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The Switched Reluctance Generator (SRG) is suitable for wind power generation due to its good reliability and robustness. However, The SRG system adopting the conventional control algorithm with Pulse Width Modulation (PWM) method has a drawback, low response speed. The pulse train (PT) control has been widely used in dc/dc power converters operating in the discontinuous conduction mode due to its advantages of simple implementation and fast response. In this paper, for the first time, the PT control method is modified and adopted for controlling the output voltage of SRG system in order to achieve fast response. The capacitor current on the output side is sampled and combined with the output voltage to select the pulse trains and the low frequency oscillation cased by PT can be suppressed by tuning the feedback coefficient of the capacitor current. Also, good performance can be guaranteed with a wide range of voltage regulations, fast response, and no overshoot. The experimental platform of an 8/6 SRG system is built, and the experimental results show that the PT control can be used for SRG system with good practicability.

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Article

# Improvement of the Response Speed for Switched Reluctance Generation System Based on Modified PT Control

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Abstract: The Switched Reluctance Generator (SRG) is suitable for wind power generation due to its good reliability and robustness. However, The SRG system adopting the conventional control algorithm with Pulse Width Modulation (PWM) method has a drawback, low response speed. The pulse train (PT) control has been widely used in dc/dc power converters operating in the discontinuous conduction mode due to its advantages of simple implementation and fast response. In this paper, for the first time, the PT control method is modified and adopted for controlling the output voltage of SRG system in order to achieve fast response. The capacitor current on the output side is sampled and combined with the output voltage to select the pulse trains and the low frequency oscillation cased by PT can be suppressed by tuning the feedback coefficient of the capacitor current. Also, good performance can be guaranteed with a wide range of voltage regulations, fast response, and no overshoot. The experimental platform of an 8/6 SRG system is built, and the experimental results show that the PT control can be used for SRG system with good practicability.

**Keywords:** switched reluctance generator; capacitance current pulse train control; voltage ripple; capacitance current; feedback coefficient

### 1. Introduction

With the rapid development of the economy energy shortages have become an inevitable problem. As a clean and abundant energy source, wind energy has been widely used. Wind power has the good features of wide distribution, large reserves, cleanness, security, etc. Therefore, wind power generation has attracted general attention from countries all over the world. Following this trend, there is a rapid development in wind power generation technologies and the wind power industry [1–3].

Switched reluctance generators (SRG) have advantages such as simple structure, high fault-tolerant ability, high operating efficiency, and hard mechanical properties, which make them widely used in aerospace, mining, textile, papermaking, and other industries [4–6]. The rotor of the SRG has no winding, no brush, and no permanent magnet so that the manufacturing cost is low and no copper loss is encountered. Since the SRG power generation system can be operated synchronously with a wind turbine, it is not restricted by stability issues when the frequency is low. Therefore, even if the wind speed is low, it can also ensure that the system runs with a high efficiency of power generation through reasonable design and control. At the same time, the application of current direct drives has become the developing trend of wind power generation systems, the advantages of SRG are attracting more and more attention than those of other generators. In particular, the magnetic and electric circuits are

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independent of each other, and hence when a fault occurs in a phase, the system can still function by isolating the faulty phase. Therefore, it has high operational reliability and fault tolerance [7].

The traditional PID control strategy is the classical method of power generation control for switched reluctance generators (SRGs) [8]. However, under PID control, the output overshoot of SRG could be large under the speed regulation, and the transient response could be quite slow due to the error compensation network [9]. In addition, PID controller parameters are normally preset and fixed, so the control performance will deteriorate when the working conditions are changed. It has been pointed out that the Fuzzy control strategy is suitable for SRG systems [10]. The fuzzy control theory refers to a bionic controller based on fuzzy knowledge and rule inference [11]. According to certain rules of inference, it can achieve the control goal in a simple way [12]. However, the independent use of a fuzzy controller may lead to an unavoidable overshoot and larger steady-state error. The sliding-mode variable structure control could also be a competitor for the control of SRGs. As compared with other control strategies, sliding-mode variable structure control has the invariance of perturbation and external disturbances to the system, making it more widely used in cases with high requirements of reliability and robustness [13]. However, the phenomenon of inherent buffeting and the inevitable steady-state error result in poor steady-state performance.

The large fluctuation of electricity loads and the regular capacitor charging and discharging processes lead to high difficulty of control for the irregular excitation current. In addition, an output voltage fluctuation can occur, and the original characteristics of power generation are affected. Besides, more harmonic contents could be injected into the grid by the grid-connected inverter. Until now, there has been some research progress of reducing the output voltage ripple and enhancing the voltage stability of SRG power systems. Aiming at reducing the output voltage ripple of SRG, a capacitor filter, as designed in a previous paper [14], is used to effectively reduce the voltage harmonics, but the parameters of the filter are difficult to determine. The switched reluctance generation system can achieve better control of the output voltage by introducing the double-closed-loop PID control with variable parameters [15]. However, the controller only considers the output voltage and phase current as the control targets, and hence ignores the impacts of other states of the system, which compromises the dynamic performance of SRG [16]. In a previous paper [17], a sliding mode controller of variable structure based on a genetic algorithm was designed to eliminate the voltage ripple caused by factors such as speed and load which change during the operation. However, the introduced genetic algorithm optimization module makes the system complicated.

Recently, pulse train (PT) control has been proposed for switching dc–dc converters [18,19] operated in the discontinuous conduction mode (DCM). The PT control method can adjust the system output voltage by using two or more sets of combination of control pulses. Without the requirement of an error amplifier and corresponding compensation network, the PT controller has excellent control performance of a fast response and simple circuit structure [20–22]. PT control methods are also attempted to be used in converters operated under the continuous conduction mode (CCM). In a previous paper [23], a buck converter operated in CCM is carried out with PT control for the first time, the research results point out that when the equivalent series resistance (ESR) of output capacitance is small, the circuit gives the phenomenon of low frequency oscillation. Though increasing the output capacitance ESR can suppress the low frequency oscillation of the converter, the ripple of output voltage is increased. To broaden the application scope of PT control, a peak capacitance current pulse train (PCC-PT) control method is described [24]. For the application of PCC-PT in converters, both excellent steady-state and transient response characteristics are revealed.

As a new contribution, a modified CC-PT control method is put forward based on the analysis of the conventional pulse train (PT) control, which is then applied in an SRG power generator system for the first time. The proposed CC-PT controlled method could adjust the output voltage by combining two or more groups of preset control pulses without the need of the error compensation network, which has the advantage of quick response compared with the PWM method.

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### 2. SRG Power Generation System

#### 2.1. Principle of SRG

The SRG is a doubly salient varied reluctant motor, and the salient poles of stators and rotors are superposed by the common silicon steel sheet [25]. Figure 1a shows the structure of a SRG, of which phase A is taken as an example to illustrate the principle of its power generation. The SRG rotates clockwise to the position as shown in Figure 1a under the external force (wind power), and the switches  $S_1$ ,  $S_2$  are closed, then excite phase A and form the circuit  $S_1 \rightarrow A \rightarrow A' \rightarrow S_2$ . Figure 1b shows the excitation and freewheeling phases: First, the winding of phase A absorbs electrical energy from the source. Then,  $S_1$  and  $S_2$  are switched off and the winding of phase A is subjected to freewheeling through the freewheeling diodes, thus feeding back the energy stored by the winding to the DC power supply.

Because both the excitation and armature windings of the SRG are stator windings, the process of excitation and power generation must be controlled periodically. Its excitation process is controllable, while the generation process is not controllable, so the power generation is commonly controlled by adjusting the excitation current.

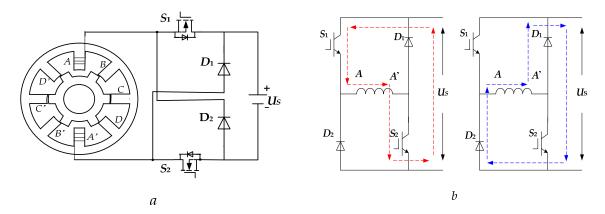


Figure 1. Principles of SRG. (a) Profile of 8/6 SRG; (b) two phases of SRG.

# 2.2. Control Methods of SRG

A SRG power generation system has two main excitation modes, which includes self-excitation and separate excitation. This paper chooses the separate excitation mode shown in Figure 2, which can separate the power generated by the winding from the excitation power completely and ensure high stability [26].

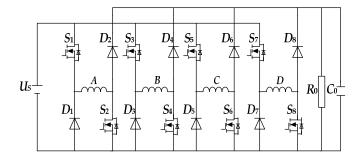


Figure 2. The main circuit structure diagram of separate excitation.

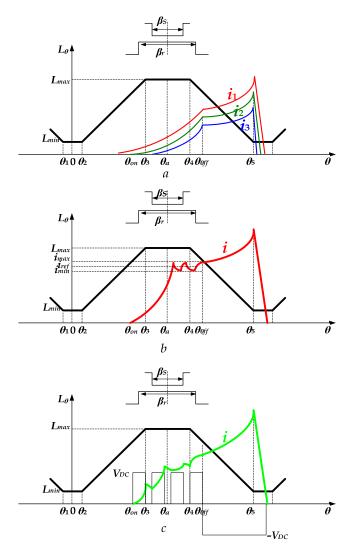
The control methods have been proposed for regulating the output power of SRG, such as angle position control (APC), current chopping control (CCC), and pulse width modulation (PWM).

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The APC control mode regulates the current waveforms by changing the turn-on angle  $(\theta_{on})$  and turn off angle  $(\theta_{off})$ . The output current can be changed by tuning the turn-on angle  $(\theta_{on})$  and turn off angle  $(\theta_{off})$ , as shown in Figure 3a. It can be seen that, higher conduction angles could lead to a larger output current. APC control can also be divided into the modes of changing  $\theta_{on}$ ,  $\theta_{off}$  and both  $\theta_{on}$  and  $\theta_{off}$  together [27].

CCC is a method that directly chops the phase currents during the specific position of each phase. In CCC, the current i is compared with the chopper current ( $i_{chop}$ ). When the rotor position angle is between  $\theta_{on}$  and  $\theta_{off}$ , where  $\theta_{on} < \theta < \theta_{off}$ , if  $I \le i_{chop}$ , the switches are turned on, then the current i rises and gradually reaches the chopper; or else, the switches are turned off and the current i declines, as shown in Figure 3b. As compared with the APC control, where the current is not controllable, CCC directly controls the phase current and can get more accurate control performance [28].

The PWM control applies the PWM modulation signals on the main switches and adjusts the excitation voltage by changing the duty cycle to realize the control of excitation current. The PWM control of SRG can also be divided into two methods: one uses the PWM cut double tubes, and the other uses the PWM cut single tube. These two methods adjust the size of the excitation current and ultimately realize the control of output voltage. The waveforms of phase current by using PWM control is shown in Figure 3.



**Figure 3.** The waveforms of the phase current using three control methods. (a) APC control method; (b) CCC control method; (c) PWM control method.

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#### 2.3. Analysis of Output Voltage Ripple of SRG

At the stage of building up the voltage field in the self-excited mode of SRG, the excited voltage source  $U_S$  provides an initial excitation voltage to the system. The self-excited mode generator system has heavy weight and high efficiency. However, when the loads fluctuate seriously and the capacitor charges or discharges, control difficulty of the irregular excitation current is encountered. The irregular excitation will finally result in the output voltage ripple, having an impact on the power generation performance and causing certain damage to the SRG's body that shortens the lifetime of SRG.

The voltage balancing equation of the kth phase winding is given by

$$U_k = R_k i_k + \frac{d\psi_k}{dt} \tag{1}$$

The phase inductance  $L_k(i_k, \theta)$  is a function of the phase current  $i_k$  and the rotor position angle  $\theta$ . Therefore, (1) can be converted to;

$$U_k = R_k i_k + L_k \frac{di_k}{dt} + i_k \omega \frac{dL}{d\theta}$$
 (2)

where  $U_k$  is kth phase output voltage,  $L_k$  is the phase inductance,  $\omega$  is the generator angular speed,  $R_k$  is the resistance of the phase winding, and  $i_k$  is the phase current.

In the nonlinear model, the voltage at generator windings in excitation and power generation are given by;

$$U_{k} = \begin{cases} i_{k}R_{k} + \frac{d\psi_{k}(i_{k},\theta)}{dt} \\ -i_{k}R_{k} - \frac{d\psi_{k}(i_{k},\theta)}{dt} \end{cases}$$
(3)

It is supposed that the load in the power generation state is R, and the voltage on capacitor is  $U_c$ . In the process of excitation, the capacitor supplies power to both the winding excitation and the load, which is expressed by the following equation;

$$C\left(\frac{dU_c}{dt}\right)\omega = -i_R - i_c \tag{4}$$

During the freewheeling process, the capacitor is charged by the winding and the capacitor supplies power to the load, which is expressed as;

$$C\left(\frac{dU_c}{dt}\right)\omega = -i_R - i_z \tag{5}$$

with  $i_z$  is the armature current.

From (3), the capacitance voltage  $U_c$  can be obtained, then the variation of the capacitance voltage  $\Delta U = \Delta U_c$  can be derived. Afterwards, the variation of the output voltage in the nonlinear model can be expressed by;

$$\Delta U = \Delta U_c(\theta_{on}) \left\{ \exp(-\theta_{off}/(\tau\omega)) - \exp(-\theta_{on}/(\tau\omega)) \right\} - Q/(C\omega)$$
 (6)

where  $\omega$  is the angular velocity of *SRG*,  $U_c$  is the capacitor voltage, R is the load resistance, and Q is the energy storage during the excitation phase,  $\tau = RC$ .

From (6), it can be seen that the parameters that affect the output voltage ripple include the capacitor voltage  $U_c$ , rpm of SRG n, load R, and capacitance C.

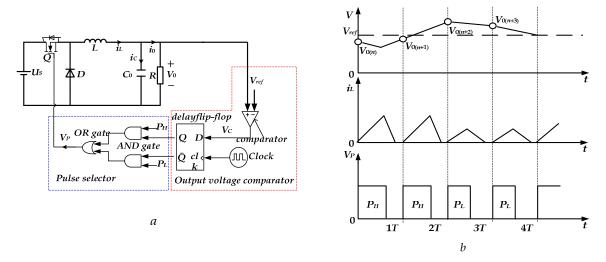
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#### 3. Capacitance Current Pulse Train Control

#### 3.1. The Principle of Pulse Train Control

The pulse train (PT) controlled method is put forward based on the linear control theory of the pulse width modulation (PWM) method [29]. The PT controlled method can adjust the output voltage by using two or more sets of a combination of preset control pulses, which has the advantages of simple circuit structure, no compensation network, and fast response. There is a wide application of the PT controlled method in systems with a switching power supply that need high performance [30,31]. Figure 4a shows the schematic diagram of the PT controlled buck converter.

A PT controller consists of a voltage comparator, clock signal, flip-flop delay, and logic gate circuit. The control circuit is simple and easy to implement [32]. The main work process is as follows. In the case that the  $n^{th}$  clock trigger signal comes, the comparator transfers the comparison  $V_0$  of the output voltage value and the reference value  $V_{ref}$  to delay the flip-flop. When  $V_0(n) < V_{ref}$ , the Q of delay flip-flop outputs 1,  $\overline{Q}$  outputs 0, and the pulse control chooses  $P_H$  as the effective control signal, which causes the converter to absorb more energy from the input  $U_S$ , forcing the output voltage to rise; similarly, when the  $(n+2)^{th}$  clock trigger signal comes, the sampling of the output voltage value is  $V_0(n+2)$ . Because  $V_0(n+2) > V_{ref}$ , the Q of delay flip-flop outputs 0,  $\overline{Q}$  outputs 1, and the pulse control chooses  $P_L$  as the effective control signal, where the converter absorbs less energy from the input  $U_S$ , forcing the output voltage to decline. The waveforms of the output voltage, inductance current, and control pulse are as shown in Figure 4b.



**Figure 4.** The principle of PT and CC-PT control. (a)VM-PT controlled Buck converter schematic; (b) schematic of working principle.

# 3.2. The Principle of Capacitor Current Train Pulse

As the full flow of current ripple flows into the output filter capacitance, the phase position of the inductance current ripple can be reflected through the capacitive current. By sampling the capacitive current of converter load side and adding the capacitive current to the output voltage as the condition of pulse choice, one can adjust the hysteresis of output voltage and realize the suppression of low frequency oscillation behavior [33,34].

The accurate circuit model of SRG does not calculate the electromagnetic torque, therefore the model is worthless. Here, the linear model of SRG is applied, since it excludes the influence of magnetic saturation, and the inductance of phase winding is irrelevant to the current. Therefore, the output voltage ripple can be decreased by controlling CC-PT.

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In a duty cycle, the inductance of phase is a function of rotor angle. The corresponding phase inductance of SRG in the linear model is expressed as:

$$L(\theta) = \begin{cases} L_{\min} & \theta_1 \le \theta < \theta_2 \\ \delta(\theta - \theta_2) + L_{\min} & \theta_2 \le \theta < \theta_3 \\ L_{\max} & \theta_3 \le \theta < \theta_4 \\ L_{\max} - \delta(\theta - \theta_4) & \theta_4 \le \theta < \theta_5 \end{cases}$$
(7)

where  $\delta = (L_{max} - L_{min})/\beta_S$ ,  $\beta_S$  is the arc angle of the stator.

Under the control of CC-PT, the structure of the phase of a SRG power generation system is shown in Figure 5.

The difference between the CC-PT controlled method and the traditional PT controlled method is in the matter of the sampling information. When the clock signal comes, the sampling circuit samples the output voltage  $V_0$  and the capacitor current  $i_c$  of the circuit, and the sampling results are compared with the reference voltage  $V_{ref}$ . When  $V_0 + \alpha i_c \leq V_{ref}$ , the pulse control chooses  $D_H$  as the effective control signal, which causes the winding of phase A to absorb more energy from the input  $U_S$ , forcing the output voltage to rise; when  $V_0 + \alpha i_c > V_{ref}$ , the pulse control chooses  $D_L$  as the effective control signal, where the converter absorbs less energy from the input  $U_S$ , forcing the output voltage to decline. The selection of pulse control is expressed as:

$$D = \begin{cases} D_H, \ V_0 + \alpha i_c \le V_{ref} \\ D_L, \ V_0 + \alpha i_c > V_{ref} \end{cases}$$
 (8)

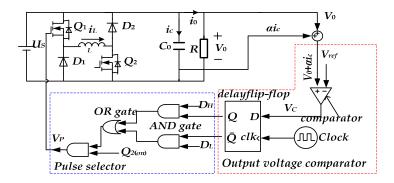


Figure 5. The structure of SRG power system under the control of CC-PT.

In the circuit shown in Figure 6, the conduction of switches is controlled by cutting the single pipe. Figure 6 shows the waveforms of winding current and output voltage when switch  $Q_2$  is conducted ( $\theta_2 \le \theta < \theta_5$ ). When switch  $Q_2$  is conducted, the inductance of winding changes with  $\theta$ , and the winding current is nonlinearly increased; when switch  $Q_2$  is turned off, the winding current is nonlinearly declined. When  $Q_1$  is on and  $\theta_2 \le \theta < \theta_4$ , the winding of phase A absorbs energy and is excited by  $U_5$ . When  $\theta_4 \le \theta < \theta_5$ , the winding of phase A converts the mechanical energy of the rotor to magnetic energy. When  $Q_1$  and  $Q_2$  are off, the magnetic energy stored in the magnetic field is released from phase A. Thus, the conversion between mechanical energy and electrical energy is completed in the form of magnetic energy.

The winding current  $i_L(\theta)$  satisfies the relationship with the current of the load  $i_0$ , which is given by;

$$i_{L(\theta)} = \begin{cases} \int_{t_{on}}^{t_{off}} \frac{U_{S}}{L(\theta)} dt & t_{on} \le t < t_{off} \\ i_{0} + C \frac{dU_{c}}{dt} & others \end{cases}$$
(9)

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where  $U_c$  is the instantaneous value of the output filter capacitor voltage.

The change of the output voltage (capacitance voltage) in a switching cycle can be determined by:

$$\Delta v_0(nT) = \frac{1}{C} \int_{nT}^{(n+1)} (i_L - i_0) dt$$
 (10)

According to Figure 6, the value of the integral item in the right-hand side of (10) equals the difference between the area of trapezium *ABCD* and that of the rectangle *ADFE*. The area of rectangle *ADFE* is given as:

$$S_{ADFE} = |\Delta i_L(nT)|T \tag{11}$$

The area of trapezium ABCD equals the sum of the areas of  $A_1$ ,  $A_2$ , and  $A_3$ . The area of  $A_3$  can be regarded as L, which equals the constant value  $L_0$ . The area of trapezium ABCD is expressed as

$$S_{ABCD} = S_{ABG} + S_{BCDG} + A_1 + A_2$$

$$= \frac{1}{2}DT \frac{U_S - V_0}{L_0}DT + \frac{1}{2} \left( \frac{U_S - V_0}{L_0}DT + \frac{U_S D - V_0}{L_0}T \right) (1 - D)T + A_1 + A_2$$

$$= \frac{T^2}{2L_0} \left[ (U_S D - V_0) + U_S D(1 - D) \right] + A_1 + A_2$$
(12)

From (10) to (12), the change in the output voltage can be derived as

$$\Delta v_0(nT) = \frac{T^2}{2L_0C} [(U_S D - V_0) + U_S D(1 - D)] + \frac{\Delta i_L(nT)T}{C} + Z_1$$

$$= Z_1 + Z_2 + \frac{i_c(nT)T}{C}$$
(13)

with 
$$Z_2 = \frac{T^2}{2L_0C}[(U_SD - V_0) + U_SD(1 - D)], Z_1 = \frac{S_1 + S_2}{C}.$$

Since  $T^2 \ll LC$ , from (13), the change in the output voltage can be approximately expressed as

$$\Delta v_0(nT) \approx \frac{i_c(nT)T}{C} \tag{14}$$

The PT controlled method adjusts the output voltage through adjusting the current of winding indirectly. When the output voltage is larger than the reference voltage, the PT controller chooses  $D_H$  as the control signal, and the output voltage may vary. Similarly, when the output voltage is lower than the reference voltage, the PT controller selects  $D_L$  as the control signal, and the output voltage may vary as well. The phenomenon of voltage hysteresis leads to the occurrence of low frequency fluctuations in PT control. It can be seen from (14) that the change of output voltage in a switching cycle is mainly determined by  $i_c(nT)$ . The output voltage increases when  $i_c(nT) > 0$ , otherwise the output voltage declines.

The above analysis shows that the phenomenon of low frequency fluctuations is caused by not adjusting the output voltage in a timely fashion. If the output voltage rises when the system chooses  $D_H$ , or it declines when the system chooses  $D_L$ , the low frequency fluctuations can be suppressed. As the full flow of the current ripple of the winding flows into the output filter capacitance, the phase position of the inductance current ripple can be reflected in the capacitive current. In addition, as can be seen from (14), the value of output filter capacitance only affects the output voltage.

From (14), it can be seen that;

$$\Delta v_0(nT) = \frac{T^2}{2L_0C} [(U_S D - V_0) + U_S D(1 - D)] + \frac{\Delta i_L(nT)T}{C}$$
(15)

where  $i_L(n)$  is the inductance current at the beginning of the  $n^{th}$  switching cycle.

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From (15) and the working principle of PT controlled method, the synchronous switching mapping equation of the output voltage and inductance current under the control of CC-PT is shown as:

$$Y_{n+1} = \begin{cases} AY_n + B^H, CY_n \le V_{REF} \\ AY_n + B^L, CY_n > V_{REF} \end{cases}$$
 (16)

where:

$$A = \begin{bmatrix} 1 - \frac{T^2}{2LC} - \frac{T}{RC} & \frac{T}{C} \\ -\frac{T}{L} & 1 \end{bmatrix}, Y_{n+1} = \begin{bmatrix} v_0(n+1) \\ i_L(n+1) \end{bmatrix}, \quad Y_n = \begin{bmatrix} v_0(n) \\ i_L(n) \end{bmatrix},$$

$$B^H = \begin{bmatrix} \frac{U_S D_H T^2 (2 - D_H)}{U_S D_H T} \\ \frac{U_S D_L T}{L} \end{bmatrix}, B^L = \begin{bmatrix} \frac{U_S D_L T^2 (2 - D_L)}{U_S D_L T} \\ \frac{U_S D_L T}{L} \end{bmatrix}, C = \begin{bmatrix} 1 - \frac{\alpha}{R} & \alpha \end{bmatrix}$$

According to (16), when the system parameters are determined, the combination of high and low pulse signals in a pulse cycle is determined as well. The inductance currents of windings and the output voltage change as the feedback coefficient of the capacitor and the value of load resistance change in each switching cycle, which results in the change of the combination of high and low pulses in the pulse cycle. The Lyapunov exponent function of the CC-PT control system is obtained as:

$$\lambda(\alpha, R) = \ln \left| 1 - \frac{T^2}{2LC} - \frac{T}{RC} \right| \tag{17}$$

 $\lambda$  is always less than 0, which indicates that the CC-PT controlled system is in the steady working state when the capacitance current regulation coefficient  $\alpha$  and load resistance R change. The output voltage of the system is oscillating at the base level and is measured by defining the standard deviation, which is expressed as:

$$\sigma(\alpha, R) = \sqrt{\frac{1}{N} \sum_{i=1}^{N} \left[ v_{oi}(\alpha, R) - V_{0ref} \right]}$$
(18)

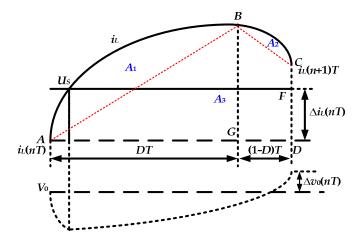


Figure 6. The waveforms of winding current and output voltage during a switching cycle.

# 4. Optimization of Power Generation Efficiency of SRG

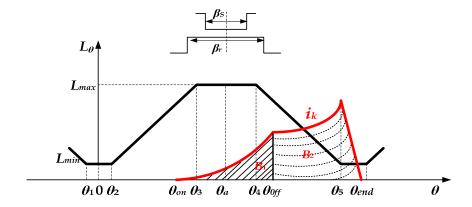
As shown in Figure 7, the ratio of the total instantaneous current value during the phase of electric power generation and excitation is calculated to measure the efficiency of power generation, which is named as  $\varepsilon$ , and it is obtained by;

$$\varepsilon = \frac{B_1}{B_2} = \frac{\int_{\theta_{on}}^{\theta_{end}} i_k d\theta}{\int_{\theta_{on}}^{\theta_{off}} i_k d\theta} \tag{19}$$

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where  $i_k$  is the current of phase k.

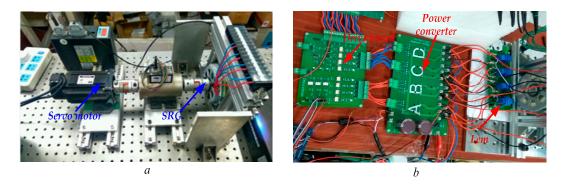
Therefore,  $\varepsilon$  can be obtained simply by calculating the integration of the phase generation current and the excitation current. In practical applications,  $\theta_{on}$ ,  $\theta_{off}$ , and  $\theta_{end}$  are needed, and the total instantaneous current value during the phase of electric power generation and excitation is calculated, which can be used to determine the efficiency of power generation.



**Figure 7.** The schematic diagram of  $\varepsilon$ .

#### 5. Experiment Model and Verification

In order to verify the validity of theoretical analysis, this paper has constructed a platform of 8/6 SRG power generation shown in Figure 8a,b which is based on the analysis of SRG and CC-PT control.

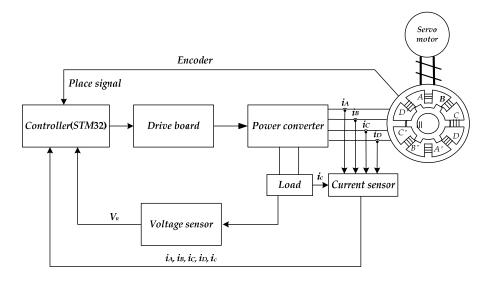


**Figure 8.** The photograph of the experimental platform of SRG power generation. (a) Experiment platform of SRG; (b) control circuits and the power converter.

Figure 9 shows the control scheme of the 8/6 SRG system. It consists of a SRG, a servo motor, a drive board, controller (STM32), and so on. The main parts of the circuit are the encoder and sensors, which detect the location of the rotors, the values of current  $i_A$ ,  $i_B$ ,  $i_C$ ,  $i_D$ ,  $V_0$ , and  $i_c$ , where  $i_c$  is the current though the filter capacitor.

The detail control of PI and CC-PT are shown in Figure 10. It can be easily seen when  $Q_2$  is open, which is controlled by the APC controller, and determined by the value of  $\varepsilon$  (the efficiency of power generation). The PI control uses the difference of  $V_0^*$  and  $V_0(t)$  to form a voltage loop and the PT control leads  $i_c$  into the control. By limiting the overshoot of  $i_c$ , the ripple of  $U_{C0}$  is reduced. Figure 11 shows the working principle flowchart of the STM32 controller.

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**Figure 9.** The control scheme of the 8/6 SRG system.

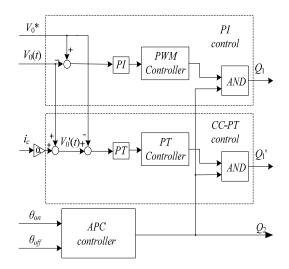
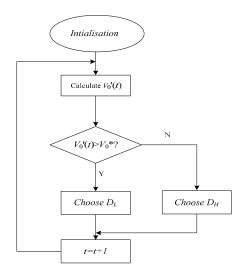


Figure 10. SRG controller.

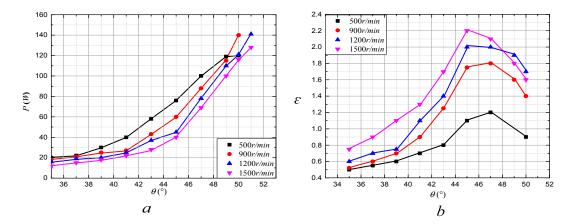


**Figure 11.** Flowchart of the *STM*32 controller.

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Figure 12a shows the trend of generation power at different speeds and different  $\theta_{off}$  when  $\theta_{on} = 20^{\circ}$ . From Figure 12a, it can be seen that at a certain speed, the generation power of SRG gradually increases with the increase of  $\theta_{off}$ .

Figure 12b shows the trend of  $\varepsilon$  with the change of  $\theta_{off}$  and speed. It can be seen that  $\varepsilon$  increases as  $\theta_{off}$  increases at different speeds. However, when  $\theta_{off}$  reaches a certain value, the value of  $\varepsilon$  decreases, according to which, the optimal  $\theta_{off}$  can be determined, as well as the optimal net generation power. The optimal  $\theta_{off}$  at different speeds with the condition of constant  $\theta_{on}$  are shown in Table 1. In the same way, the optimal  $\theta_{on}$  can be obtained at different speeds with the condition of constant  $\theta_{off}$ , which is also shown in Table 1.



**Figure 12.** Optimize the  $\theta_{off}$ . (a) The trend of generation power; (b) the trend of  $\varepsilon$ .

**Table 1.** The optimal  $\theta_{on}$  and  $\theta_{off}$ .

n, r/min	$\theta_{on}$ , deg	$\theta_{\it off}$ , deg
500	25	47
900	23	47
1200	25	45
1500	25	45

From (18), the feedback coefficient of capacitor  $\alpha$  with i ranging from 0 to 1, and the value of the load resistance R with i ranging from 0 to 10, are combined as parameters. With the change of feedback coefficient, the output voltage error approximation is small when the feedback coefficient is larger than 0.2, and the low frequency oscillation can be suppressed by the CC-PT controlled method. In this paper, the PI parameters of traditional PWM control is determined by the critical ratio method (P = 0.5, I = 0.032). In order to compare the ripple of the output voltage with that under PI control, a small capacitor is used in the experiment, the capacitance of which is 680 uF.

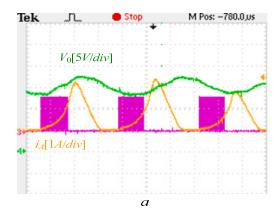
In summary, the parameters used in the experiment are shown in Table 2.

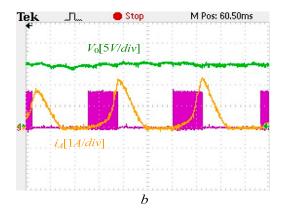
Table 2. Parameters of experiment model.

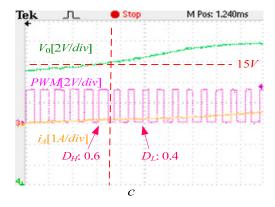
D (	<b>3</b> 7.1	.1 D	
Parameters	Value	Parameters	Value
m	4	$R, \Omega$	8
Ns	8	C, uF	680
$N_r$	6	P	0.5
Us, V	80	I	0.032
n,r/min	1200	$D_H$	0.6
$\theta_{on}$ , deg	25	$D_L$	0.4
$\theta_{off}$ , deg	45	f, Hz	6000

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When the desired output voltage  $V_0 = 15$  V and the load R = 8  $\Omega$ , the experiment waveforms of  $V_0$  under PWM control are shown in Figure 13a. It can be seen from Figure 13a, when the SRG runs at a stable state with a constant speed n = 1200 r/min, the ripple of  $V_0$  is large, which is up to 5 V.







**Figure 13.** The experiment waveforms of SRG. (a) Experiment waveforms of output voltage  $V_0$  under PWM control; (b) experiment waveforms of output voltage  $V_0$  under PT control; (c) the details of experiment waveforms under PT control.

The parameters of the SRG power generator system under the PT controlled method are:  $D_H = 0.6$ , DL = 0.4, and f = 6 kHz. Figure 13b shows the experiment waveforms of  $V_0$  under the PT controlled method. The ripple of  $V_0$  is smaller than that obtained by applying the PI controlled method, but the ripple is still up to 2 V.

Figure 13c shows the details of the PT controlled method. It can be seen that when  $V_0$  is smaller than the target value of 15 V, the controller chooses the PWM scheme with  $D_H = 0.6$ , and the output

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voltage increases. On the other hand, when the value of  $V_0$  is larger than 15 V, the controller chooses the PWM scheme with  $D_L = 0.4$  to decrease the output voltage value.

Figure 14 shows the experiment waveforms of  $V_0$  under the CC-PT controlled method. The coefficient of ratio  $\alpha$  is 1. From (14), the ripple of output voltage  $\Delta v_0(nT)$  can be calculated. The largest  $\Delta v_0(nT)$  is about  $\pm 0.49$  V. It can be seen from Figure 14 that the ripple of  $V_0$  is the smallest among these three controlled methods. The value of the output voltage ripple is about 1 V, which is consistent with the calculation results of (14).

In order to investigate the response of the SRG system starting process, a larger filter capacitance is used in the experiment and the value of it is 0.27 F. Figure 15 shows the starting processes under the control of PI and CC-PT.

It can be easily seen that the output voltage derived by applying the PI controlled method takes about 1.4 s to achieve a stable state. However, the output voltage obtained by using the CC-PT controlled method only takes about 0.7 s to achieve a stable state. Therefore, the system under the CC-PT controlled method responds more quickly than that under the PI controlled method. Meanwhile, from Figure 15, it also can be seen that  $V_0$  has a bigger overshoot under the control of PI control, but there is nearly no overshoot of  $V_0$  under the control of the CC-PT control. The ripple of  $V_0$  derived by the CC-PT controlled method is smaller than that obtained by the PI controlled method.

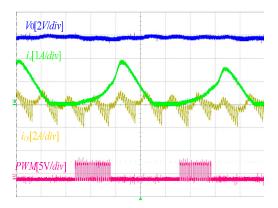


Figure 14. The experiment waveforms of output voltage under CC-PT control.

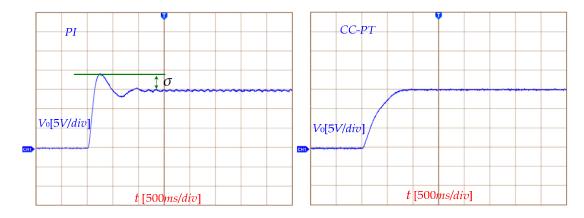


Figure 15. The starting process under the control of PI and CC-PT.

### 6. Conclusions

Based on the traditional PT control, a CC-PT controlled method is proposed in this paper to improve the performance of an SRG power system. Through experiment verification, as compared with the traditional SRG power generation system under PWM control, the CC-PT controlled SRG has the following advantages:

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(a) The CC-PT controlled method can adjust the output voltage by using two or more sets of combinations of preset control pulses, which has the advantages of simple circuit structure and no compensation network.

- (b) The SRG power generation system under the CC-PT controlled method can realize a fast response during start-up. By reasonably configuring the value of  $D_H$ , the output voltage overshoot can be eliminated.
- (c) The start-up phase current is reduced, which makes the system more secure and cost saving. The output voltage ripple is smaller than 5% of the rated value.

**Author Contributions:** X.Z. and D.Y. suggested the method of CC-PT control used in SRG generation system; M.C. and R.X. analyzed the data. M.C. and X.Z. wrote the paper. K.N. reviewed and edited.

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Conflicts of Interest: The authors declare no conflicts of interest.

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