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Article

Application of the Extension Taguchi Method to Optimal Capability Planning of a Stand-alone Power System

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Abstract: An Extension Taguchi Method (ETM) is proposed on the optimized allocation of equipment capacity for solar cell power generation, wind power generation, full cells, electrolyzer and hydrogen tanks. The ETM is based on the domain knowledge containing the product specifications and allocation levels provided by suppliers and design factors since most of the renewable energy equipment available in the market comes with a specific capacity. A proper orthogonal array is used to collect 18 sets of simulation responses. The extension theory is introduced to determine the correlation function, and factor effects are used to identify the optimized capacity allocation. The hours of power shortage are simulated using Matlab for all capacity allocations at the lowest establishment cost and the optimized capacity allocation of loss of load probability (LOLP). Finally, the extension theory, extension AHP theory, ETM and Analytic Hierarchy Process (AHP) are used to determine the optimized capacity allocation of the system. Results are compared for the above four optimization simulation methods and verify that the proposed ETM surpasses the others on achieving the optimized capacity allocation.

Keywords: stand-alone power system (SAPS); extension theory; extension Taguchi method (ETM); analytic hierarchy process (AHP); loss of load probability (LOLP)

1. Introduction

This paper integrates the renewable energy equipment of the photovoltaic (PV) power system, wind power, fuel cell, electrolyzer and hydrogen tank into one stand-alone power system. The optimized capacity allocation is an important issue for a stand-alone renewable energy system. A stand-alone renewable energy system is usually installed in remote mountains, on an island or where the utility power grid does not reach. A poor capacity allocation will not balance the power supply and demand and waste the costs for the system establishment. The simulated analysis shall be the reference of capability configuration [1,2]. The allocation of system device capacity affects the stand-alone power system [3,4]. When the device capability configuration is not appropriate, it may cause power shortages, or generate too much electricity while the system is unavailable, which wastes money [5,6]. On the contrary, with reasonable system allocation, the operation of power supply system will be set at the optimum cost.

Nelson *et al.* applied particle swarm optimization on the optimal sizing of a stand-alone wind/fuel cell power system [7]. They presented the unit sizing and cost analysis of stand-alone hybrid

wind/PV/fuel cell power generation systems. Ekren *et al.* [8] used simulated annealing method for the size optimization of a PV/wind hybrid energy conversion system with battery storage. The drawback of this method is that it takes too much computing time and the computing results needs to be adjusted through experience to fit in the specifications of the common practical products.

Yang *et al.* [9] applied genetic algorithm to calculate the optimal system configuration with relative computational simplicity. Some commercial software like HOMER [10], IHOGA [11] were developed to figure out the optimal allocation. Based on the simulated weather data, this study estimates the possibility of loss of load probability (LOLP) for one or more years. Taguchi quality engineering was developed and advocated by Dr. Taguchi Genichi [12] in 1950. The orthogonal array experiment design and analysis of variance (ANOVA) were used for the analysis with a limited experimental data to effectively improve product quality [12]. The Taguchi method is widely applied in the manufacturing field, but this study is the first to apply the Taguchi method in the optimization of hybrid power systems.

This paper combines the extension theory with the Taguchi method, selects the proper design factors and levels via the orthogonal array to greatly decrease the number of experiments to acquire the optimum experiment result through the classical domain and neighborhood domain extension to narrow down and find the optimum capability planning. The advantages of the proposed ETM include: (1) the optimization process is subject to the specifications of practical equipment; (2) fast computing speed; and (3) the results could be directly applied on the real situation.

2. System Model

The stand-alone power system is divided into electricity generation, energy storage and standby energy. Electricity generation is formed by the wind power and PV power system using the kinetic energy of wind and the solar luminous energy. Although the wind and solar complementary systems make up for each other's deficiencies as shown in Figure 1, where the natural energy generating capacity cannot create a continuous power supply all the time due to weather variations. Therefore, energy storage equipment is required. When the electricity generated is enough, it shall launch the electrolyzer to produce the hydrogen, and store the latter in the hydrogen tank. When the generating capacity is insufficient, it could use the hydrogen in the hydrogen tank and the fuel cell to satisfy the load as shown in Figure 2. The dump load is also included as a component in the system to consume the excess electricity when renewable power is abundant and the storage system is fully charged. In order to make a system device with the most cost-saving and most efficient power supply capacity, the system capability configuration must operate optimally.

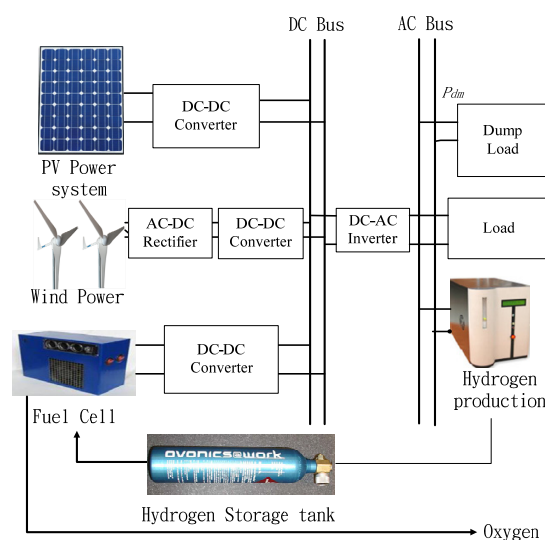


Figure 1. System architecture.

2.1. The Objective Function

Normally, this system uses wind power and PV power system, and makes use of wind-light complementarity feature to generate electricity. If wind turbines and solar cell cannot supply rated load, then determine whether there is hydrogen can be used, and then use hydrogen to satisfy load. The loss of load hours β_H will increase if hydrogen is not sufficient. The calculation process is shown in Figure 2, where P_W is power capacity of wind power, P_{PV} is power capacity of the PV power system, P_L is load capacity.

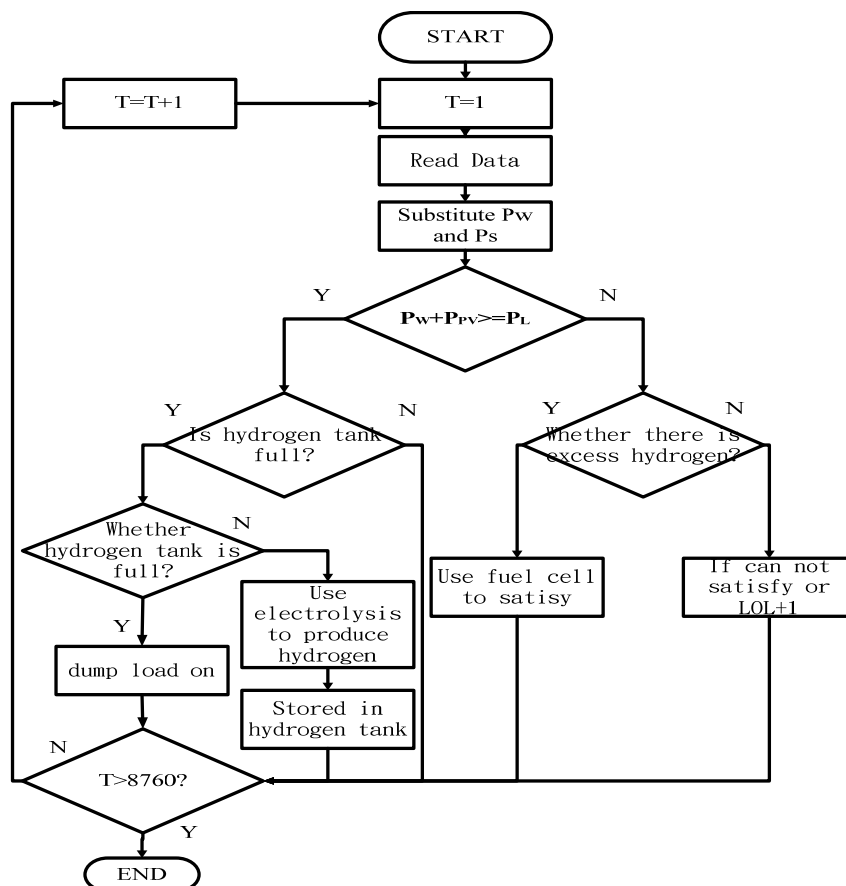


Figure 2. Operation flowchart of the proposed stand-alone power system.

The above β_H of the system can be used to calculate the loss of load probability (LOLP) β_P . Bringing β_P into the algorithm is to solve the contradiction of load capacity, loss of load, and cost. The calculation of β_P is shown in Equation (1):

$$\beta_P = \frac{\beta_H}{T} \quad (1)$$

β_P per hour is often expressed as 0 or 1. When β_P is 1 in one hour, it indicates that the power system cannot supply the rated load [3]. The more times a 1 is recorded in total time T , the poorer the reliability of the independent power system.

Many methods and cost functions are available, and differences exist among them. Considering a stand-alone power system, especially in a remote area that the utility power grid cannot reach, the possibility of LOLP and the return on investment are the most two important factors in Taiwan. According to the cost planning of available products, cost B_c and LOLP are equally important. The sum

of weights is 1, and the weights of cost (λ_1) and LOLP (λ_2) are set as 0.5. The weights vary depending on different system requirements. The objective function of the paper is shown in Equation (2):

$$\text{Min}F = \sum \beta_C(pu) \times \lambda_1 + \beta_p(pu) \times \lambda_2 \quad (2)$$

where:

$$\beta_C(pu) = \frac{B_C(k) - B_{C \min}}{B_{C \max} - B_{C \min}} \quad (3)$$

$$\beta_p(pu) = \frac{B_p(k) - B_{p \min}}{B_{p \max} - B_{p \min}} \quad (4)$$

In addition, we also calculate the investment recovery period of the total power generation, and the total recovery period is shown in Equation (5):

$$Y_C = \frac{C_t}{(E_p \times G_p - C_t \times C_p)} \quad (5)$$

where Y_C is the return period on investment, C_t is the setup cost, E_p is total power generation, G_p is the power unit cost, and C_p is bank interest rate in Taiwan.

2.2. Mathematical Models of Solar Photovoltaic

Silicon is the most easily obtainable material used for manufacturing semiconductors, and it is plentiful on the planet. Currently silicon is the main material for solar cells. Photovoltaic modules are major formed by serially/parallelly connecting solar cells together, and usually photovoltaic module structures contain large PN junction diodes. When solar cells are illuminated by sunlight, they will convert light energy into electrical energy. Being serially or parallelly connected in a module, a solar cell will have a different impact on the current and voltage of array output. When a parallelly connected solar cell is added, it will increase the array current; when a serially connected solar cell is added, it will increase the array voltage, where I_{ph} is the current generated by solar cell when it is illuminated by sunlight, [4], and the equations of the solar energy equivalent circuit are shown in Equations (6) and (7):

$$I_{PH} = Z \times I_{SC}(1 + K_o \times (T_{PV} - T_r)) \quad (6)$$

$$P_{PV} = n_p I_{PH} V - n_p I_{sat} V \left[e\left(\frac{q}{BK T_{PV}} \frac{V}{n_s}\right) - 1 \right] \quad (7)$$

where Z is illuminance, I_{SC} is a current on a light intensity 1000 W/m^2 and ambient temperature 298 K , I_{sat} is the reverse saturation current, n_p is the number of solar cells connected in parallel, n_s is the number of solar cells in series, K_o is the short circuit current correction coefficient, B is an ideal parameter which is 1, K is the Boltzmann constant ($1.3806 \times 10^{-23} \text{ J/K}$), T_{pv} and T_r are the real and reference temperature of the solar cell.

2.3. Mathematical Models of Wind Power

Wind turbines obtain kinetic energy from wind, mainly from blades touched by air flow when the Earth rotates. Wind energy will rotate blades; the wind turbine blade shaft will convert wind energy into useful mechanical energy, and this is followed by the conversion of mechanical energy into electrical energy. Due to the aerodynamic effect, the blade rotor will be rotated by the force of the wind, and the aerodynamic force is divided into lift force and drag force to produce torque on the blades [5]. The output power of the wind turbine is converted into mechanical energy, and the equation generated by wind power generation is shown as in Equation (8) [6]:

$$P_A = \frac{1}{2} \rho \pi R^2 V_w^3 \quad (8)$$

When the wind speed is constant, the wind turbine power output is proportional to the square of wind turbine's diameter. When a wind turbine's diameter is fixed, its power output is proportional to the cube of wind speed, when wind diameter and wind speed remain unchanged. A wind turbine's power output is proportional to C_p [13], and the wind output equation is shown as in Equation (9):

$$P_w = C_p \times (T_{SR}) \times P_A \quad (9)$$

where ρ the is air density (kg/m^3), R is the radius of the rotor blade (m), V_W is wind speed (m/s), T_{SR} is the wind turbine's blade tip speed ratio, and C_p is the wind turbine's performance index.

When the wind speed reaches V_{off} , the turbine will generally lock the rotor and suspend power generation in order to prevent the wind turbine from operating at speeds which may damage the blades, and this wind speed is called the shutdown wind speed. On the contrary, when the wind speed is lower than V_{on} , although the wind turbine can continue generating electricity, usually its operation will be suspended to prevent the wind turbine from disconnecting from/connecting to the power system too frequently, and this wind speed is called the cut-in wind speed. Based on Equation (10), the typical curve of the wind power system is shown in Figure 3 [14]:

$$P_w(V_W) = \left\{ \begin{array}{l} 0 \\ C_p \times (T_{SR}) \times \left(\frac{1}{2} \rho \pi R^2 V_w^3 \right) \\ 0 \end{array} \middle| \begin{array}{l} V_w < V_{on} \\ V_{on} \leq V_w \leq V_{off} \\ V_w > V_{off} \end{array} \right\} \quad (10)$$

where V_w is the current wind speed, V_{on} is the starting wind speed, and V_{off} is the ending wind speed.

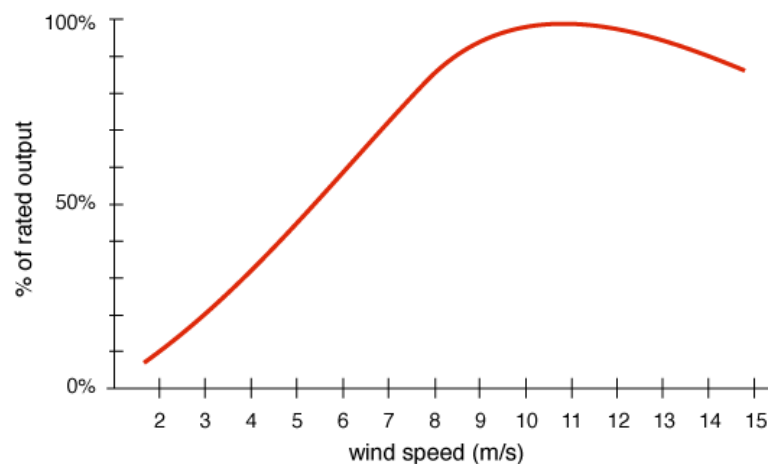


Figure 3. Typical curve of a wind power system [14].

2.4. Mathematical Models of Fuel Cell

Fuel cells are a kind of device that converts chemical energy into electrical energy. The voltage of a single fuel cell is too low to be practical (approximately 0.6 to 0.8 volts), so it is necessary to serially connect fuel cells together in order to raise the power output voltage [15]. Fuel cells are subject to some losses when converting chemical energy into electrical energy. For fuel cells, the power output can reach its highest value only in a reversible state, but the power output is less than the ideal power because it is subject to some restrictions in actual operation. The fuel cells used in this study are proton exchange membrane fuel cells, and the expression governing these fuel cells is given by Equation (11):

$$V_{FC} = E_{Nerm} - V_{act} - V_{ohmic} - V_{con} \quad (11)$$

where, V_{FC} is output voltage, E_{Nernmo} is the voltage of the reversible cell (thermal electric potential of fuel cell), V_{act} is the activation overpotential, V_{ohmic} is the ohmic overpotential (ohmic overvoltage produced by the resistance effect of electrons passing through the electrode and protons passing through the exchange membrane), V_{con} is the concentration overpotential (concentration overpotential caused by the reduction of reaction gas concentration).

In Equation (11), E_{Nernmo} is the thermodynamic reversible voltage output by a single open circuit. Results obtained through the Nernst equation at a reference temperature of 25 °C are shown in Equation (12):

$$E_{Nernst} = \frac{\Delta G}{2F} + \frac{\Delta S}{2F} (T - T_0) + \frac{RT}{2F} \left[\ln(P_{H_2}) + \frac{1}{2} \ln(P_{O_2}) \right] \quad (12)$$

where, the Gibbs Free Energy change value is indicated by ΔG (J/mol), F is the Faraday constant (96487C), ΔS is the entropy value change, R is the universal gas constant (8.314 J/K·mol), P_{H_2} and P_{O_2} are the pressures of hydrogen and oxygen needed by fuel cell, T is the working temperature of fuel cell and T_0 is the reference temperature. ΔG , ΔS and T_0 under standard temperature and standard atmospheric pressure are substituted into Equation (12) to obtain the simplified Equation (13):

$$E_{Nernmo} = 1.229 - 0.85 \times 10^{-3} (T - 298.15) + 4.31 \times 10^{-5} T \times [\ln(P_{H_2}) + 0.5 \ln(P_{O_2})] \quad (13)$$

V_{act} in Equation (11) is the voltage drop produced by the activated anode and cathode, which is shown in Equation (14):

$$V_{act} = [\xi_1 + \xi_2 T + \xi_3 \ln(CO_2) + \xi_4 T \ln(I_{FC})] \quad (14)$$

I_{FC} in Equation (14) is the current of the fuel cell, CO_2 (atm) the oxygen concentration and ξ_i ($i = 1-4$) are the characteristic coefficients of all fuel cells. V_{ohmic} voltage drop in Equation (11) will cause a voltage loss of the fuel cell due to the resistance in charge transfer, in conformity with Ohm's Law, see Equation (15):

$$V_{ohmic} = I_{FC} (R_M + R_C) \quad (15)$$

The Ohmic loss of a fuel cell can be minimized through use of a thin electrolyte membrane and conductive materials. R_C in Equation (15) is the resistance of the contact electron current, which is deemed as constant in the literature since it can't be obtained within the working temperature of proton exchange membrane fuel cell. R_M is the resistance of the proton exchange membrane, which can be obtained through an empirical formula, see Equation (16):

$$R_M = \frac{\rho_M \times l}{A_C} \quad (16)$$

$$\begin{aligned} \rho_M &= a/b \\ a &= 181.6 \left[1 + 0.03 \frac{I_{FC}}{A_C} + 0.062 \left(\frac{T}{303} \right)^2 \left(\frac{I_{FC}}{A_C} \right)^{2.5} \right] \\ b &= \left[\psi - 0.634 - 3 \left(\frac{I_{FC}}{A_C} \right) \right] \exp \left[4.18 \left(T - \frac{303}{T} \right) \right] \end{aligned} \quad (17)$$

A_C in Equation (16) is the activation area of the fuel cell (cm²), while the thickness of the electrolyte membrane is expressed by l (cm), and the resistance of the electrolyte membrane ρ_M (Ω -cm) indicates the coefficient, which is given by Equation (17). Parameter Ψ is the water content of membrane. The value of Ψ falling at 14 indicates an ideal relative humidity of 100%. However, the value of Ψ generally falls in the oversaturation region of 22–23, which is an adjustable parameter.

The voltage loss produced by a fuel cell in large-current operation is V_{con} , indicating the concentration loss caused by diffusion limited mass transfer, see Equation (18):

$$V_{con} = B \times \ln \left(1 - \frac{J}{J_{max}} \right) \quad (18)$$

In Equation (18), B is the constant of a fuel cell of any type, which is determined by the fuel cell and its operation status. J is the current density (mA/cm^2) produced by the fuel cell, J_{max} is the largest current density, which is determined between 500 and 1500 (mA/cm^2). Due to electrochemical action, the nitric oxide and carbonic oxide discharged by fuel cell is quite abundant. Thus, the invention of hydrogen energy converters with economic effectiveness and high efficiency will promote future commercial use. A typical 200 W fuel cell characteristic curve is as shown in Figure 4.

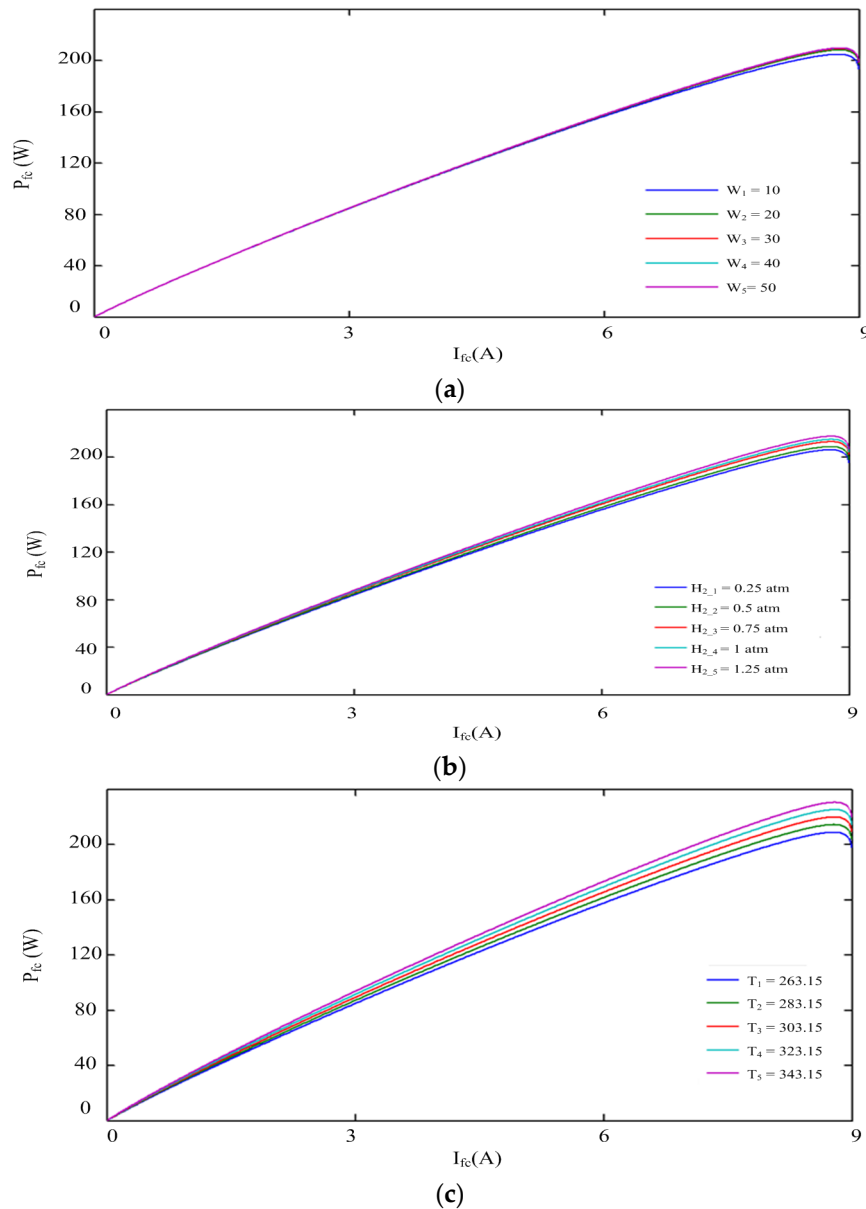


Figure 4. Characteristic curves of the tested fuel cell. (a) Characteristic curves of power-current under different humidity; (b) Characteristic curves of power-current under different hydrogen pressures; (c) Characteristic curves of power-current under different temperatures.

2.5. Objective Function Setting and Limitation

A well-optimized system will reduce costs to a minimum while satisfying the load demand. The targeted function of this paper is as Equation (2) [16], in which, the commercial market product has the consumption costs shown in Table 1.

Table 1. Cost of Each Design Factor.

Equipment Name	Equipment Cost	Unit Capacity	Cost (USD)
Wnd power	C_W	1000 W	688
PV power system	C_{PV}	230 W	565
Hydrogen tank	C_{HT}	40 L	235
Fuel Cell	C_{FC}	100 W	1250
Electrolyzer	C_E	100 W	1563

According to the regular market specifications of power equipment, the minimum power supply needs to satisfy the Equation (19) as follows:

$$\sum_{i=1} (P_W + P_V + P_{FC}) \geq P_{LOAD} + P_E + P_{dm} \quad (19)$$

3. Extension Taguchi Method

To optimize the allocation of equipment capacity, this paper proposes an optimization method combining extension theory and the Taguchi method. In 1983, the concept of extension theory was proposed to solve the contradictions and incompatibility problems. Based on some proper transformation, some problems that cannot be directly solved by given conditions may become easier or solvable [17]. One of the commonly used techniques in engineering fields is the Laplace transformation. The concept of fuzzy sets is a generalization of well-known standard sets to extend their application fields. Therefore, the concept of an extension set is to extend the fuzzy logic value from [0,1] to $(-\infty, \infty)$, which allows us to define any data in the domain and has given promising results in many fields [18–20]. Extension theory is used to calculate the comprehensive correlative degree of each group of the simulation experiment, then the analytical method average value of the Taguchi method is used to select the optimum capability configuration system and assess whether the selected group is the optimum result [21]. If the output result is optimal, then the process is done; otherwise, the extension correlative degree shall be recalculated. The advantage of this method is the ability to find the optimum solution in the shortest time and to limit the number of experiment trials needed. The calculation steps are as described below:

Step 1. Setting the level and design

This paper selects five three-level design factors in order to conform to the basic principle of an L_{18} orthogonal array. The design factors are used to reduce the power shortage probability while not ignoring the equipment cost. Thus the price is also set as a design objective. The design factor and the corresponding levels are shown in Table 2. The five three-level design factors are wind power, PV power, hydrogen tank, fuel cell, and electrolyzer. For example, the numbers of the wind power equipment designed for three corresponding levels are 1, 2, and 3. The numbers of equipment of each level for the design factors in Table 2 are subject to adjustment according to the setup costs, and the optimal results could be different.

Table 2. The design factors and their corresponding levels.

Design Factors		Level 1	Level 2	Level 3
Wind power	Q_W	1	2	3
PV power	Q_{PV}	3	4	5
Hydrogen tank	Q_{HT}	10	15	20
Fuel Cell	Q_{FC}	3	4	5
Electrolyzer	Q_E	2	3	4

Step 2. Using the proper orthogonal array

The Taguchi method significantly reduces the number of experimental configurations to be studied. Originally, there are $3^5 = 243$ experiments in the full factorial design, and the L_{18} orthogonal array can accommodate five three-level design factors in only 18 experiments to efficiently collect experimental results to find the optimized factor combination. The proposed L_{18} orthogonal array table is shown in Table 3.

Table 3. The orthogonal array of L_{18} .

L_{18}	Q_W	Q_{PV}	Q_{HT}	Q_{FC}	Q_E
1	1	1	1	1	1
2	1	2	2	2	2
3	1	3	3	3	3
4	2	1	1	2	2
5	2	2	2	3	3
6	2	3	3	1	1
7	3	1	2	1	3
8	3	2	3	2	1
9	3	3	1	3	2
10	1	1	3	3	2
11	1	2	1	1	3
12	1	3	2	2	1
13	2	1	2	3	1
14	2	2	3	1	2
15	2	3	1	2	3
16	3	1	3	2	3
17	3	2	1	3	1
18	3	3	2	1	2

Step 3. Calculating the initial result

According to the experimental combinations in the orthogonal array, Matlab is applied to generate the 18 different electric power generation system quantities in the stand-alone power system which could simulate 18 different systems, and calculate each electric power generation system quantity price and power shortage hours, respectively. The results are shown in Table 3.

Step 4. Calculating the per-unit values

The simulated experiment data cannot be compared or calculated for the unit reference value difference, thus it requires per-unit value calculation to get the physical quantity relative to the reference value [22]. The necessary equation is as shown in Equations (3) and (4).

Step 5. Establishing the matter-element

In extension theory, N is given as the name of an object for the definition of the object, and the quantity value of its character c is v . The orderly combination is taken as the fundamental element describing the object, namely the matter-element. The name of the object may not be expressed by the single matter-element, but expressed by the multi-dimensional matter-element. The multi-dimensional matter-element assumes the object has n characters respectively $c_1, c_2 \dots c_n$, and its corresponding quantity value is $v_1, v_2 \dots v_n$. Putting the above $S_{pu}^g(k)$ into v , the multi-dimensional matter-element expression is as shown in Equation (20), and the second group is placed after calculating the correlation functional value:

$$R_t = \begin{bmatrix} N & \beta_c(pu) & V_{t1} \\ & \beta_p(pu) & V_{t2} \end{bmatrix} \quad (20)$$

Step 6. Establishing the classical domain and neighborhood domain

In extension theory, the positional relation of one point to two sections must be considered. If $V_o = \langle a, b \rangle$ and $V_p = \langle c, d \rangle$ are two sections in the real domain, it shall firstly confirm the classical domain and the neighborhood domain before getting the matter-element in. Establishing the system's matter-element model, the defined classical domain is as Equation (21) and the neighborhood domain is as Equation (22). Defining the range according to the design factor demand, in extension theory, the classical domain is the expected value, and the neighborhood domain is the overall range.

$$R_o = \begin{bmatrix} \text{system} & \beta_p(pu) & \langle 0.7713, 1.1739 \rangle \\ & \beta_c(pu) & \langle 0.5181, 1.1242 \rangle \end{bmatrix} \tag{21}$$

$$R_p = \begin{bmatrix} \text{system} & \beta_p(pu) & \langle 0.1539, 1.1739 \rangle \\ & \beta_c(pu) & \langle 0.1827, 1.1242 \rangle \end{bmatrix} \tag{22}$$

Step 7. Calculating the correlation values

According to the definition of distance, we confirm the correlation function and use Equation (23) for assessment. If the value to be measured is within the classical domain, it shall be calculated by the method of Equation (23a); if the value to be measured is outside the classical domain, it shall be calculated in the method of Equation (23b) to get the correlation function.

$$K_i(v_i) = \begin{cases} \frac{-\rho(v_i, V_{oj})}{|V_{oj}|}, v_i \in V_{oj} \dots\dots (a) \\ \frac{\rho(v_i, V_{oj})}{\rho(v_i, V_{pj}) - \rho(v_i, V_{oj})}, v_i \notin V_{oj} \dots\dots (b) \end{cases} \tag{23}$$

The proposed extension relation function can be shown as Figure 5, where $0 \leq K(v) \leq 1$ corresponds to the normal fuzzy set. It describes the degree to which v belong to V . When $K(v) < 0$, it indicates the degree to which v does not belong to V .

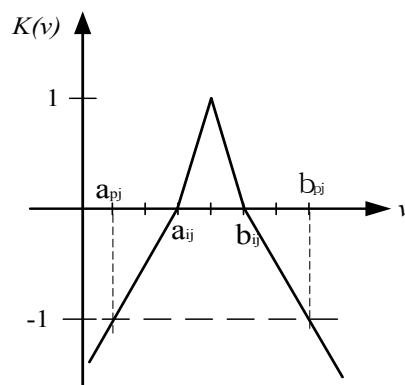


Figure 5. The proposed extension relation function.

Step 8. Comprehensive correlation degree

In the stand-alone power system, normally, the power shortage hours have higher priority than cost and the correlation degree function α_1 is set at 0.62 and α_2 is at 0.38 as in Equation (24), the result is given as shown in Table 4.

$$K(p) = \sum_{i=1}^n \alpha_j K_i(v_i) \tag{24}$$

Table 4. This research's level and design factor table.

L_{18}	β_P	Cost (USD)
1	0.35927	11,609
2	0.32500	16,162
3	0.27777	20,715
4	0.21527	15,110
5	0.15833	19,663
6	0.14305	15,777
7	0.10416	17,286
8	0.07316	17,150
9	0.08333	18,174
10	0.36388	18,022
11	0.33472	15,300
12	0.28055	15,164
13	0.19444	15,972
14	0.15972	16,775
15	0.18472	17,803
16	0.09444	19,711
17	0.09305	16,050
18	0.07638	16,853

Step 9. Average value analysis

Average value analysis uses the Taguchi method to calculate the influence of the factor effects to confirm the optimal factor combination by taking the average value analysis of levels for each factor by normalizing each level of comprehensive correlative degree of Table 5 according to the L_{18} orthogonal array grade in Table 4 to calculate the average value. The average value analysis is as shown in Equation (25), and the result is as shown in Table 6.

$$\bar{m} = \frac{1}{n} \sum_{i=1}^n K(p) \quad (25)$$

Table 5. Comprehensive Correlative Degree.

L_{18}	Comprehensive Correlative Degree
1	-0.02697
2	-0.15052
3	-0.74338
4	0.110458
5	-0.39659
6	0.162556
7	0.059634
8	0.068294
9	-0.07669
10	-0.45393
11	-0.45393
12	0.006634
13	0.064505
14	0.046478
15	-0.14816
16	-0.30322
17	0.216926
18	0.118986

Step 10. Solution of optimum system parameter

Through the analysis of factor effects, the maximum stand-alone power system optimum allocation can be selected through average value analysis of the Taguchi method as shown in Table 6.

Table 6. Optimum Parameters of the ETM.

Parameter	Load	Q_W	Q_{PV}	Q_{HT}	Q_{FC}	Q_E
Level	2	2	1	1	1	2
Optimum quantity	500 W	2	3	10	3	3

4. Simulated Result and Discussion

This study's simulation adopts the weather data of the Wuci area in central Taiwan in 2014, provided by Taiwan Central Weather Bureau, to compare the wind speed and the illumination of the winter and summer, as shown in Figures 6 and 7. The sun radiates directly on the Southern Hemisphere, and the illumination is small and the wind power is strong in Taiwan. The load power (PL), wind (pw) power and PV power (PPV) of the calculated optimum allocation are shown in Figure 8. If the amount is less than the generating capacity load, fuel cells will supply the load power, as shown in Figure 9. In summer, the load power (PL), wind (pw) power and PV power (PPV) of the calculated optimum allocation are also shown in Figure 10. If the amount is less than the generating capacity load, fuel cells power will be used to supply the load, as shown in Figure 11. In summer, the sun directly radiates on the Northern Hemisphere, the PV power increases in energy. However, there are usually windless situations in the summer, and the operation of the wind power generator is suspended during typhoon season, thus wind power generation shall decrease. Generally, during the daytime, solar energy is abundant and the use of the fuel cells is not required, and the system is able to produce hydrogen for extra needs. At night, there is no illumination, and only wind power generation provides energy. The fuel cells shall use the hydrogen to support the load. At night, in addition the home electricity usage increases, therefore, in the stand-alone power system, the fuel cell does not need much generating capacity, but needs more hydrogen tanks for standby to supplement the load demand.

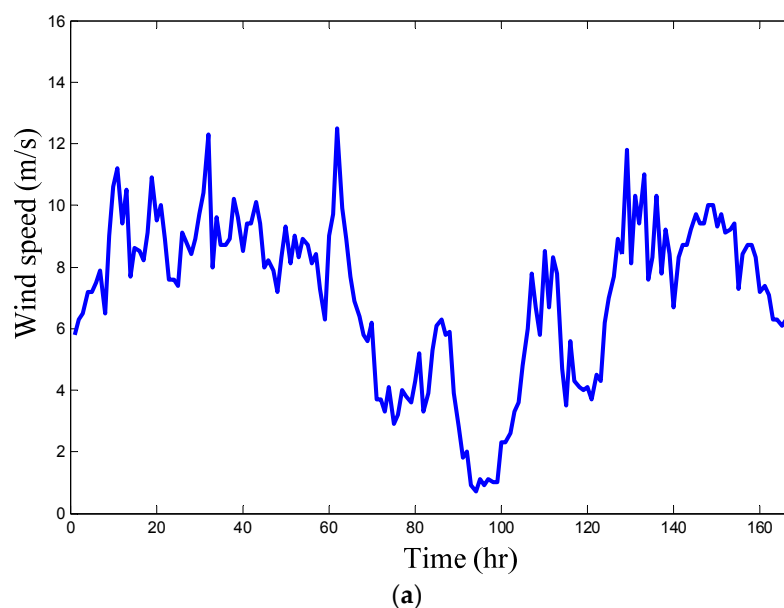


Figure 6. Cont.

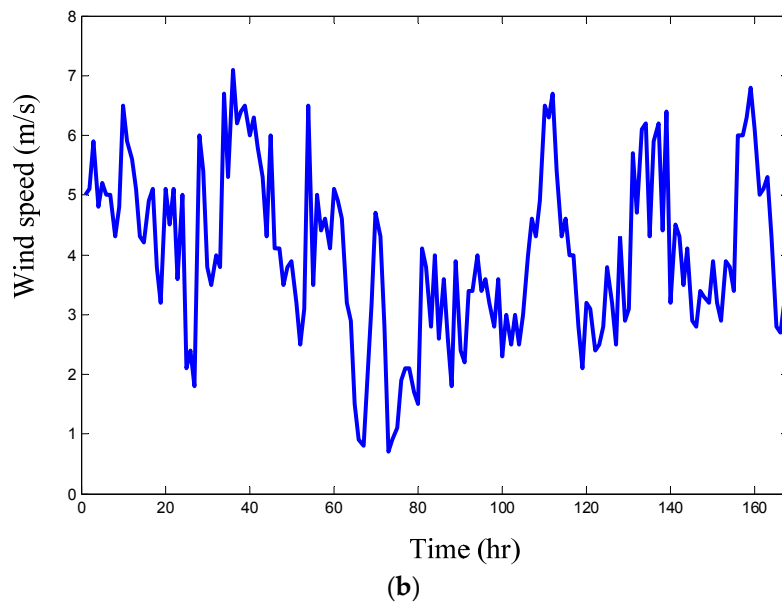


Figure 6. The curves of the typical weekly wind speed (a) winter; (b) summer.

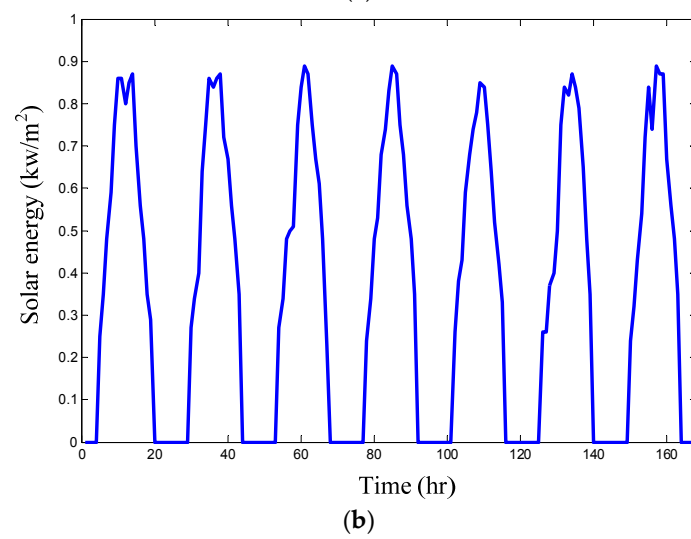
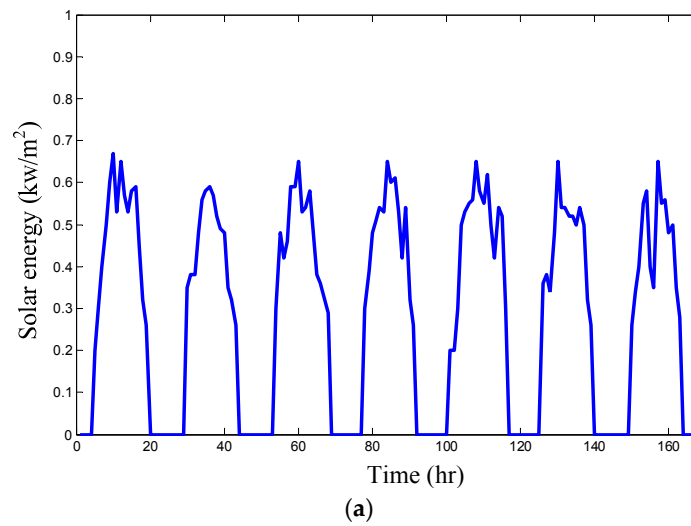


Figure 7. The curves of the typical solar illuminance (a) winter; (b) summer.

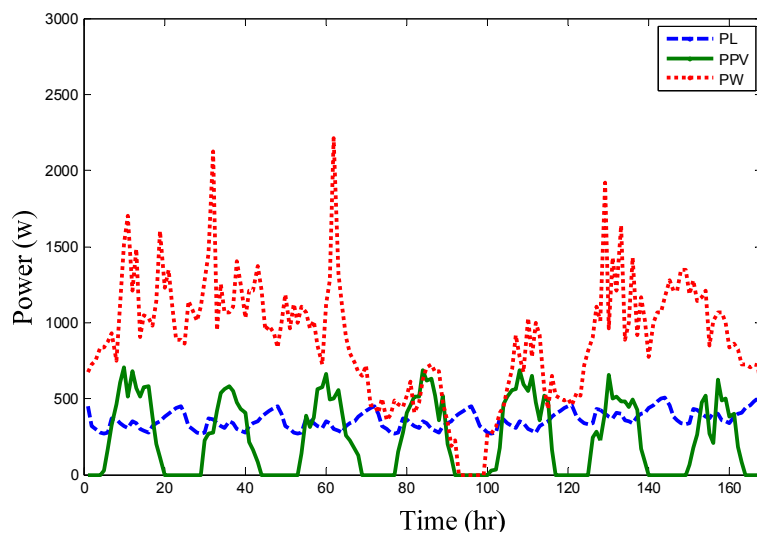


Figure 8. The power curves of the power system in the first week of December.

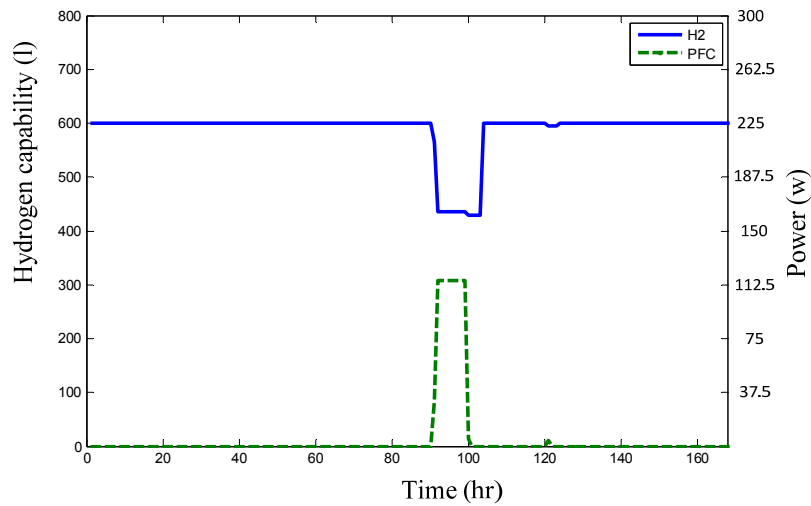


Figure 9. The curves of the hydrogen capability and fuel cell power in the first week of December.

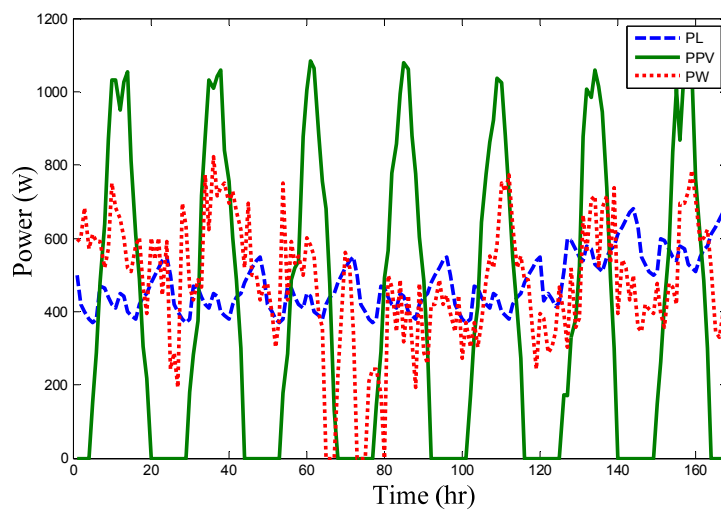


Figure 10. The power curves of the power system in the first week of June.

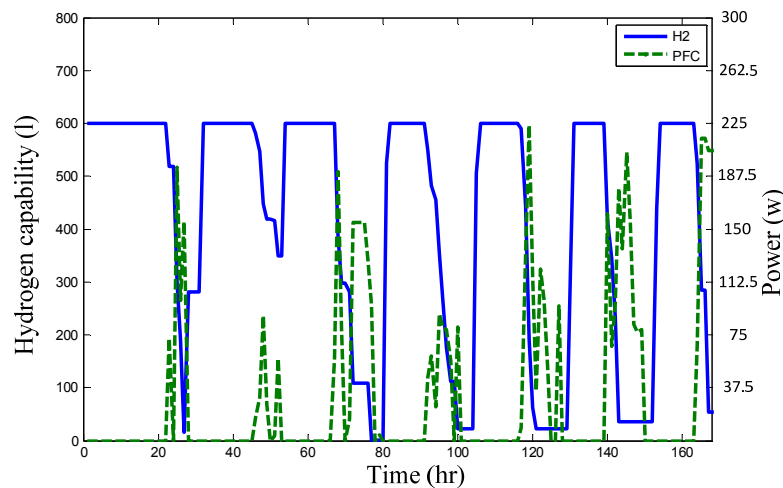


Figure 11. The curves of the hydrogen capability and fuel cell power in the first week of June.

The optimum allocation into the weekly and monthly average data shall be simulated to compare the probability of shortage allocated for the four types of algorithms, as shown in Figure 12.

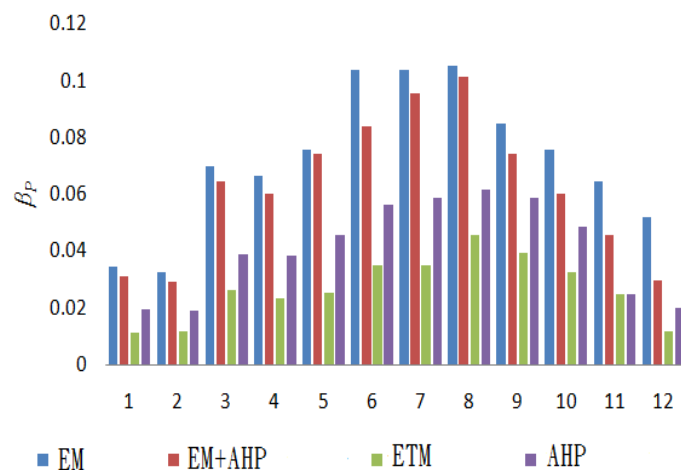


Figure 12. Annual Power Shortage Probability (LOLP).

The extension hierarchical method firstly adopts the extension classical domain and neighborhood domain, taking the matter-element to be measured to calculate the correlation function and extension distance, and forming the contrast matrix by the empirical law to establish hierarchical analysis method to conform to the requirement of consistency and gain weight. Comparing AHP and the Extension Taguchi Method (ETM), although the power shortage hours of AHP are good, the allocation of the ETM is better than with other optimum methods.

5. Conclusions

This study aims to compare the performance of the extension theory, extension AHP theory, ETM and Analytic Hierarchy Process (AHP) in determining the optimized capacity allocation of stand-alone power systems based on calculating the power shortage probability and construction cost. Through the experiments setting of orthogonal array, ETM is used to significantly reduce the number of experiments to efficiently verify the best factor combination for the capacity allocation. Results show that the ETM's allocation parameters are the best among all models, and the conclusion of this paper are as follows:

- (1) This paper proposes an optimum capability planning combining the extension theories and Taguchi method to solve the SAPS optimum problem; the proposed model reaches the optimal solution efficiently.
- (2) The proposed ETM needs to firstly specify the level and design factor. To guarantee the experimental results, the domain knowledge and expert experience are required when setting the design factors and their levels.
- (3) Since the specifications of commercial equipment are pre-specified, the optimum system allocation can be practically achieved by using the proposed ETM.
- (4) With fast computation speed, the proposed ETM can be easily applied to mathematical models with complicated objective functions and power systems, and the generated results could be directly implemented on practical equipment without further experimental adjustments.

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Conflicts of Interest: The authors declare no conflict of interest.

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