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Keywords: pore-scale simulations, Lattice Boltzmann method, microfractures, CT, digital rock

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Article

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Abstract: Microfractures have great significance in the study of reservoir development because they are an effective reserving space and main contributor to permeability in a large amount of reservoirs. Usually, microfractures are divided into natural microfractures and induced microfractures. Artificially induced rough microfractures are our research objects, the existence of which will affect the fluid-flow system (expand the production radius of production wells), and act as a flow path for the leakage of fluids injected to the wells, and even facilitate depletion in tight reservoirs. Therefore, the characteristic of the flow in artificially induced fractures is of great significance. The Lattice Boltzmann Method (LBM) was used to calculate the equivalent permeability of artificially induced three-dimensional (3D) fractures. The 3D box fractal dimensions and porosity of artificially induced fractures in Berea sandstone were calculated based on the fractal theory and image-segmentation method, respectively. The geometrical parameters (surface roughness, minimum fracture aperture, and mean fracture aperture), were also calculated on the base of digital cores of fractures. According to the results, the permeability lies between 0.071–3.759 (dimensionless LB units) in artificially induced fractures. The wide range of permeability indicates that artificially induced fractures have complex structures and connectivity. It was also found that 3D fractal dimensions of artificially induced fractures in Berea sandstone are between 2.247 and 2.367, which shows that the artificially induced fractures have the characteristics of self-similarity. Finally, the following relations were studied: (a) exponentially increasing permeability with increasing 3D box fractal dimension, (b) linearly increasing permeability with increasing square of mean fracture aperture, (c) indistinct relationship between permeability and surface roughness, and (d) linearly increasing 3D box fractal dimension with increasing porosity.

Keywords: CT; digital rock; microfractures; Lattice Boltzmann method; pore-scale simulations

1. Introduction

The study of fractures has great importance in performing the following tasks: (a) properly characterizing and developing fractured oil and gas reservoirs, (b) nuclear-waste repository

performance-assessment studies, (c) geothermal energy development, (d) studies of groundwater contamination, etc. In oil and gas development, microfractures are divided into natural microfractures and induced microfractures. Inducing fractures by hydraulic fracturing is one of the main methods to increase production. The existence of induced fractures will affect the fluid-flow system (expand the drainage radius of production wells), and act as flow paths for the leakage of fluids injected to the wells, and even facilitate depletion in tight reservoirs. Therefore, the characteristic of the flow in artificially induced fractures is of great significance.

Significant attention has been paid to the analysis of the microflow mechanism in fractures. The effect of fracture size and data uncertainties on fractured-rock permeability was analyzed by Sagar et al. [1]; the parameters influencing the interaction among closely spaced hydraulic fractures were reported by Bungler [2]; the hydraulic conductivity of rough fracture surface was studied by References [3–5]. It is well known that the flow in fractures is influenced by many factors [6], such as: (1) flow behavior through single fractures, (2) fracture network pattern, and (3) in situ stress system. It can be found that the induced fractures are composed of many intersected single fractures. The flow and stress-coupling characteristics of a rock depend largely on the behavior of the fluid flowing through a single fracture. Hence, the study of fluid flow through single fractures is essential.

Research on the flow through single fractures has been extensive and has led to a general understanding that the fractures in reservoirs are usually rough and it is impossible to put forward a fixed value of a fracture aperture. Therefore, the validity of the cubic law [7] is inappropriate for this case.

$$Q/\Delta h = \frac{\gamma}{12\mu} \frac{w}{L} b^3 \quad (1)$$

where Q , w , b , L , Δh , γ , and μ represent the linear fluid-flow rate, fracture width, fracture aperture, fracture length, total hydraulic head drop along the length of the fracture, weight of the flowing fluid, and the dynamic viscosity of the flowing fluid, respectively.

For rough fractures, various methods have been proposed. The roughness was incorporated into cubic-law simulations by many studies [8–10]: fractal theory was used to generate fracture models with different roughness [11], and the aperture of the idealized parallel smooth fracture was also replaced by the hydraulic aperture in many reports [12–14]. But so far none of these methods is unanimous.

The Lattice Boltzmann method (LBM) is a discrete approximation of the incompressible Navier–Stokes (N-S) equations based on kinetic theory [15]. This method is becoming a strong tool to simulate fluid flow in complex geometries. Besides, numerous studies extended LBM to perform the simulations from a microscale to a macroscale, which made it possible for LBM to be widely used. LBM has also been used to analyze the influence of wettability on fluid flow based on an ideal model [16] or generated self-affine rough fracture [17]. However, there were few reports on fluid-flow simulations in real three-dimensional (3D)-induced rough fractures based on LBM. A characterization of the flow simulations considering real rough-walled fractures is significant to many studies, such as the mechanical properties and transport properties of fractures [18].

Researchers made use of many techniques to obtain the structure of fractures in rocks, such as stylus profilometers [19,20], surface laser scanning [21,22], nuclear magnetic-resonance imaging [14,23], and computed tomography (CT) scanning [3,24,25]. CT scanning and nuclear magnetic-resonance imaging are two methods by which we can get the structure of fractures without destroying the core.

The CT scanning method, which is known as X-ray computed tomography, can detect the inner structure of nontransparent objects without damage. Because the different components of the rock have different densities, which result in different X-ray absorption coefficients, the skeleton and pore space of rocks can be distinguished. CT scanning was applied widely on the characterization of fractures [26–30]. OP Wennberg et al. scanned the core samples to investigate the effect of natural open fractures on reservoir flow [31]; precise 3D numerical modeling was coupled with X-ray CT to analyze the heterogeneous fracture flow as well as measure porosity and permeability [32]. The X-ray

CT scanning experiment is the most accurate and direct method for establishing a 3D digital core, which provides a basis for quantitative analysis and flow simulation of fractures.

In this study, LBM is used to simulate single-phase fluid flow through nine 3D actual fractures and calculate the equivalent permeability of the digital cores. Based on fractal theory, the fractal dimensions of artificially induced fractures in Berea sandstone are calculated. The geometric parameters (porosity, surface roughness, and mean fracture aperture) of the digital cores were calculated. Besides, the following relations were studied: (a) permeability versus 3D box fractal dimension in induced fractures, (b) permeability versus surface roughness, (c) permeability versus mean fracture aperture, and (d) 3D box fractal dimension versus porosity, etc. Finally, partial least square (PLS) regression was applied to observe the marginal effect of each independent variable (3D box fractal dimension, mean fracture aperture, surface roughness and minimum fracture aperture) in explaining permeability.

2. Methodology

2.1. The 3D Digital Core

The 3D digital core is a 3D digital image of the rock, which reflects the microscopic pore structure of the rock on the pore scale. In 2003, Dvorki et al. put forward the concept of Digital Rock Physics (DRP) technology, which is based on the 3D digital core and uses the numerical simulation algorithm to accurately calculate the acoustic, electrical, nuclear magnetic resonance, and seepage characteristics of the rock [33]. Compared to petrophysics experiments, DRP experiments are fast and low in cost. They can simulate different rock physical properties based on the same 3D digital core, and it is easy to analyze the correlation between different physical attributes.

The common methods for constructing a 3D digital core are divided into two types: an X-ray CT-scanning experiment and reconstruction method based on a couple of two-dimensional (2D) images. The reconstruction method based on 2D images is not accurate when compared with an X-ray CT-scanning experiment because the 2D images contain less information of the pore structure. The X-ray CT-scanning experiment is the most accurate and direct method for establishing a 3D digital core, although the capacity of pore recognition is limited by the resolution of the instrument. The schematic diagram is shown in Figure 1.

An X-ray CT-scanning experiment was conducted to construct the 3D digital cores of the fractured cores, which are Berea sandstones with an induced fracture. The fracture was artificially induced using a modified Brazilian technique, which was created by Karpyn et al. [34].

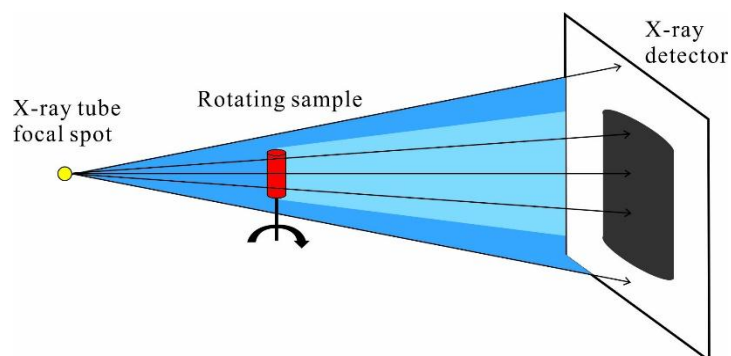


Figure 1. Schematic plot of X-ray micro-CT setup.

2.2. Fractal Theory and Fractal Dimension

2.2.1. The Concept of “Fractals”

In 1967, Mandelbrot published the title of "How long is the British coastline?" in the journal Science [35]. Comparing the photo of 100 kilometers of the coastline in the air to the enlarged

10 kilometers of the coastline, he found that the two pictures were very similar; Mandelbrot called the part, similar to the whole phenomenon, as the “Fractal”.

Fractals include regular fractals and irregular fractals. Regular fractals can be generated by simple iterations or by certain rules, such as the Cantor set and Koch curve; the self-similarity and scaling invariance of the regular fractal are theoretically infinite. Irregular fractals refer to randomly generated nonsmooth fractal objects that have statistical self-similarity. Porous media are a kind of irregular fractal object, the fractal research of which has been various [36–40].

2.2.2. The Box-Counting Method and Fractal Dimension

The box-counting method is one of the most familiar methods of calculating the fractal dimension. In the past 20 years, the box-counting method has been applied to various subjects, such as medical studies, physical studies, and chemical studies.

The box-counting method is implemented by covering the function with a grid of identical square boxes and counting the number of boxes intersecting the function as a function of the box size [41,42].

$$N(r) = \frac{1}{r^{D_f}} = r^{-D_f} \quad (2)$$

$$D_f = \frac{\ln N(r)}{\ln(1/r)} \quad (3)$$

In Equation (3), D_f is called the fractal dimension (also called Hausdorff dimension); the fracture is covered with different box sizes r , and the resulting number of boxes $N(r)$, and the corresponding box sizes can be used to compute the fractal dimension.

Fractal dimension is the most important concept and content in fractal theory, and which is proposed by Mandelbrot for the study of complexity and the nondifferentiability (at everywhere) of surface curves. Fractal dimension is the main tool to characterize the complex structure of the fractal object, and the introduction of which is the novelty of fractal theory. It can be easily noticed from existing fractal research that the relationship between the fractal dimensions of the research objects and other physical parameters is the focus of many studies [43,44].

The 2D box fractal dimension was extended to 3D in this work to fully characterize fractures, and then 3D fractal dimensions of artificially induced fractures in Berea sandstone were calculated.

2.3. The Calculating of Permeability by LBM

The LBM is applied to the numerical simulations of different physical phenomena and is the primary domain of application is fluid dynamics. The advantage of the LBM is based on its ability to easily simulate complex practical problems in simulation. To calculate the dimensionless equivalent permeability of fractures by LBM, the binary data of digital cores were the input file of the program.

In the present work, the D3Q19 lattice model was used [45]. Where D represents the space dimension, Q represents the number of discrete velocity vectors. The distribution function, $f_i(x)$ (at each site x , for each lattice vector e_i), stands for the average movement of fluid particles. Figure 2 illustrates the numerical model of LBM. The Lattice Bhatnagar–Gross–Krook (LBGK) approximation was applied for distribution function at time t [45]:

$$f_i(x + e_i\Delta t, t + \Delta t) - f_i(x, t) = -\frac{1}{\tau} [f_i(x, t) - f_i^{\text{eq}}(x, t)] \quad (4)$$

The left part of Equation (4) represents the streaming step, while the right represents the collision in the evolution of the distribution function. $f_i^{\text{eq}}(x, t)$ is the equilibrium distribution function, and τ is the relaxation parameter.

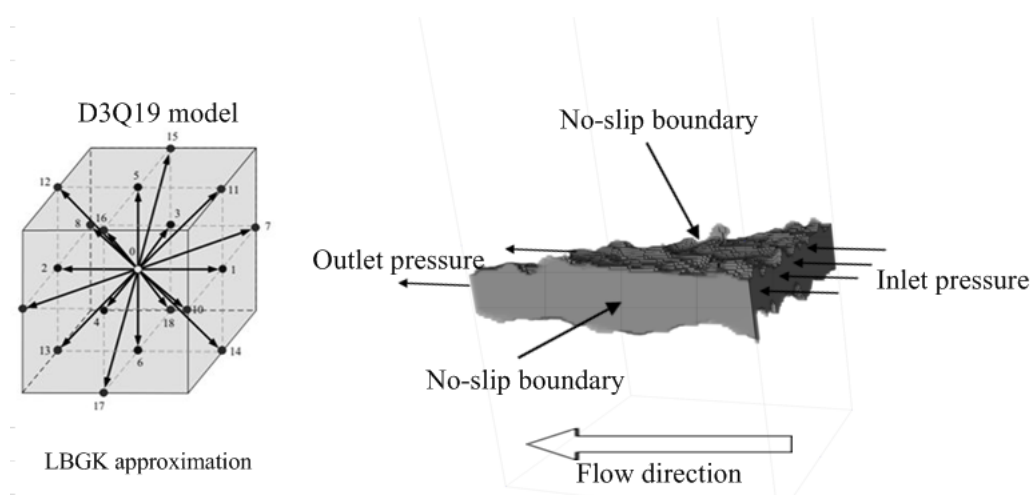


Figure 2. The numerical model of the lattice Boltzmann method (LBM) (The lattice Bhatnagar–Gross–Krook (LBGK) approximation was applied).

$$\tau = \frac{\nu}{c_s^2 \Delta t} + 0.5 \quad (5)$$

where ν and c_s represent the kinematic viscosity of fluid and the lattice pseudo-sound-speed, respectively. And the value of c_s is $\frac{1}{\sqrt{3}}$.

According to the incompressible LBM [46], the equilibrium distribution function for model D3Q19 is:

$$f_i^{\text{eq}}(x) = \omega_i \left[\rho(x) + \rho_0 \left(3(e_i \cdot u) + \frac{9}{2}(e_i \cdot u) - \frac{3}{2}(u \cdot u) \right) \right] \quad (6)$$

where ρ_0 is the mean density and ω_i is the weight factor in i -th direction. ω_i for D3Q19 is specified as:

$$\omega_i = \begin{cases} 1/3, & i = 0, \\ 1/18, & i = 1, 2, 3, 4, 5, 6, \\ 1/36, & i = 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18 \end{cases} \quad (7)$$

And the fluid macroscopic density (ρ) and velocity (u) at a node x , are defined as:

$$\rho(x) = \sum_{i=0}^{18} f_i(x) \quad (8)$$

$$u = \frac{1}{\rho(x)} \sum_{i=0}^{18} f_i(x) e_i \quad (9)$$

Besides, the pressure in the calculating of LBM is defined as:

$$p(x) = c_s^2 \rho(x) \quad (10)$$

In this work, the single-phase fluid is driven by pressure difference, which is realized by setting the inlet and outlet pressure as fixed values. As represented in Figure 2, the pressure-boundary condition was set on inlet surface and outlet surface, and the pressure gradient was 0.00005 for all fractures. Using the segmented images as input data, the walls of the porous medium are converted to bounce-back boundary conditions. A bounce-back scheme is a common scheme for dealing with no-slip boundaries. In this scheme, when the particle reaches the wall node, the particle will return to the fluid node along the original path, and the direction is opposite to the incident direction. It is worth

noting that particles do not collide on the wall. The bounce-back scheme is very easy to implement, and is suitable for handling systems with complex geometry [47].

The steady state is reached by checking the velocity and density of the fluid in fracture every 1000 steps, until the difference between the 2 adjacent times is less than 10^{-6} . According to Darcy's law, Equation (11), the equivalent permeability of the induced fracture in Berea sandstone was calculated.

$$-\frac{dP}{dx} = \frac{\mu}{k} U \quad (11)$$

3. Results and Discussion

3.1. The Digital Rocks of Fractures

The digital rocks presented in this study are Berea sandstone (with an induced fracture), which were downloaded in the sharing portal [48]. The core samples were prepared in such a way that the images are denoised and smoothed, then fractures were segmented by the multithresholding segmentation method, and the results are shown in Figure 3.

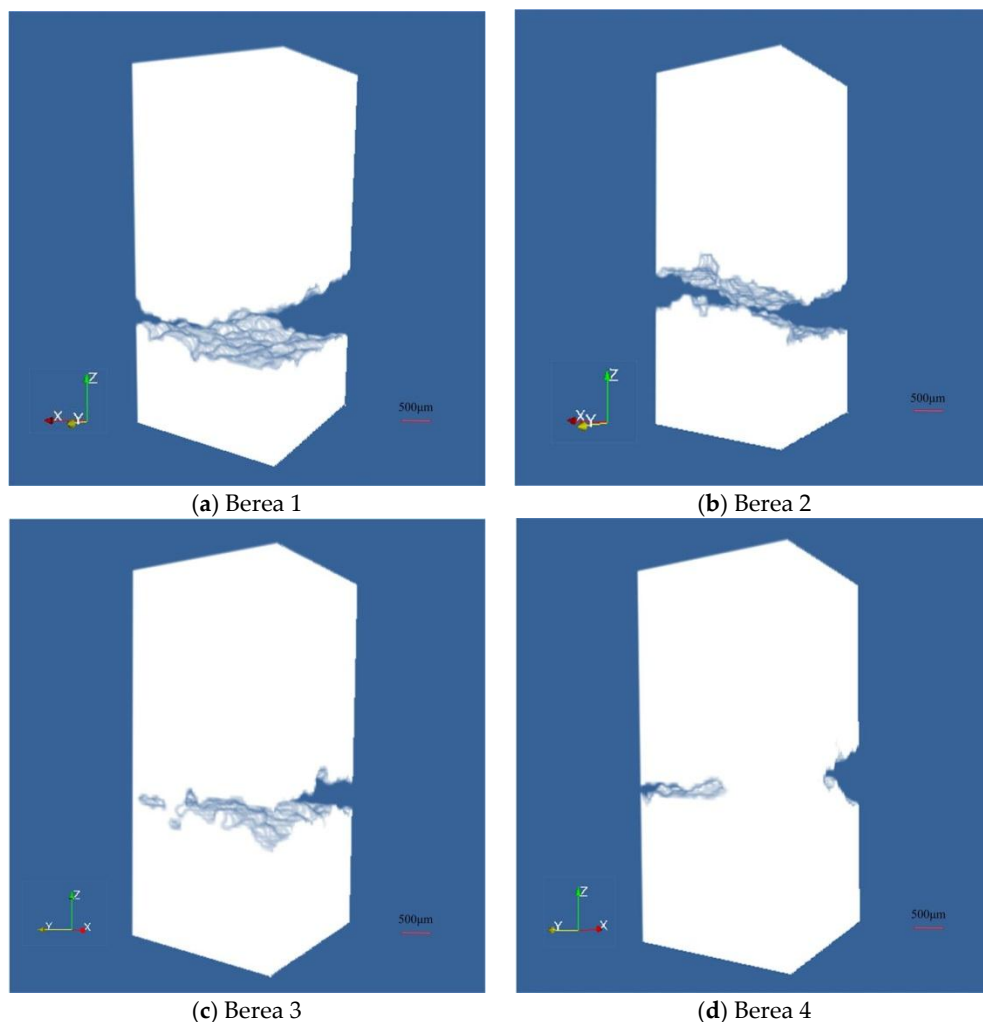


Figure 3. Cont.

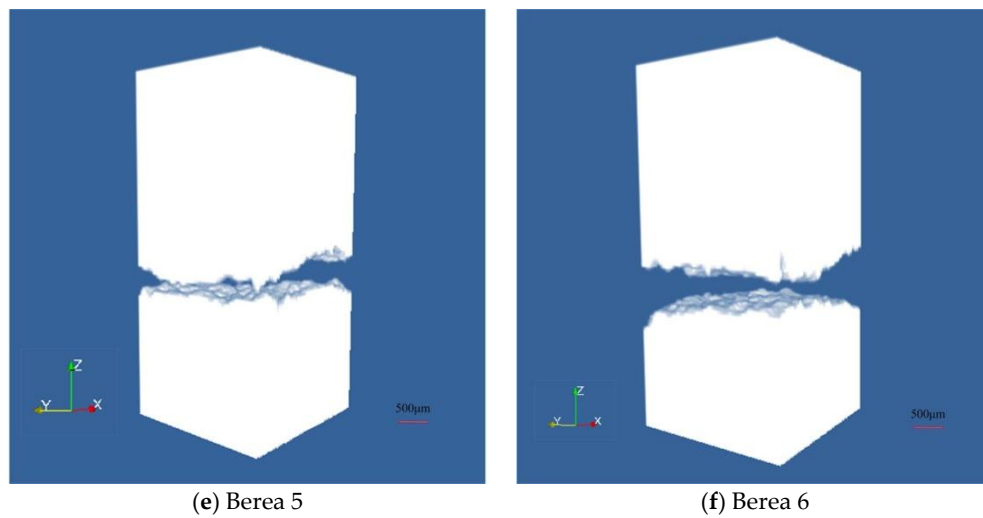


Figure 3. Digital cores of Berea sandstone with induced fracture (the size of every digital core is $2.743 \times 2.743 \times 6.035 \text{ mm}^3$), (a) Berea 1 to (f) Berea 6 are samples of all nine digital cores; their aperture and roughness are totally different.

The minimum aperture values, the mean aperture values, surface roughness, and the fracture porosity (which is the ratio of fracture volume to total volume) of all the fractures are shown in Table 1.

Tamura et al. generalized six image texture features related to human visual perception. Roughness is one of them, and its ability to describe texture is very strong. It has more application value in texture synthesis, image analysis and recognition, color migration, and so on. The calculation method of surface roughness came from his article [49].

Table 1. The minimum aperture values, mean aperture values, and fracture porosity of all the fractures.

Core Sample	Porosity	Minimum Fracture Aperture/Pixels	Mean Fracture Aperture/Pixels	Surface Roughness/Pixels
Berea 1	0.111	7	24.4	8.962
Berea 2	0.082	2	18.4	8.568
Berea 3	0.068	0	15.0	7.865
Berea 4	0.067	0	14.7	7.892
Berea 5	0.093	2	20.5	8.424
Berea 6	0.100	8	21.9	8.384
Berea 7	0.117	7	25.7	9.141
Berea 8	0.088	6	19.3	7.972
Berea 9	0.106	8	23.3	8.743

3.2. Fractal Dimension Calculating of Fractures

The digital cores shown in Section 3.1 were used to calculate the fractal dimensions of different fractures. It is noticeable that the 3D box fractal dimension was the fractal dimension of fracture, which was carried out by inverting the pore phase and skeleton phase in Figure 3, and then obtaining the structure of complete fracture, as shown in Figure 4, and Tables 2 and 3:

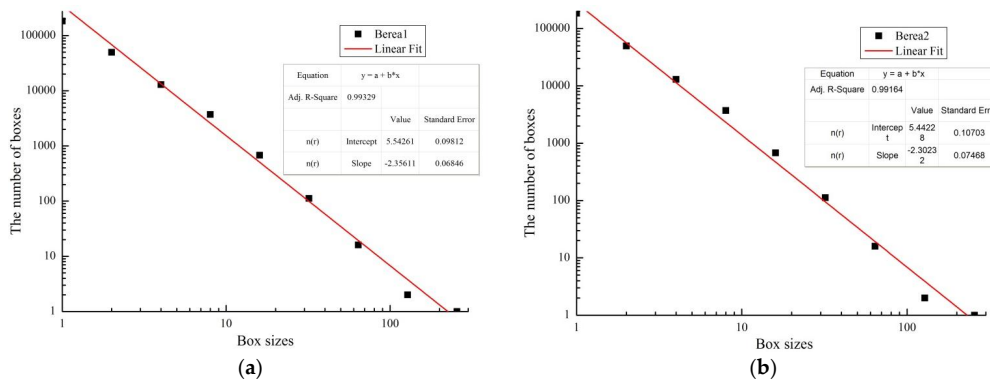


Figure 4. Fractal dimension calculating of (a) Berea 1 and (b) Berea 2.

Table 2. Statistical results of 3D box fractal dimensions.

r	1	2	4	8	16	32	64	128	256
Berea 1	243,739	64,473	14,952	3899	682	112	16	2	1
Berea 2	184,084	49,754	12,946	3714	679	112	16	2	1
Berea 3	149,777	40,921	10,970	3302	640	104	16	2	1
Berea 4	146,858	39,713	9936	2982	637	107	16	2	1
Berea 5	205,178	54,841	13,687	3751	685	112	16	2	1
Berea 6	219,441	58,328	14,339	3866	685	112	16	2	1
Berea 7	256,973	67,771	15,537	4025	686	112	16	2	1
Berea 8	193,450	51,953	13,339	3734	686	112	16	2	1
Berea 9	232,925	61,929	14,801	3926	686	112	16	2	1

Table 3. 3D box fractal dimension of Berea with an induced fracture.

Core Sample	Berea 1	Berea 2	Berea 3	Berea 4	Berea 5	Berea 6	Berea 7	Berea 8	Berea 9
3D Box Fractal Dimension	2.356	2.302	2.259	2.247	2.323	2.337	2.367	2.312	2.349

3.3. The Permeability of Fractures

The streamlines of induced fractures are shown in Figure 5, and the permeability of induced fractures in Berea sandstone is obtained in Table 4. It should be noted that all units in this work are nondimensional LB units.

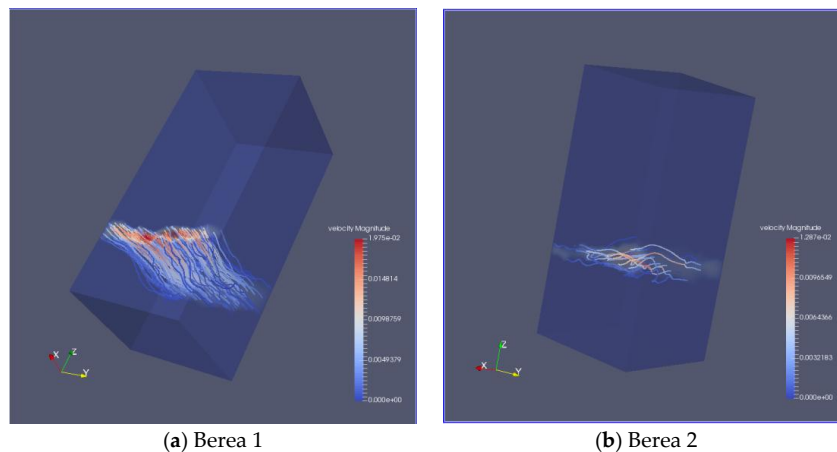


Figure 5. Cont.

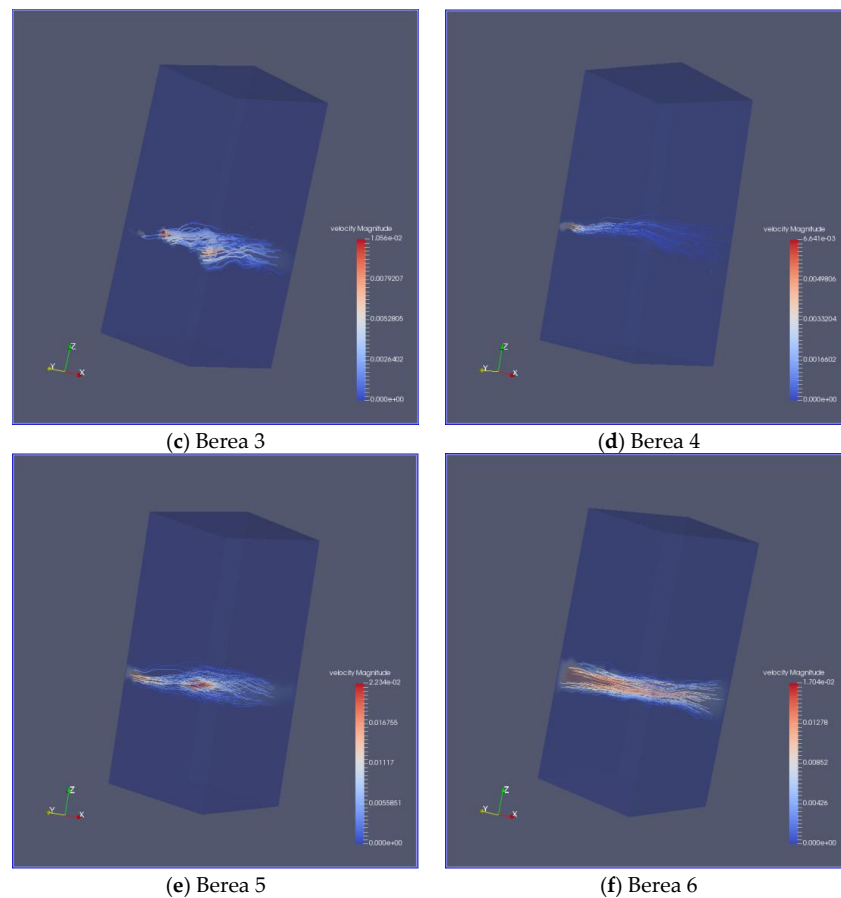


Figure 5. The streamlines of induced fractures in Berea.

Table 4. The permeability of Berea with an induced fracture.

Core Sample	Berea 1	Berea 2	Berea 3	Berea 4	Berea 5	Berea 6	Berea 7	Berea 8	Berea 9
Permeability	1.903	0.820	0.300	0.071	1.183	2.108	3.759	1.492	2.852

3.4. The Relations of Permeability and Other Parameters

Fluid flow through a single fracture was determined by spatial distribution of fracture aperture, which can be quantified by fractal parameter, mean aperture, or surface roughness. So we study the functional relations between (a) permeability and 3D box fractal dimension, (b) permeability and surface roughness, (c) permeability and mean fracture aperture, (d) 3D box fractal dimension and porosity, and (e) 3D box fractal dimension and mean fracture aperture.

3.4.1. Permeability versus 3D Box Fractal Dimension

The correlation between permeability and 3D box fractal dimension is widely studied; Ju et al. investigated the mechanism of fluid flow through a single rough fracture of rocks, and a nonlinear relationship between the fractal equivalent permeability of a single fracture and the fractal dimension D of its rough structure [11]. They generated a single fracture based on the Weierstrass–Mandelbrot fractal function. The relationship between permeability and 3D box fractal dimension obtained in this work is different from theirs, which is shown in Figure 6:

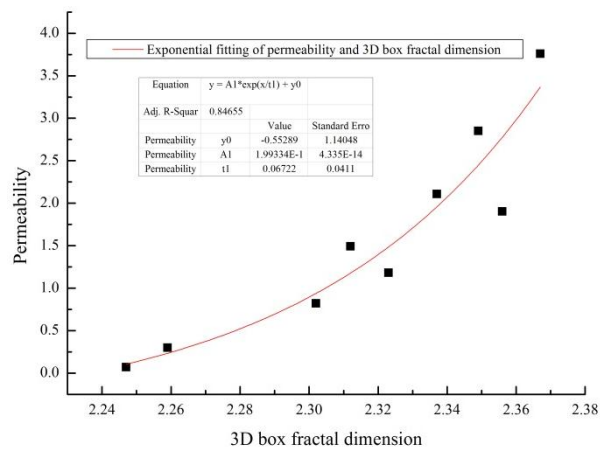


Figure 6. The relationship between permeability and 3D box fractal dimension.

The equivalent permeability (dimensionless LB units) of induced fracture, k_{LB}^{equ} , increase exponentially with the increasing of 3D box fractal dimension, FD_{3d} . The equation between permeability and 3D box fractal dimension obtained is:

$$k_{LB}^{equ} = e^{-10.32+14.92FD_{3d}} - 0.553 \tag{12}$$

3.4.2. Permeability versus Surface Roughness

The relationship between permeability and surface roughness is shown in Figure 7. The roughness of natural rock fractures is a topic of interest to many researchers, including rock hydrogeologists, geochemists, and geophysicists. The complexity of fracture morphology (the roughness and variability in fracture aperture) is the fundamental property that keeps fractures open and makes flow through fractures significant and important to subsurface fluid flow. Nevertheless, this parameter is hard to measure and determine [49].

Tayfun et al. found that surface roughness of fracture walls had a critical effect on the hydraulic conductivity of a fracture [50]. The hydraulic conductivity ratio also shows decreasing trend with increasing fracture surface roughness.

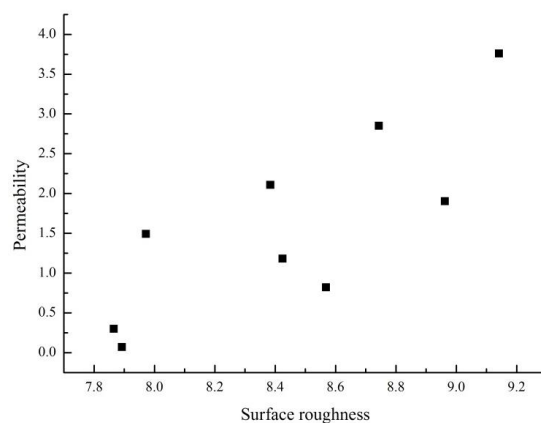


Figure 7. The relationship between permeability and surface roughness.

However, in this study, the relationship between permeability and surface roughness is indistinct in Berea sandstone with an induced fracture and the permeability shows an increasing trend with the increase of surface roughness. This is because of the difference between real fractures and the artificially generated fracture by the Weierstrass–Mandelbrot fractal function. Real fractures have

no fixed aperture, and the roughness of fractures with a different aperture is varied, which results in increasing permeability with the increase of surface roughness. In large part, it is caused by the influence of other factors, for instance, the mean fracture aperture on permeability. As shown in Section 3.6, the influence of surface roughness on a dependent variable is much weaker compared with the square of mean fracture aperture and minimum fracture aperture.

3.4.3. Permeability versus Mean Fracture Aperture

Although it is impossible to put forward a fixed value of fracture aperture, the relationship between permeability and mean fracture aperture is still worth analyzing, as illustrated in Figure 8. It is generally known that the relationship between permeability and the square of mean fracture aperture for a horizontal flat-plate model is:

$$k^{equ} = \frac{b^2}{12} \quad (13)$$

where k^{equ} is the equivalent permeability of the horizontal flat-plate model.

So the relationship between permeability and the square of mean fracture aperture is studied in the following figure:

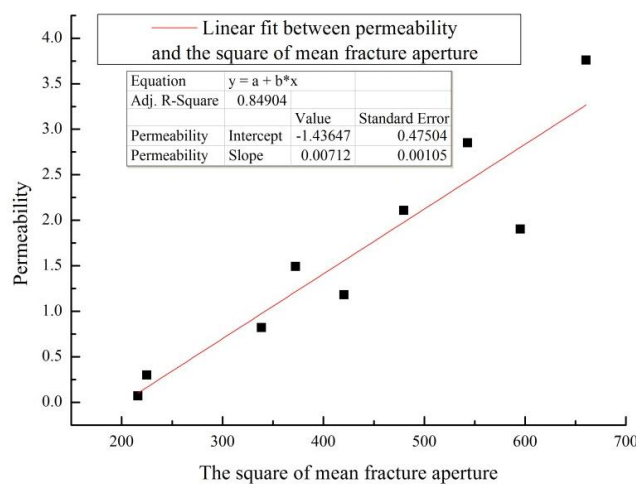


Figure 8. The relationship between permeability and the square of mean fracture aperture of Berea sandstone with an induced fracture.

Figure 8 shows a very strong linear relation between permeability and mean fracture aperture, which illustrates that the equivalent permeability of real fractures is proportional to the square of the mean fracture aperture. High R^2 also indicates that there is a strong correlation between permeability and the square of mean fracture aperture.

3.4.4. Permeability versus Minimum Fracture Aperture

In Figure 9, the relationship between permeability and minimum fracture aperture is shown. Minimum fracture aperture has a significant impact on the flow because, the smaller the minimum fracture aperture is, the greater the pressure drops. From Figure 9 we can also conclude that permeability increases with the increasing minimum fracture aperture.

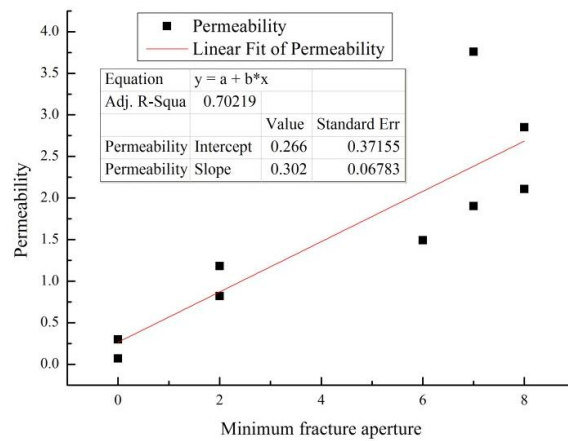


Figure 9. The relationship between permeability and minimum fracture aperture of Berea sandstone with an induced fracture.

3.5. The Relationship of 3D Box Fractal Dimension and Other Parameters

To characterize the spatial distribution of fracture aperture, the 3D box fractal dimension, FD_{3d} , was used to characterize 3D artificially induced fractures in Berea sandstone. The relationship of 3D box fractal dimension and other parameters was analyzed below.

3.5.1. 3D Box Fractal Dimension versus Porosity

Figure 10 displays the curve of the 3D box fractal dimension versus porosity, which shows that the 3D box fractal dimension increases linearly with increasing porosity.

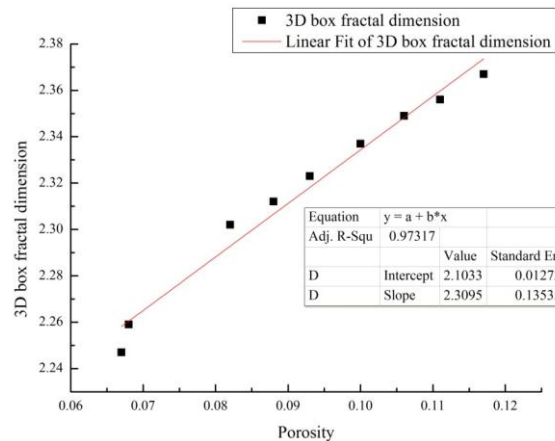


Figure 10. The relationship between the 3D box fractal dimension and porosity of Berea sandstone with an induced fracture.

The figure shows a very strongly linear relation between the 3D box fractal dimension and porosity (R^2 value is greater than 0.97). The standard errors of slope and intercept of the linear relationship lie in a small range.

3.5.2. 3D Box Fractal Dimension versus Mean Fracture Aperture

In the previous sections, it was found that the relationship between 3D box fractal dimension and porosity is strongly linear, and the relationship between permeability and mean fracture aperture is almost the same as the relationship between permeability and porosity, as shown in Figure 11.

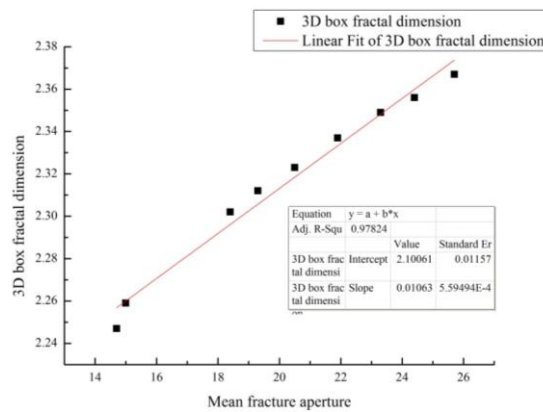


Figure 11. The relationship between 3D box fractal dimension and mean fracture aperture.

It is not difficult to see that the R^2 value of the relationship between 3D box fractal dimension and mean fracture aperture is even larger than that of 3D box fractal dimension and porosity, which indicates that mean fracture aperture has a great impact on 3D box fractal dimension.

3.5.3. 3D Box Fractal Dimension versus Surface Roughness

Surface roughness may have a great impact on 3D box fractal dimension because more boxes are counted by the box-counting method if surface roughness is larger. The relationship between 3D box fractal dimension and surface roughness of Berea sandstone with an induced fracture is shown in Figure 12.

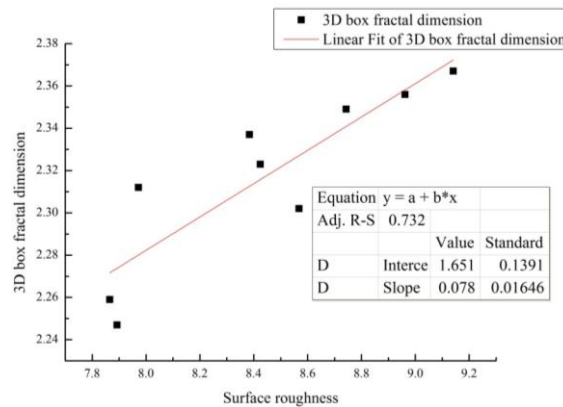


Figure 12. The relationship between 3D box fractal dimension and surface roughness of Berea sandstone with an induced fracture.

The Figure 12 shows that 3D box fractal dimension increases with the increasing surface roughness in Berea sandstone; however, a good linear fit was not achieved ($R^2 = 0.733$).

3.6. PLS Regression

In order to observe the marginal effect of each independent variable in explaining permeability more quickly and intuitively, we can draw a regression coefficient map, as shown in Figure 13, which is based on regression equation for standardized data.

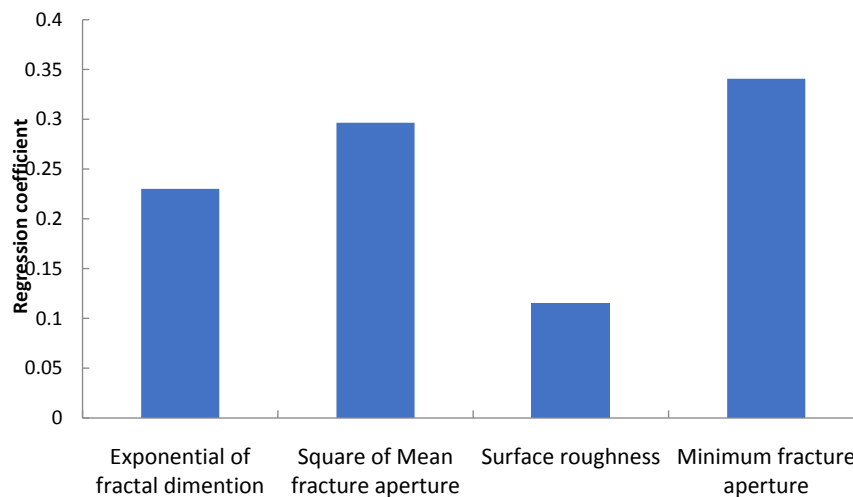


Figure 13. Regression coefficient map based on regression equations for standardized data.

It can be observed from the regression coefficient diagram that the minimum fracture aperture and square of mean fracture aperture play a very important role in explaining the regression equation. At the same time, it can be seen from the Figure 13 that the influence of surface roughness on dependent variable is weaker than other variables, which indicates that the permeability of real fractures is more strongly affected by other parameters.

In order to investigate the accuracy of the regression equation model, we used $(\hat{k}_{LB}^{equ}, k_{LB}^{equ})$ as the coordinate values to draw the prediction map for all the sample points. \hat{k}_{LB}^{equ} was the predicted value of the sample point (k_{LB}^{equ}) . As shown in Figure 14, all points are evenly distributed near the diagonal of the graph, the difference between the fitting value of the equation and the original value is very small, and the fitting effect of the equation is satisfactory.

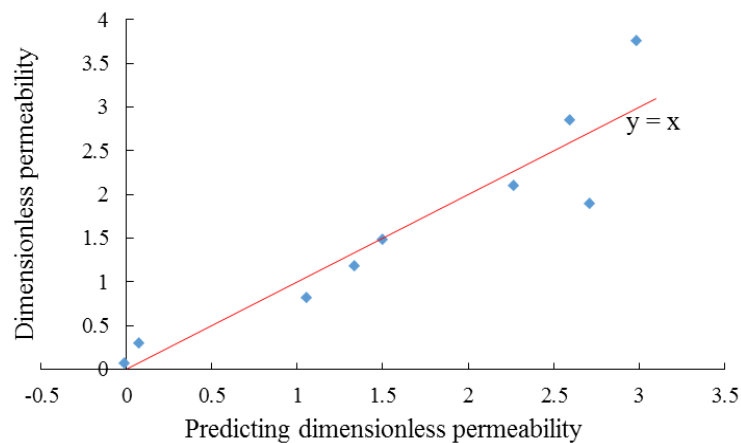


Figure 14. The fitting value of the equation versus the original value.

The regression equation is:

$$k_{LB}^{equ} = -9.0185 + 0.6541 \exp(FD_{3d}) + 0.0023\bar{b}^2 - 0.2945Ra + 0.1198b_{\min} \quad (14)$$

where \bar{b} , Ra and b_{\min} represent mean fracture aperture, surface roughness, and minimum fracture aperture, respectively.

4. Conclusions

(1) Artificially induced fractures were studied in this work, and their geometrical parameters (porosity, surface roughness, minimum fracture aperture, and mean fracture aperture) were calculated. 3D box fractal dimension of fractures was also calculated; it was found that a 3D box fractal dimension is between 2.247–2.367, which shows that the artificially induced fractures have the characteristics of self-similarity.

(2) LBM was used to compute the permeability of artificially induced fractures; the permeability was between 0.071–3.759 (dimensionless LB units). The difference in permeability indicates that artificially induced fractures have complex structures.

(3) The following relations have been identified: (a) exponentially increasing permeability with increasing 3D box fractal dimension in induced fractures, (b) linearly increasing permeability with increasing square of mean fracture aperture, (c) indistinct relationship between permeability and surface roughness, and (d) linearly increasing 3D box fractal dimension with increasing porosity, mean fracture aperture, and surface roughness.

(4) By PLS regression, it can be concluded that minimum fracture aperture and mean fracture aperture play a significant role in explaining the fracture permeability. The influence of surface roughness on dependent variables is much weaker compared with the square of mean fracture aperture and minimum fracture aperture. Besides, the regression equation was obtained, and the fitting result of which was satisfactory.

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