arc-linear motor can directly drive the load to operate back and forth within a limited angle range that is less than 180° (mechanical angle), which saves space and power consumption and improves the performance of the whole robot.

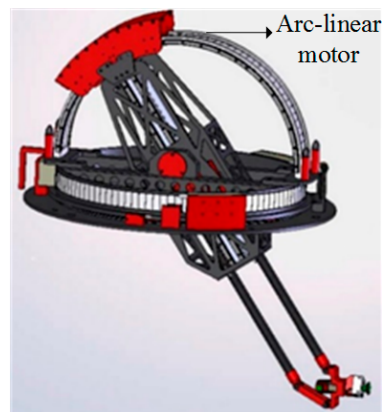


Figure 1. Galileo sphere robot.

Instead of rotating motor plus reduction gearboxes, arc-linear permanent-magnet synchronous motor (AL-PMSM) is a good candidate as the drive motor directly connecting the load for these aforementioned applications such as antenna scanning system, satellite scan mirror system and robot. It can also satisfy the requirements of high positioning accuracy and high response performance for these applications. Moreover, the direct drive motor can reduce the additional losses, reduce the backlash, and increase the reliability of the system. The arc-linear motors are researched and usually adopt the mover structure with surface-mounted permanent magnets (PMs) [9,10]. However, this kind of AL-PMSM has a limited length of stator structure and PMs are mounted on the whole rotor. Thus, only small parts of PMs are effective during the operation and the PMs that do not produce effective magnetic field may cause electromagnetic interference to peripheral devices. Therefore, this kind of AL-PMSM cannot make full use of the PMs and increases the PMs cost. In recent years, flux reverse permanent-magnet machine (FRPM), double salient permanent-magnet machine (DSPM) and flux-switching permanent-magnet machine (FSPM) have been widely investigated due to the advantages of simple and robust rotor structure that is composed of cheap iron core with salient tooth [11–15]. Since the armature windings and the permanent magnets are both installed in the stator of these structures, they can protect the PMs from sliding off caused by centrifugal force and from demagnetizing caused by the heat dissipation difficulties. Compared with the DSPM and the FRPM, the FSPMs have the performances of high power density and sinusoidal back electromotive force (EMF) [11,16,17]. Therefore, this paper researches a novel modular arc-linear flux-switching permanent-magnet motor (MAL-FSPM), which can integrate the merits of high power density and low manufacturing cost, and avoid electromagnetic interference to peripheral devices, as shown in Figure 2. The MAL-FSPM can be applied in robot fields, radar scanning systems, and so on.

However, due to the inherent double salient effect in the FSPM, torque ripple of the FSPM is relatively high [18–20], which is unexpected for a direct driving motor. Because the PMs are located

in the stator, slots skewing method, magnet segmentation method and optimization of the pole arc coefficient may be ineffective for the FSPM. Therefore, it is good and convenient to optimize the rotor. For the cogging torque and torque ripple reduction of the FSPM, Reference [20] verifies that rotor tooth with odd number has lower cogging torque compared with the rotor tooth with even number; multi-tooth structure can reduce the cogging torque and torque ripple [21,22]; and rotor tooth shapes combined with stepped and notched technology can greatly reduce the cogging torque [23–25]. However, these methods may not be all effective for special structure motor, such as the modular motor. Due to the simple rotor structure, rotor skewing technology is an effective and easy way to reduce torque ripple. Detent force of the flux-switching linear motor is greatly reduced by using the skewing technology [26]. Torque ripple of 12/10 stator/rotor pole and 12/14 stator/rotor pole flux-switching machine topology is effectively reduced based on the rotor step skewing [27]. However, the period ratio of cogging torque to the back EMF is ≥ 3 in [26,27]. This paper mainly researches torque ripple reduction for modular motor and arc-linear motor, especially for that period ratio of cogging torque to the back EMF equals one.

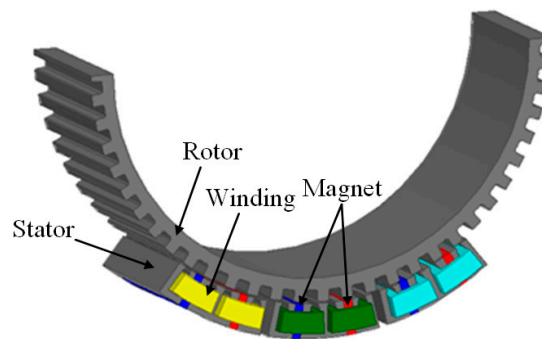


Figure 2. The 3D structure of the arc-linear permanent-magnet motor (AL-PMSM).

A novel MAL-FSPM, which can directly drive the load to rotate back and force within a limited angle range, is proposed and researched in this paper. In Section 2, structure and operation principle of the MAL-FSPM are introduced. In Section 3, cogging torque model is established and characteristics of torque ripple are analyzed. In Section 4, influence of period ratio of cogging torque to back EMF on the rotor step skewing is investigated. In Section 5, in order to increase the period ratio of cogging torque to back EMF, first harmonic and second harmonic of cogging torque are dramatically reduced by the optimization of rotor tooth width and stator slot open width. In Section 6, 3D finite element method (FEM) model is established to verify the 2D results.

2. Structure and Operation Principle of the Modular Arc-Linear Flux-Switching Permanent-Magnet Motor

2.1. Structure of the Modular Arc-Linear Flux-Switching Permanent-Magnet Motor

The MAL-FSPM includes one arc stator and one arc rotor. Rotor is laminated by the steel sheet and the rotor arc radian (θ_{rotor}) is 180° (mechanical degree). Stator arc radian (θ_{stator}) is 76° (mechanical degree). Thus, the scanning range is $\pm 52^\circ$ (mechanical degree), which is decided by the following Equation (1):

$$\theta_L = \theta_R = (\theta_{\text{rotor}} - \theta_{\text{stator}})/2 \quad (1)$$

The effective operating electromagnetic part is a 12-slots/13-poles structure, as shown in Figure 3a. Stator structure of the MAL-FSPM is more complex than rotor structure. The stator consists of three modules, representing Phases A, B and C in the counter-clockwise direction, respectively. Single layer and concentrated windings are placed in each stator slot. Furthermore, each phase windings are connected in series, as shown in Figure 3b. Each module consists of one “E” type iron core, two “U”

type iron cores and two PMs. The PMs are inserted between “E” type iron core and “U” type iron core. Magnetization direction of the adjacent PMs is opposite in the circumference direction. Furthermore, the non-magnetic material is placed between adjacent modules to obtain balanced three-phase back EMF and to reduce the interaction of the three phase windings. The d_{end} is represented the distance between left end of stator and left end of rotor.

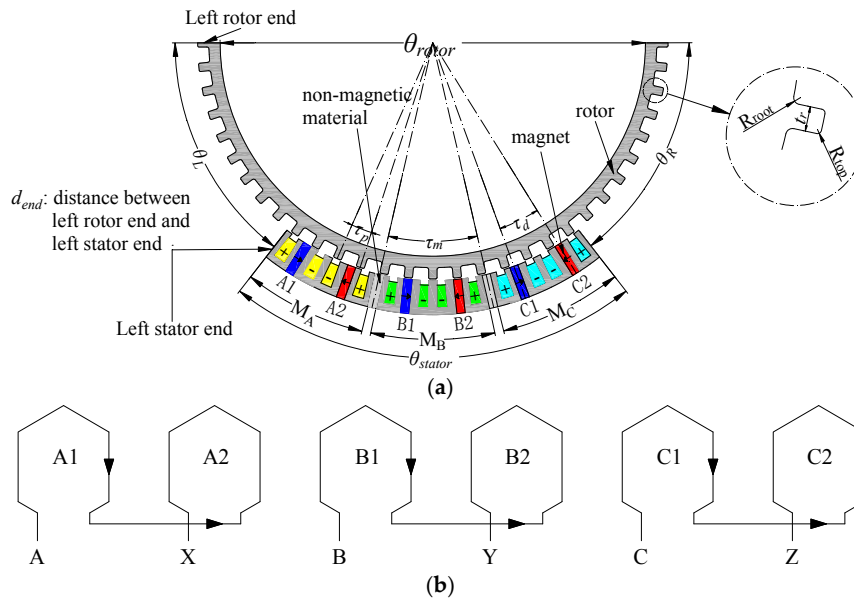


Figure 3. (a) The structure of the modular arc-linear flux-switching permanent-magnet motor (MAL-FSPM); and (b) connection form of each phase windings.

As for the FSPM, the period of back EMF is one rotor pole pitch [16–18]. Therefore, one rotor pole pitch of the MAL-FSPM can be equivalent to 360° (electrical angle), which is also the period of the magnetic field. Consequently, the electrical frequency of the back EMF can be determined by the following Equations (2) and (3):

$$\omega_r = 2\pi \times \frac{n}{60} \tag{2}$$

$$\frac{1}{f} = \frac{\pi}{180} \times \tau_p \times \frac{1}{\omega_r} = \frac{\tau_p}{6n} \tag{3}$$

where τ_p is rotor tooth pitch (distance between two adjacent rotor tooth) and its unit is degree ($^\circ$); n is rotation speed of rotor and its unit is revolutions per minute (r/min); ω_r is angular speed and its unit is radian per second (rad/s); and f is the electrical frequency.

In order to realize maximum back EMF of each phase winding and to obtain balanced three-phase back EMF, the geometric dimension of each module is supposed to be carefully designed. The τ_d , τ_m and τ_p , which are measured in the mechanical angle, should meet the following Equations (4) and (5). Because the period of magnetic field is one rotor pole pitch, Equation (4) can make the phase angle of back EMFs for different coils that belong to the same phase winding be cophase or antiphase. Equation (5) can make the phase difference of back EMFs between different phase windings be 120° (electrical degree). It is worth noting that phase angle of conductors for each coil is antiphase.

$$\tau_d = (i + 1/2^k) \times \tau_p \tag{4}$$

$$\tau_m = (j + 2^k/3) \times \tau_p \tag{5}$$

where the value of k is 0 or 1, i and j are both nonnegative integers, τ_d is the distance between two PMs in each module, and τ_m is the distance between two adjacent modules.

Since the MAL-FSPM has different type of iron cores, Equations (4) and (5) can be easily satisfied under careful design. Main dimension parameters of each module are shown in the Table 1. Based on the Table 1, the FEM model is established in the software of ANSYS Maxwell as shown in Figure 4a. For the convenience of modeling, slot insulation and conductor insulation are neglected; windings placed in slot are depicted as one conductor and the conductor is set with type of Stranded in the FEM model. Non-magnetic material is set as air and boundary condition of Vector Potential (0 Wb/m) is adopted in the FEM model. Boundary condition is labeled with red circle in Figure 4a. Based on the FEM model, back EMF of the MAL-FSPM is shown as Figure 4b. In Figure 4b, the d_{end} is represented distance between left end of rotor and left end of stator, as shown in Figure 3a; $2\tau_p > d_{\text{end}} > 0$ is represented that distance between left end of rotor and left end of stator is less than two rotor tooth pitch; $d_{\text{end}} > 2\tau_p$ is represented that distance between left end of rotor and left end of stator is more than two rotor tooth pitch. It can be seen that back EMF of $2\tau_p > d_{\text{end}} > 0$ is in agreement with back EMF of $d_{\text{end}} > 2\tau_p$. Due to good structure of the MAL-FSPM, three-phase back EMF is well balanced during the whole operation.

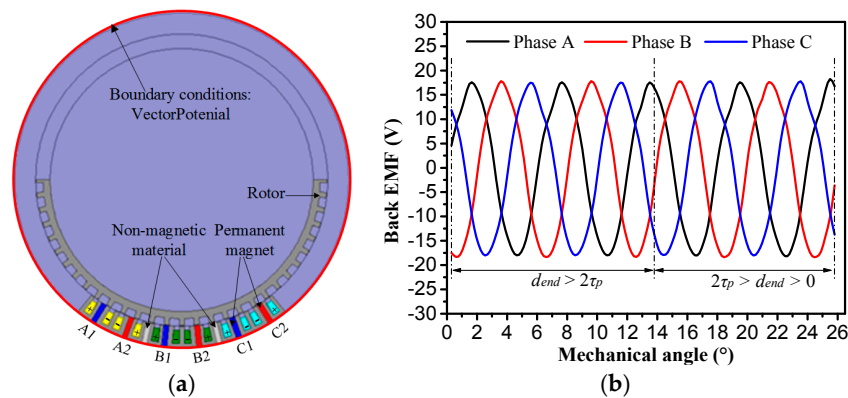


Figure 4. (a) Finite element method (FEM) model of the MAL-FSPM; and (b) back electromotive force (EMF) of the MAL-FSPM.

Table 1. Main dimension parameters of each module.

Parameters	Values	Parameters	Values
Rotor tooth height (mm)	5	Each module width (°)	24
Motor length (mm)	65	Non-magnetic material width (°)	2
Stator outer diameter (mm)	240	Slot width t_s (°)	2
Air-gap length (mm)	0.75	Tooth width of "U" type (°)	1.5
Rotor tooth width t_r (°)	2	Tooth width of "E" type (°)	2
Rotor tooth pitch τ_p (°)	6	Phase number	3
Magnet thickness t_{PM} (°)	2	Rated speed (r/min)	100
Magnet height (mm)	15	Amplitude of rated current (A)	2.26
Chamfering radius R_{top} (mm)	0.6	Chamfering radius R_{root} (mm)	1

2.2. Operation Principle of the Modular Arc-Linear Flux-Switching Permanent-Magnet Motor

When rotor is at the different position of θ_1 , θ_2 , θ_3 and θ_4 , the no-load magnetic field distributions of module M_B obtained by the FEM are shown in Figure 5a–d, respectively; the flux linkage waveforms of phase B, coil B_1 and coil B_2 are shown in Figure 6a. According to Figure 5, the flux linkage direction of coil B_1 in the module M_B is from the stator to the rotor, while the flux linkage direction of coil B_2 is from the rotor to the stator. According to Figures 5 and 6 flux linkage directions of the coil B_1 and coil B_2 remain unchanged during the operation of rotor, so flux linkages of coil B_1 and coil B_2 are both unipolar. On the other hand, the changing trend of flux linkage for coil B_1 and coil B_2 is the same, and either maximum flux linkage or minimum flux linkage can be achieved simultaneously for coil B_1

and coil B₂. Due to phase B formed by the series connection of coil B₁ and coil B₂, θ_1 and θ_3 are the switching positions of polarity for phase B. Then, it can be found that flux linkage of phase B is zero at the position of θ_1 and θ_3 , flux linkage of phase B reaches the negative extreme value at the position θ_2 , and flux linkage of phase B reaches positive extreme value at the position θ_4 . Therefore, flux linkage of phase B is bipolar, which is the principle of flux switching. In corresponding to the flux linkage of phase B, back EMF waveform can be deduced by Faraday's law of electromagnetic induction, as shown in Figure 6b. When the current fed in the coils is cophasal with back EMF as shown in Figure 6b, continuous and stable electromagnetic torque can be produced.

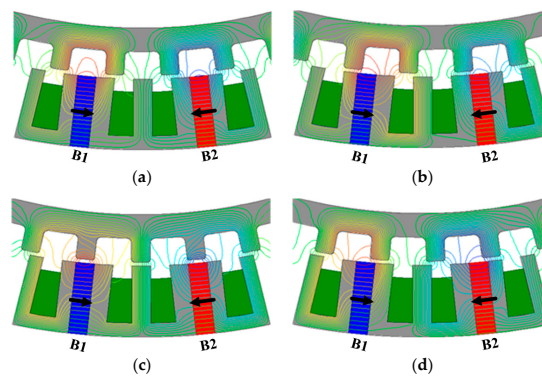


Figure 5. The non-load magnetic field distribution of the module M_B for: (a) position θ_1 ; (b) position θ_2 ; (c) position θ_3 ; and (d) position θ_4 .

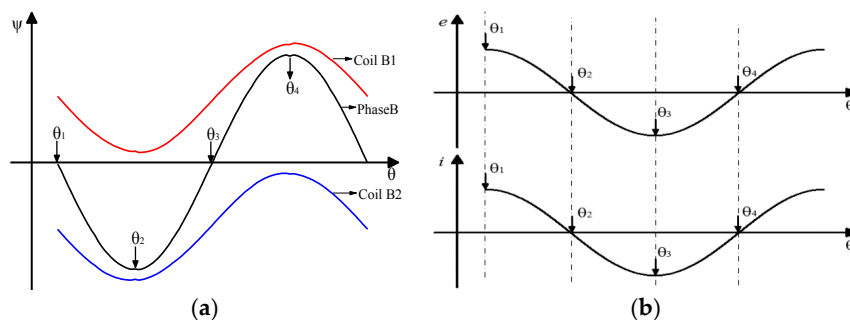


Figure 6. (a) Flux linkage waveforms of coil B1, coil B2 and phase B; and (b) back EMF and current waveforms (from top to bottom).

3. Analysis of the Cogging Torque Characteristics

3.1. Cogging Torque of the Modular Arc-Linear Flux-Switching Permanent-Magnet Motor

Cogging torque of the MAL-FSPM includes two parts: slot torque and end torque. The slot torque is caused by the double salient structure of the MAL-FSPM. Similar to the linear motor, the end torque is caused by the limited length of stator. Furthermore, cogging torque can be deduced by energy method, as shown in Equation (6):

$$T_{\text{cog}}(\alpha) = -\frac{\partial W(\alpha)}{\partial \alpha} = -\left(\frac{\partial W_{\text{slot}}(\alpha)}{\partial \alpha} + \frac{\partial W_{\text{end}}(\alpha)}{\partial \alpha}\right) \quad (6)$$

where α is the position of rotor, W is the whole field energy, W_{slot} is the field energy stored in the slot part, and W_{end} is the field energy stored in the stator end part.

The end torque is generated by the limited length of stator. Furthermore, field distribution of left stator end core and right stator end core changes periodically with one rotor tooth pitch. Therefore, the end torque can be expressed by the Fourier series as follows:

$$T_{\text{end}} = \sum_{\nu=1}^{\infty} T_{L,\nu} \sin(k \times \frac{2\pi}{\tau_p} \times \alpha + \gamma_{\nu}) + \sum_{k=1}^{\infty} T_{R,\nu} \sin(k \times \frac{2\pi}{\tau_p} \times \alpha + \beta_{\nu}) \quad (7)$$

where $T_{L,\nu}$ and γ_{ν} are the ν^{th} harmonic amplitude and phase angle of the left end torque, respectively; and $T_{R,\nu}$ and β_{ν} are the ν^{th} harmonic amplitude and phase angle of the right end torque, respectively.

Considering that each of the stator models is independent from the others, the slot torque can be synthesized by the sum of all stator modules. As for each stator module, the field distribution also changes periodically with one rotor tooth pitch, so the slot torque of each stator module can be expressed by the Fourier series as follows:

$$T_{\text{slot},i} = \sum_{\nu=1}^{\infty} T_{\text{slot},i,\nu} \sin(k \times \frac{2\pi}{\tau_p} \times \alpha + \varphi_{i,\nu}) \quad (8)$$

where $T_{\text{slot},i,\nu}$ and $\varphi_{i,\nu}$ are the ν^{th} harmonic amplitude and phase angle of the i^{th} module, respectively.

The slot torque can be expressed as follows:

$$T_{\text{slot}} = \sum_{i=1}^3 \sum_{\nu=1}^{\infty} T_{\text{slot},i,\nu} \sin[k \times (\frac{2\pi}{\tau_p} \times \alpha + \theta_i) + \varphi_{i,\nu}] = \sum_{k=\nu}^{\infty} \sum_{i=1}^3 T_{\text{slot},i,\nu} \sin[k \times (\frac{2\pi}{\tau_p} \times \alpha + \theta_i) + \varphi_{i,\nu}] \quad (9)$$

The cogging torque can be expressed as Equation (8). The period of fundamental harmonic of cogging torque is one rotor tooth pitch of 6° :

$$\begin{aligned} T_{\text{cog}} &= T_{\text{end}} + T_{\text{slot}} \\ &= \sum_{\nu=1}^{\infty} T_{L,\nu} \sin(\nu \times \frac{2\pi}{\tau_p} \times \alpha + \gamma_{\nu}) + \sum_{\nu=1}^{\infty} T_{R,\nu} \sin(\nu \times \frac{2\pi}{\tau_p} \times \alpha + \beta_{\nu}) + \sum_{\nu=1}^{\infty} \sum_{i=1}^3 T_{\text{slot},i,\nu} \sin[\nu \times (\frac{2\pi}{\tau_p} \times \alpha + \theta_i) + \varphi_{i,\nu}] \quad (10) \\ &= \sum_{\nu=1}^{\infty} [f_{\nu} \sin(\nu \times \frac{2\pi}{\tau_p} \times \alpha) + h_{\nu} \cos(\nu \times \frac{2\pi}{\tau_p} \times \alpha)] = \sum_{\nu=1}^{\infty} [\sqrt{f_{\nu}^2 + h_{\nu}^2} \sin(\nu \times \frac{2\pi}{\tau_p} \times \alpha + \arctan \frac{h_{\nu}}{f_{\nu}})] \end{aligned}$$

where:

$$f_{\nu} = \sum_{\nu=1}^{\infty} \sin(\nu \times \frac{2\pi}{\tau_p} \times \alpha) \times [T_{L,\nu} \cos(\gamma_{\nu}) + T_{R,\nu} \cos(\beta_{\nu}) + \sum_{i=1}^3 T_{\text{slot},i,\nu} \cos(\nu \times \theta_i + \varphi_{i,\nu})] \quad (11)$$

$$h_{\nu} = \sum_{\nu=1}^{\infty} \cos(\nu \times \frac{2\pi}{\tau_p} \times \alpha) \times [T_{L,\nu} \sin(\gamma_{\nu}) + T_{R,\nu} \sin(\beta_{\nu}) + \sum_{i=1}^3 T_{\text{slot},i,\nu} \sin(\nu \theta_i + \varphi_{i,\nu})] \quad (12)$$

3.2. Torque Ripple of the Modular Arc-Linear Flux-Switching Permanent-Magnet Motor

Based on the FEM model established in Figure 4a, cogging torque and load torque curves are shown in Figure 7. According to Figure 7, two curves change periodically, and the period is one rotor tooth pitch of 6° . It is found that the period of cogging torque is the same as that of back EMF. When rotor end meets stator end, the end effect will be enhanced. However, due to the good structure of the MAL-FSPM, the minimum values of cogging torque and load torque during $\tau_p > d_{\text{end}} > 0$ are a little smaller than that of cogging torque during $d_{\text{end}} > \tau_p$. It should be noted that cogging torque curve and load torque curve have the same varying trend for both $d_{\text{end}} > \tau_p$ and $\tau_p > d_{\text{end}} > 0$. Therefore, it can be concluded that torque ripple is mainly caused by cogging torque. Figure 8 shows the harmonics analysis of cogging torque by the Fourier transform for $d_{\text{end}} > 2\tau_p$ and $2\tau_p > d_{\text{end}} > 0$. First harmonic, second harmonic, fourth harmonic and sixth harmonic are main components for both $d_{\text{end}} > 2\tau_p$ and $2\tau_p > d_{\text{end}} > 0$. Average torque and torque ripple are calculated in the Table 2. The torque ripple is calculated by Equation (13) and the torque ripple is very large. It shows that torque ripple for $\tau_p > d_{\text{end}} > 0$ is a little bigger than that of $d_{\text{end}} > \tau_p$:

$$Ripple = \frac{T_{\max} - T_{\min}}{2T_{AV}} \times 100\% \quad (13)$$

Table 2. Torque performance of the MAL-FSPM.

Range of d_{end}	Maximum Torque (N·m)	Minimum Torque (N·m)	Average Torque (N·m)	Torque Ripple (%)
$d_{\text{end}} > 2\tau_p$	7.88	4.08	5.78	32.9
$2\tau_p > d_{\text{end}} > \tau_p$	7.93	4.09	5.83	32.9
$\tau_p > d_{\text{end}} > 0$	7.90	2.87	5.58	45.1

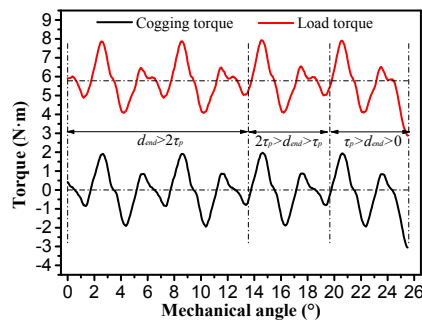


Figure 7. The no-load cogging torque and load torque curves.

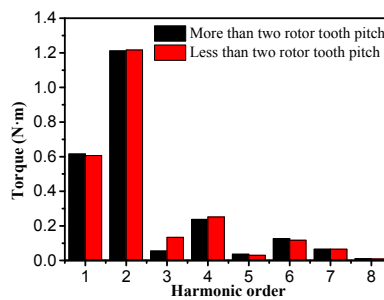


Figure 8. Harmonic analysis of cogging torque.

4. Rotor Step Skewing Technology

4.1. Analysis of Rotor Step Skewing

Due to the simple rotor structure of the MAL-FSPM, rotor step skewing technology can be easily realized to decrease cogging torque and torque ripple. When rotor of the MAL-FSPM is divided into N steps that are arranged axially in the discrete steps, the MAL-FSPM equivalently consists of N sub-motors that magnetic field of adjacent sub-motor has a phase difference of A_n degree (electrical degree). Figure 9 shows an example of rotor step skewing of three. Figure 10a shows phase relationship of sub-motors when step number is even, while Figure 10b shows phase relationship of sub-motors when step number is odd.

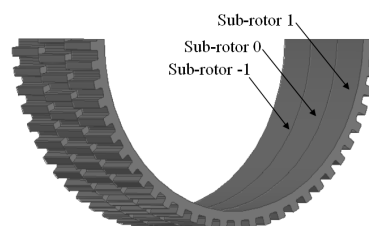


Figure 9. Example for rotor step skewing of three.

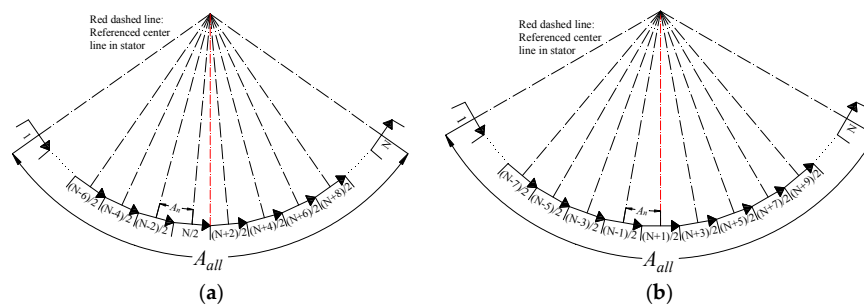


Figure 10. The phase relationship of sub-motors: (a) step skewing number is even; and (b) step skewing number is odd.

According to Figure 10a,b, the rotor step skewing effect on the v^{th} harmonic of cogging torque can be expressed as follows:

$$SkewC_{v,N} = \frac{\sin(N \times v \times \frac{A_n}{2})}{N \times \sin(v \times \frac{A_n}{2})} \tag{14}$$

$$A_n = \frac{A_{all}}{N - 1} \tag{15}$$

where A_{all} is the total skewing angle measured in electrical degree, N is skewing step number, v is harmonic order, and A_n is the angle between adjacent sub-motors.

The total cogging torque of the MAL-FSPM with rotor step skewing can be obtained as follows:

$$T_{cogskew} = \sum_{v=1}^{\infty} [SkewC_{v,N} \times \sqrt{f_v^2 + h_v^2} \sin(v \times \frac{2\pi}{\tau_p} \times \alpha + \arctan \frac{h_v}{f_v})] \tag{16}$$

Therefore, the cogging torque and torque ripple can be decreased as much as possible when the total skewing angle meets Equation (17):

$$A_{all} = \frac{2\pi(N - 1)}{N} \tag{17}$$

Since the limit value of $SkewC_{v,N}$ equals 1 at $v = k \times N$ (k is nonnegative integer), the harmonic of $v = k \times N$ cannot be eliminated. On the other hand, rotor skewing technology will also influence the output torque. If the sinusoidal current is adopted and phase angle of current is the same as the corresponding phase angle of back EMF, the output torque can be expressed as follows:

$$T = \frac{mE_m I_m}{2\omega_r} \tag{18}$$

where m is the phase number, E_m is amplitude of the fundamental back EMF per phase, I_m is the amplitude of the input sinusoidal current, and ω_r is the mechanical angular speed.

Therefore, the output torque can be reflected by the back EMF. Equation (19) shows the rotor step skewing on the fundamental component of back EMF:

$$SkewV_N = \frac{\sin(N \times \frac{A_n}{2t})}{N \times \sin(\frac{A_n}{2t})} \tag{19}$$

In Equation (19), t is represented the period ratio of cogging torque to the back EMF. Comparing Equations (14) and (19), it is found that cogging torque and back EMF will be reduced at the same time if t equals one. Figure 11 shows the relationship among the step number N , $SkewV_{v,N}$ and t . It can be seen that big value of t is corresponding to big $SkewV_{v,N}$ for the different step number. As for a constant value of t , the lower step number has higher value of $SkewV_{v,N}$. When step number is

more than three, the $SkewV_{v,N}$ starts to saturate and flat. Therefore, in order to reduce torque ripple as much as possible and influence average torque as small as possible, bigger value of the t and smaller value of step number are necessary.

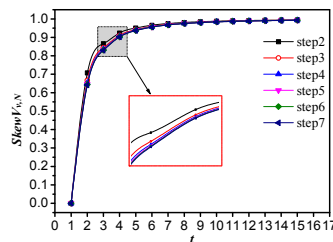


Figure 11. The relationship among $SkewV_{v,N}$, N and t .

4.2. The 2D Finite Element Method Verifying

As for the MAL-FSPM, period ratio of cogging torque to back EMF equals one. Based on Equations (15) and (17), the step number and the corresponding skewing angle are shown in the Table 3 and the skewing angle is calculated based on the period of cogging torque. Realization of the 2D FEM with rotor step skewing is as follows: when the number of rotor step skewing equals N , N FEM sub-motor models are established with $1/N$ total axial length. Stator parts of the N models are the same and in the same position, while initial positions of sub-motor rotors are shifted at different angle at interval of corresponding angle A_n in Table 3. According to Figure 10, $N/2$ (N is even) or $(N-1)/2$ (N is odd) sub-motor rotors are at right of the referenced center line in stator, and $N/2$ (N is even) or $(N-1)/2$ (N is odd) sub-motor rotors are at left of the referenced center line in stator. Back EMF, cogging torque and average torque of the total MAL-FSPM are obtained by superimposing that of N sub-motor models.

Table 3. The step number and skewing angle of the MAL-FSPM.

Step Number	2	3	4	5	6	7
A_{all} (°)	180	240	270	288	300	308.6
A_n (°)	180	120	90	72	60	51.4
Mechanical degree for A_n (°)	3	2	1.5	1.2	1	0.86

With the step number increasing, the amplitude of back EMF, average torque and the maximum value of cogging torque are shown in Figure 12. It can be seen that the cogging torque can be effectively reduced when step number is more than two. However, back EMF and average torque are also heavily reduced. Cogging torque harmonic analysis varying with the step number is shown in Figure 13. Since the main harmonics of the MAL-FSPM are first harmonic, second harmonic, fourth harmonic and sixth harmonic, step skewing number of two is the least effective for reducing cogging torque.

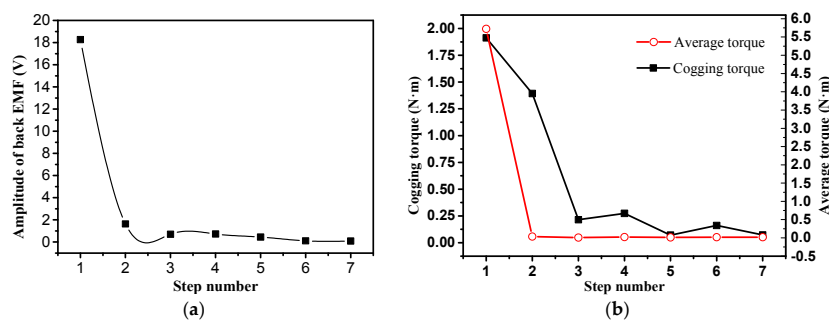


Figure 12. Increase of step skewing number: (a) amplitude of back EMF; and (b) average torque and maximum value of cogging torque.

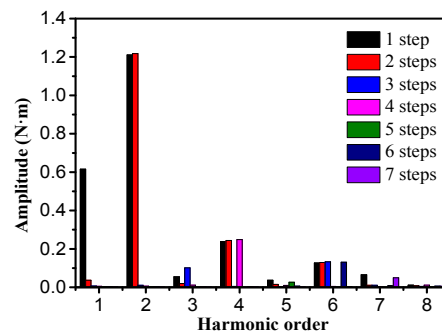


Figure 13. Relationship between cogging torque harmonic and step number.

Therefore, rotor step skewing technology cannot be directly used for the MAL-FSPM. The low-order harmonics, such as first harmonic and second harmonic, are supposed to be removed firstly to increase the value of t .

5. First and Second Harmonic Reduction

5.1. Rotor Tooth Width

Rotor tooth width is an important factor to influence the torque performance of the MAL-FSPM, as shown in Figure 3. The k_{rw} is defined as the ratio of rotor tooth width t_r to the PM thickness t_{PM} . In order to avoid rotor tooth saturating and big flux leakage, the value of k_{rw} ranges from 1.0 to 1.5 with step of 0.1 while PM width is kept constant. Amplitude of cogging torque harmonics, average torque, torque ripple with k_{rw} varying are shown in Figure 14. It can be seen from Figure 14 that the first harmonic, second harmonic and fourth harmonic of cogging torque all decrease with k_{rw} increasing, while the third harmonic increases firstly and then decreases. Higher harmonics of cogging torque are small and change little with k_{rw} varying. When k_{rw} is more than 1.2, the third harmonic is the most main component in the cogging torque and maximum amplitude of third harmonic can be obtained at value of k_{rw} 1.4. In order to change the period ratio of cogging torque to the back EMF t , the third harmonic should be kept as high as possible. In addition, due to bigger flux leakage caused by rotor tooth closing to the permanent magnet, average torque starts to be reduced when k_{rw} is more than 1.1. Considering that the lower-order harmonic (first harmonic and second harmonic) can be reduced as much as possible, and the third harmonic of cogging torque and average torque should be kept as high as possible, the value of k_{rw} 1.4 is selected.

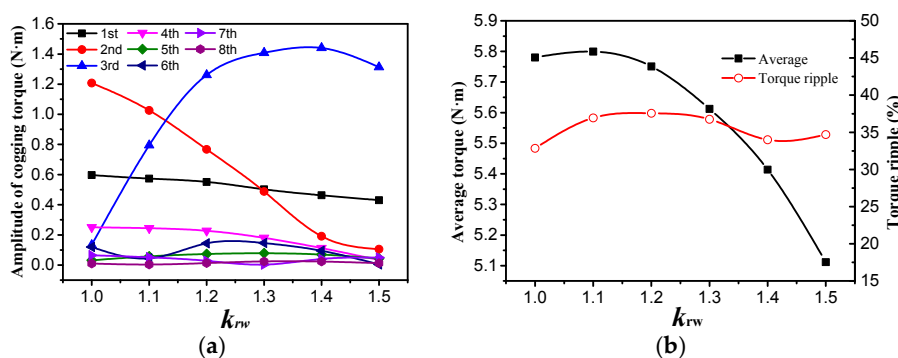


Figure 14. Influence of k_{rw} : (a) cogging torque harmonics; and (b) average torque and torque ripple.

5.2. Stator Slot Open Width

Based on the foregoing optimization, the rotor tooth width is chosen as 2.8° . Stator slot open width t_s is also an important factor to influence cogging torque, as shown in Figure 15. k_{sw} is defined

as the ratio of stator slot open width t_s to the PM thickness t_{PM} . In order to easily place the winding into slot, minimum value of k_{sw} is set 0.4. Furthermore, k_{sw} ranges from 0.4 to 1.0 with step of 0.1.

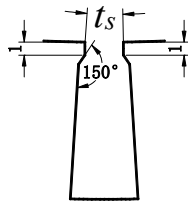


Figure 15. Slot open width adjustment.

Cogging torque harmonics, average torque, and torque ripple with varying of k_{sw} are shown in Figure 16. The amplitude of fundamental harmonic is reduced with the decrease of k_{sw} . Since the increase of stator slot open width decreases the opportunity of flux leakage produced by PMs, the average torque is increased with the k_{sw} increasing. Torque ripple increases firstly and then decreases with k_{sw} increasing. Maximum value of torque ripple is obtained at k_{sw} of 0.6. In addition, the slot open width almost has no influence on the amplitude of second harmonic and higher-order harmonic that is more than three, and third harmonic is most main component. Therefore, third harmonic should be remained and first harmonic should be reduced to increase the value of t . When k_{sw} is not more than 0.8, first harmonic can be reduced much. Amplitude of third harmonic reaches maximum value at value k_{sw} of 0.7, but average torque is reduced and torque ripple is increased compared with the value k_{sw} of 0.8. Based on the principle that the lower-order harmonics can be reduced as much as possible while the average torque is reduced as small as possible, the value of k_{sw} is obtained at 0.8. The corresponding cogging torque curve is shown in Figure 17. It can be seen that the period of the cogging torque is about 2° (mechanical angle) at the value k_{sw} of 0.8. The value of t is increased from 1 to 3. Furthermore, average torque, amplitude of cogging torque and torque ripple are $5.24 \text{ N}\cdot\text{m}$, $2.76 \text{ N}\cdot\text{m}$ and 55.3% , respectively. Although torque ripple is increased, the value of t is increased.

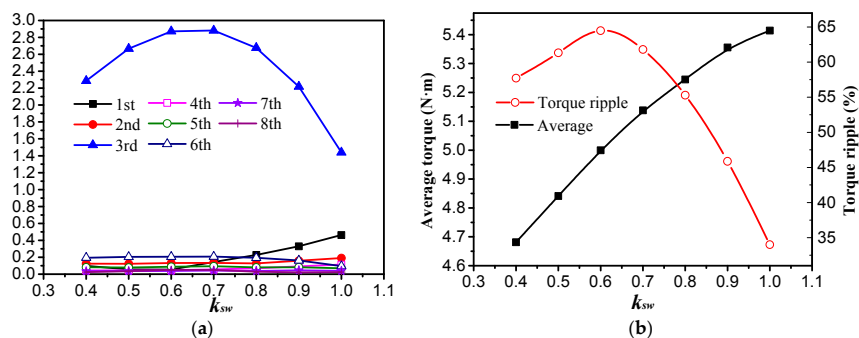


Figure 16. Increase of k_{sw} : (a) the cogging torque harmonics; and (b) average torque and torque ripple.

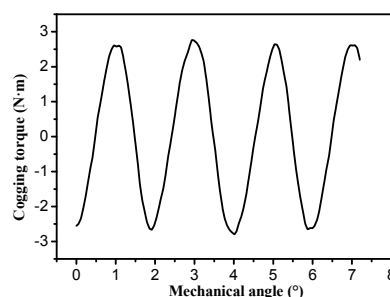


Figure 17. Cogging torque curve at $k_{sw} = 0.8$.

6. Torque Ripple Reduction

After the optimization of rotor tooth width and stator slot open width, the period ratio of cogging torque to the back EMF equals three. According to the analysis in Section 4, step number and corresponding skewing angle are shown in Table 4. According to the analysis in Section 3, cogging torque and torque ripple are bigger for the d_{end} that is less than one rotor tooth pitch (τ_p). Therefore, two cases are researched: (1) d_{end} is more than one rotor tooth ($d_{\text{end}} \geq \tau_p$); and (2) d_{end} is less than one rotor tooth ($\tau_p > d_{\text{end}} \geq 0$).

Table 4. Step number and skewing angle.

Step Number	2	3	4	5	6	7
A_{all} (°)	180	240	270	288	300	308.6
A_n (°)	180	120	90	72	60	51.4
Mechanical degree for A_n (°)	1	0.67	0.5	0.4	0.33	0.29

6.1. Torque Ripple Reduction by the 2D Finite Element Method

6.1.1. d_{end} More Than One Rotor Tooth Pitch

When d_{end} is more than one rotor tooth pitch ($d_{\text{end}} > \tau_p$), with the increasing of step skewing number, amplitude of back EMF, maximum of cogging torque, harmonic analysis of cogging torque, average torque and torque ripple are shown in Figure 18. According to Figure 18, the cogging torque is effectively suppressed and torque ripple is within 10% when the step number is more than two. Amplitude of back EMF and average torque decrease slowly with the increase of step number. When the step number is more than three, the decrease of cogging torque and torque ripple is starting to flatten. Comprehensively considering, step number of three is optimum and the corresponding skewing angle for adjacent sub-motors is 0.667° (mechanical degree). Average torque and torque ripple are $4.37 \text{ N}\cdot\text{m}$ and 6.4% , respectively. The torque curves before and after rotor step skewing are shown in Figure 19. After the three-step skewing, torque ripple is decreased from 55.3% to 6.4% , by 88.4% , at the expense of reducing average torque from $5.24 \text{ N}\cdot\text{m}$ to $4.37 \text{ N}\cdot\text{m}$, by 16.6% . Compared with initial structure, torque ripple is decreased from 32.9% to 6.4% , by 79.8% .

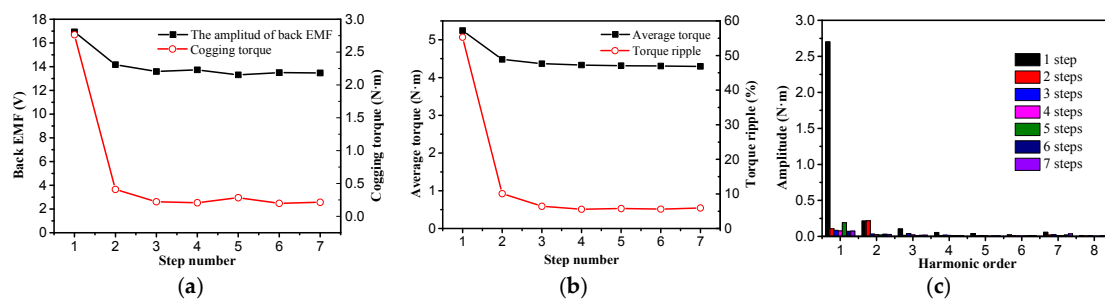


Figure 18. Increase of step skewing number: (a) amplitude of back EMF and cogging torque; (b) average torque and torque ripple; and (c) cogging torque harmonics.

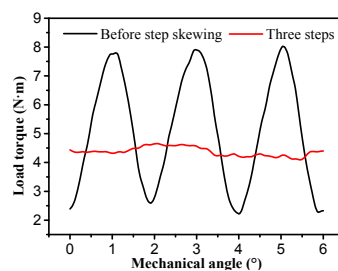


Figure 19. Load torque of before and after rotor step skewing.

6.1.2. d_{end} Less Than One Rotor Tooth Pitch

When the distance d_{end} between left end of rotor and left end of stator is less than one rotor tooth pitch ($\tau_p > d_{\text{end}} > 0$), cogging torque curves and load torque curves are shown as Figure 20. Because the angular difference exists between adjacent rotor steps as shown in Figure 9, the width of left rotor end tooth is different for each sub-rotor. It is the same for other step skewing number. Compared with the initial structure as shown in Figures 2 and 3 rotor step skewing causes small distortion of magnetic field when d_{end} is less than one rotor tooth pitch. Therefore, cogging torque and torque ripple are bigger when d_{end} is less than 1° , as shown in Figure 20. Nevertheless, compared with the structure before rotor step skewing, rotor step skewing can effectively reduce the torque ripple, as shown in the Table 5. It also can be seen that when step number is more than two, cogging torque curves and load torque curves are entirely coincident. Therefore, rotor step of three is enough. After the rotor three-step skewing, torque ripple is decreased from 58.7% to 22.7%, by 61.3%. Compared with the initial structure, torque ripple is decreased from 45.1% to 22.7%, by 49.7%.

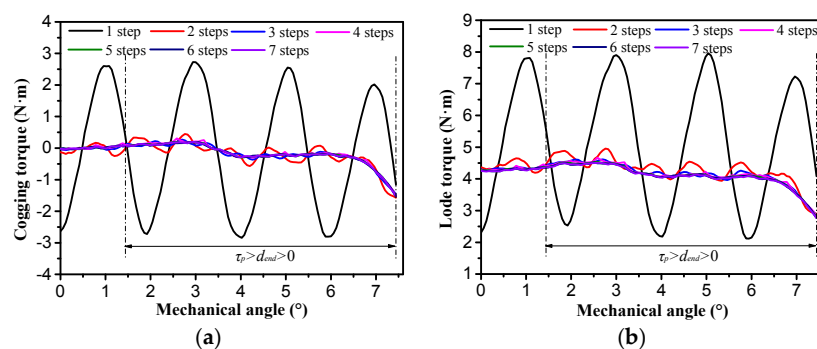


Figure 20. (a) Cogging torque; and (b) load torque.

Table 5. Torque characteristics for $\tau_p > d_{\text{end}} > 0$.

Parameter	1 Step	2 Steps	3 Steps	4 Steps	5 Steps	6 Steps	7 Steps
Peak-peak cogging (N·m)	5.57	2.04	1.87	1.99	1.86	1.87	1.87
Average torque (N·m)	4.98	4.26	4.14	4.13	4.09	4.08	4.07
Ripple (%)	58.7	24.2	22.7	24.4	23.0	22.9	22.9

6.2. Result Verifying by the 3D Finite Element Method

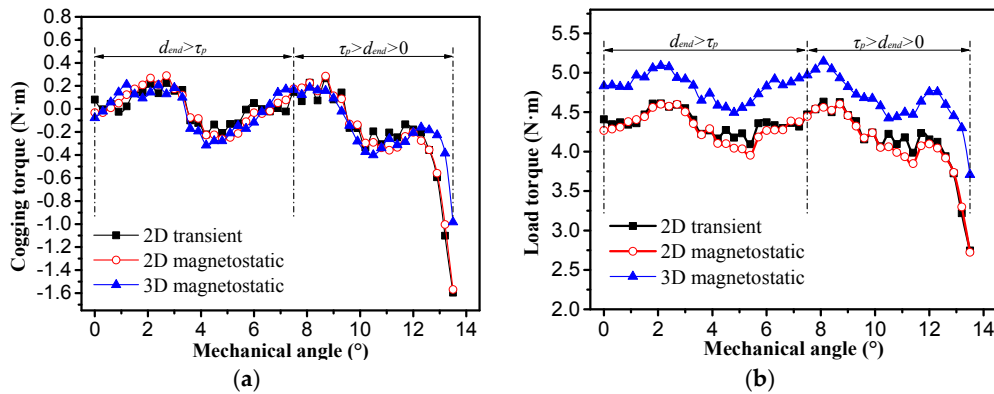
Based on the aforesaid analysis, rotor step skewing number of three is enough. Therefore, 3D FEM magnetostatic model with rotor step skewing of three is established. As for 2D and 3D magnetostatic, cogging torque and load torque are calculated by rotating the rotor to different positions step by step, and the load torque needs additional current injected to the winding in correspondence with the rotor position. As for distance (d_{end}) between left end of rotor and left end of stator is $d_{\text{end}} > \tau_p$ or $\tau_p > d_{\text{end}} > 0$, cogging torque curves for 2D transient, 2D magnetostatic and 3D magnetostatic are shown as Figure 21a, and the corresponding values of maximum cogging torque and minimum cogging torque are shown in the Tables 6 and 7. Load torque curves are shown as Figure 21b; Tables 6 and 7 show the corresponding torque characteristics.

Table 6. Characteristics of torque for $d_{\text{end}} > \tau_p$.

Parameters	2D Transient	2D Magnetostatic	3D Magnetostatic
Peak-peak cogging (N·m)	0.45	0.55	0.52
Peak-peak load torque (N·m)	0.56	0.65	0.6
Average torque (N·m)	4.37	4.32	4.82
Torque ripple (%)	6.4	7.5	6.2

Table 7. Characteristics of torque for $\tau_p > d_{end} > 0$.

Parameters	2D Transient	2D Magnetostatic	3D Magnetostatic
Peak-peak cogging torque(N·m)	1.87	1.86	1.11
Peak-peak load torque (N·m)	1.87	1.88	1.43
Average torque (N·m)	4.14	4.08	4.65
Torque ripple (%)	22.7	23.0	15.5

**Figure 21.** (a) Cogging torque; and (b) load torque.

As for the cogging torque, it can be seen that three curves are in good agreements. As for the load torque, load torque curves of 2D transient and 2D magnetostatic are also in good agreements for both $d_{end} > \tau_p$ and $\tau_p > d_{end} > 0$ in Figure 21b. The shape of the three torque curves at load are almost the same. However, it is worth noting that average torque at load of 3D FEM is a little bigger than that of 2D FEM. According to the aforesaid comparison of 2D and 3D FEM results, it can be concluded that end effects and axial interactions existing in the 3D FEM may compensate the cogging torque caused by rotor end meeting stator end and may be beneficial to increase the average torque. Nevertheless, 3D FEM results verify that torque ripple and cogging torque can be greatly reduced by the aforesaid method. On the other hand, when left scanning range (θ_L) and right scanning range (θ_R) are reduced to 50° , by 2° , the torque ripple will be within 6.4% during whole operation by analyzing the results obtained by 2D transient FEM.

7. Conclusions

A novel modular AML-FSPM used for scanning system instead of reduction gearboxes and kinematic mechanisms is researched in this paper. Structure of the AML-FSPM is introduced and back EMF of the AML-FSPM is well balanced. Cogging torque model of the AML-FSPM is established based on end torque and slot torque. Furthermore, slot torque can be expressed by the sum of each stator module. Both the period of end torque and the period of slot torque are just one rotor tooth pitch of 6° (mechanical angle), which is the same as the period of the back EMF. Therefore, period ratio of cogging torque to the back EMF equals one. The characteristics of the cogging torque and torque ripple are investigated for both $d_{end} > 2\tau_p$ and $d_{end} < 2\tau_p$. It shows that peak-peak cogging torque of $d_{end} < \tau_p$ is bigger than that of $d_{end} > \tau_p$. Furthermore, the torque ripple is mainly caused by the cogging torque. The first harmonic, second harmonic, fourth harmonic and sixth harmonic are main components in the cogging torque. In order to reduce the cogging torque as much as possible and affect the back EMF as little as possible, influence of period ratio of cogging torque to the back EMF is investigated. It shows that bigger value of t is better. Therefore, rotor tooth width and stator slot open width are optimized to enhance third harmonic and restrain first and second harmonic. After optimization of rotor tooth width and slot open width, period ratio of cogging torque to back EMF is increased from 1 to 3. Then, step rotor skewing is adopted to reduce torque ripple. After the rotor three-step skewing,

torque ripple is decreased from 32.9% to 6.4%, by 79.8%, for $d_{\text{end}} > \tau_p$, torque ripple is decreased from 45.1% to 22.7%, by 49.7%, for $d_{\text{end}} < \tau_p$ when scanning range is kept unchanged, and torque ripple will be within 6.4% during whole operation if left scanning range (θ_L) and right scanning range (θ_R) are reduced by 2° . Finally, the result obtained by 2D FEM is validated by 3D FEM.

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